

$z$	$erf(z)$	$z$	$erf(z)$	$z$	$erf(z)$
0	0	0.55	0.5633	1.3	0.9340
0.025	0.0282	0.60	0.6039	1.4	0.9523
0.05	0.0564	0.65	0.6420	1.5	0.9661
0.10	0.1125	0.70	0.6778	1.6	0.9763
0.15	0.1680	0.75	0.7112	1.7	0.9838
0.20	0.2227	0.80	0.7421	1.8	0.9891
0.25	0.2763	0.85	0.7707	1.9	0.9928
0.30	0.3286	0.90	0.7970	2.0	0.9953
0.35	0.3794	0.95	0.8209	2.2	0.9981
0.40	0.4284	1.0	0.8427	2.4	0.9993
0.45	0.4755	1.1	0.8802	2.6	0.9998
0.50	0.5205	1.2	0.9103	2.8	0.9999

$$\begin{aligned}
C_0 &= 0.25 \text{ wt\% C} \\
C_s &= 1.20 \text{ wt\% C} \\
C_x &= 0.80 \text{ wt\% C} \\
x &= 0.50 \text{ mm} = 5 \times 10^{-4} \text{ m} \\
D &= 1.6 \times 10^{-11} \text{ m}^2/\text{s}
\end{aligned}$$

Thus,

$$\frac{C_x - C_0}{C_s - C_0} = \frac{0.80 - 0.25}{1.20 - 0.25} = 1 - \operatorname{erf} \left[ \frac{(5 \times 10^{-4} \text{ m})}{2\sqrt{(1.6 \times 10^{-11} \text{ m}^2/\text{s})(t)}} \right]$$

$$0.4210 = \operatorname{erf} \left( \frac{62.5 \text{ s}^{1/2}}{\sqrt{t}} \right)$$

We must now determine from Table 5.1 the value of  $z$  for which the error function is 0.4210. An interpolation is necessary, as

$z$	$\operatorname{erf}(z)$
0.35	0.3794
$z$	0.4210
0.40	0.4284

$$\frac{z - 0.35}{0.40 - 0.35} = \frac{0.4210 - 0.3794}{0.4284 - 0.3794}$$

or

$$z = 0.392$$

Therefore,

$$\frac{62.5 \text{ s}^{1/2}}{\sqrt{t}} = 0.392$$

and solving for  $t$ , we find

$$t = \left( \frac{62.5 \text{ s}^{1/2}}{0.392} \right)^2 = 25,400 \text{ s} = 7.1 \text{ h}$$