

Pose from a planar target - Stéphane Maillot

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Homography computation

```
im = imread('mvg.bmp');
corners_pic = [ 345, 218 ; 50, 286 ; 383, 424 ; 565, 169 ; 325, 119 ];
l = 17.3;
L = 24.6;
corners_real = [ 0, 0 ; -l/2, -L/2 ; l/2, -L/2 ; l/2, L/2 ; -l/2, L/2 ];
imshow(im)
hold on;
plot(corners_pic(:,1), corners_pic(:,2), '.r', 'MarkerSize', 15)

[u, s, v] = svd(DLT_system(corners_pic, corners_real));
s
```

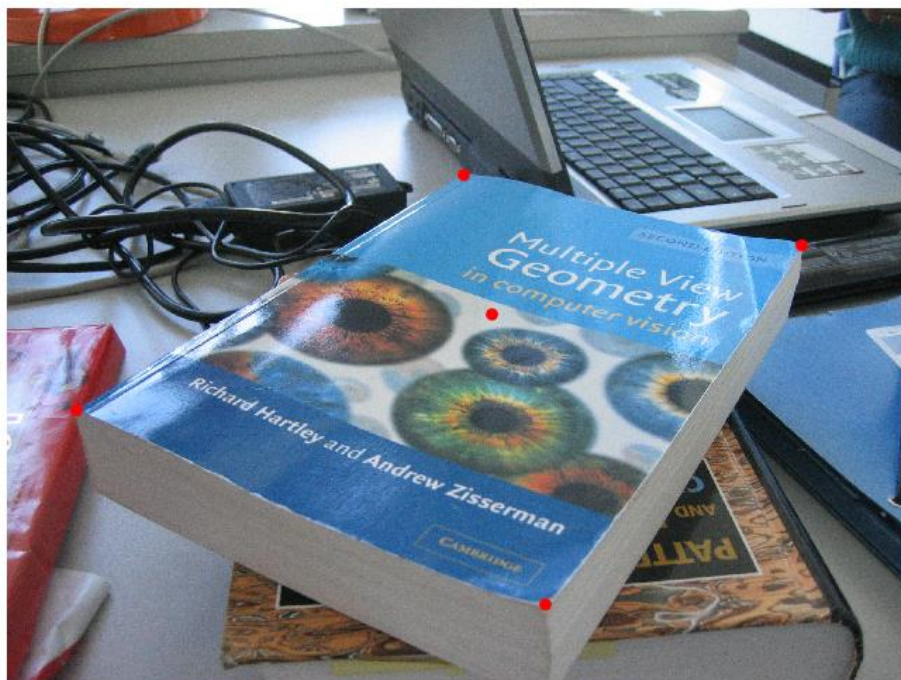
S =

1.0e+04 *

Columns 1 through 9

1.1529	0	0	0	0	0	0	0	0
0	0.8120	0	0	0	0	0	0	0
0	0	0.0886	0	0	0	0	0	0
0	0	0	0.0023	0	0	0	0	0
0	0	0	0	0.0017	0	0	0	0
0	0	0	0	0	0.0012	0	0	0
0	0	0	0	0	0	0.0006	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0.0002	0
0	0	0	0	0	0	0	0	0.0000

The last column of V will then be the kernel of this matrix.



```
ker = v(:,end);
H = reshape(ker, 3, 3)'
```

H =

```
    0.0295    0.0393    0.8430
    0.0047   -0.0084    0.5356
   -0.0000    0.0000    0.0024
```

If we use $-H$, the Z-axis will be reversed.

Pose estimation

```
A = [ 800, 0, 320 ; 0, 800, 240 ; 0, 0, 1 ]
G = A^-1 * H;
R1 = G(:,1);
R2 = G(:,2);
R3 = cross(R1, R2);
t = G(:,3);
```

A =

```
800    0    320
  0    800   240
  0     0     1
```

Normalization

```
l = sqrt(norm(R1) * norm(R2));
R1 = R1 / l;
R2 = R2 / l;
t = t / l
c = R1 + R2;
d = cross(c, R3);
R1 = 1 / sqrt(2) * (c / norm(c) + d / norm(d));
R2 = 1 / sqrt(2) * (c / norm(c) - d / norm(d));
R3 = cross(R1, R2);
R = [R1, R2, R3]
```

t =

```
1.2424
-1.0812
40.7744
```

R =

```
0.8770    0.4804   -0.0048
0.2156   -0.4025   -0.8897
-0.4294    0.7792   -0.4566
```

As R and t are the rotation and translation to convert a point in the book coordinates into camera coordinates.

$C = -R't$ is the coordinate of the camera in the book frame.

```
C = -R'*t
P = A * [R, t]
```

C =

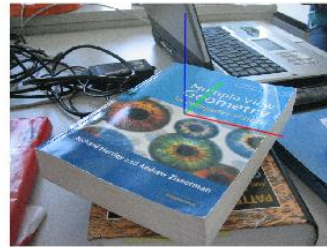
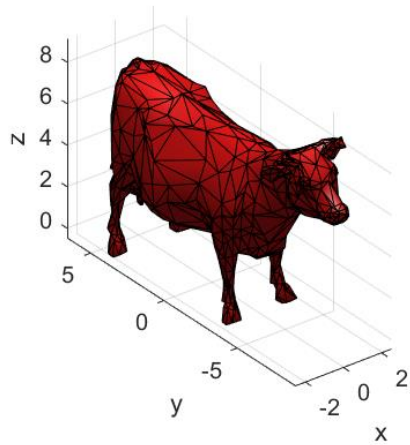
```
16.6501
-32.8042
17.6612
```

P =

```
1.0e+04 *  
  
    0.0564    0.0634   -0.0150    1.4042  
    0.0069   -0.0135   -0.0821    0.8921  
   -0.0000    0.0001   -0.0000    0.0041
```

Projection of a virtual object

```
load('model3d-cow.mat','fv');  
v=fv.vertices;  
F=fv.faces;  
nV = size(v, 1);  
  
%rotate and translate model 3d to align it with the book  
v = v * rotx(-90);  
v = v * rotz(90);  
v = v + [0, 0, 5];  
  
%plot original model in 3D  
figure; subplot(1,2,1);  
trisurf(F,v(:,1),v(:,2),v(:,3),'FaceColor',[1,0.1,0.1],...  
        'EdgeColor',[0.0 0.0 0.0]);  
light('Position',[-1.0,-1.0,100.0],'Style','infinite');  
lighting phong;  
xlabel('x');  
ylabel('y');  
zlabel('z');  
axis equal;  
  
%project model onto the image  
frame = [ 0, 0, 0 ; 10, 0, 0 ; 0, 10, 0 ; 0, 0, 10];  
  
frame = (P * [frame, ones(4, 1)]')';  
frame = frame(:,1:2) ./ frame(:,end);  
  
proj = (P * [v, ones(nV, 1)]')';  
proj = proj(:,1:2) ./ proj(:,end);  
uCow = proj(:,1);  
vCow = proj(:,2);  
  
%plot projected model in 2D  
subplot(1,2,2); imshow(im);  
line([frame(1,1), frame(2,1)], [frame(1,2), frame(2,2)], 'color', 'r')  
line([frame(1,1), frame(3,1)], [frame(1,2), frame(3,2)], 'color', 'g')  
line([frame(1,1), frame(4,1)], [frame(1,2), frame(4,2)], 'color', 'b')
```



```
color= repmat([1,0.1,0.1],nV,1);
fv2d.vertices=[uCow,vCow];
fv2d.faces=F;
fv2d.facevertexcdata=color;
p = patch(fv2d,'FaceAlpha',1,'EdgeAlpha',0.25);
shading faceted;
```

