

General Relativity vs Light

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December 25, 2022

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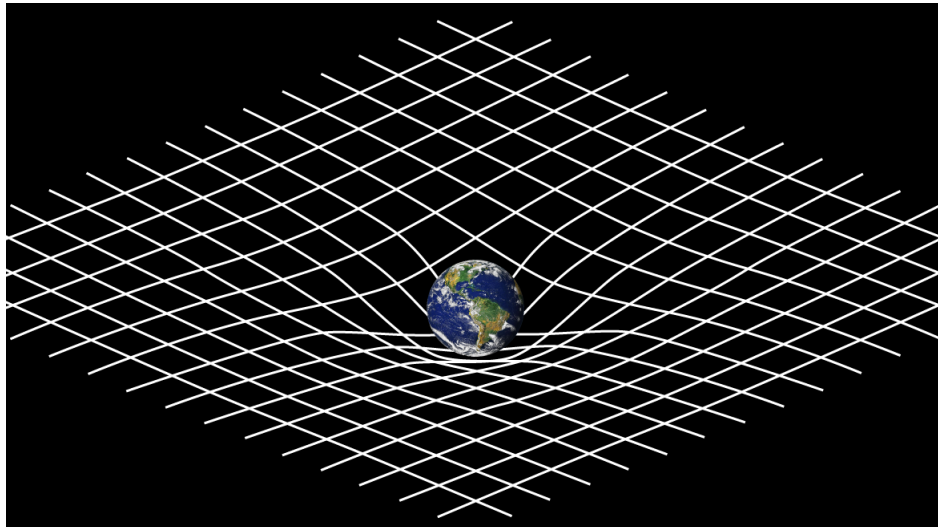
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1 General Relativity

Albert Einstein's theory of general relativity is based on the idea that massive objects cause a distortion in space-time. The image below exhibits a clear representation of what that distortion looks like.



2 Waves

2.1 Mechanical Waves

A mechanical wave is an [oscillation](#) of matter and is responsible for the transfer of energy through a medium. (Note: Light is not a mechanical wave because it is not matter. The particles that make up light ([photons](#)) have no mass.)

2.1.1 Different Types of Mechanical Waves

In total there are *three* general forms of mechanical waves. These waves are: Transverse Waves, Longitudinal Waves, and Combined Waves.

2.2 Electromagnetic Waves

Electromagnetic waves are those created by [oscillating](#) electric and magnetic fields. A great example of an electromagnetic wave is light. Light has two components: vertical and horizontal (electric and magnetic field oscillation). This combination results in an electromagnetic wave.

2.2.1 Different Types of Electromagnetic Waves

In total there are *seven* general forms of electromagnetic waves. These waves are: Radio Waves, Microwaves, Infrared, Visible, Ultraviolet, X-Ray, and Gamma Rays.

2.3 Gravitational Waves

First proposed by Albert Einstein in 1916 following his famously recognized [Theory of General Relativity](#), gravitational waves are ripples in space-time (the fabled “fabric” of the Universe) caused by massive objects moving with extreme accelerations.

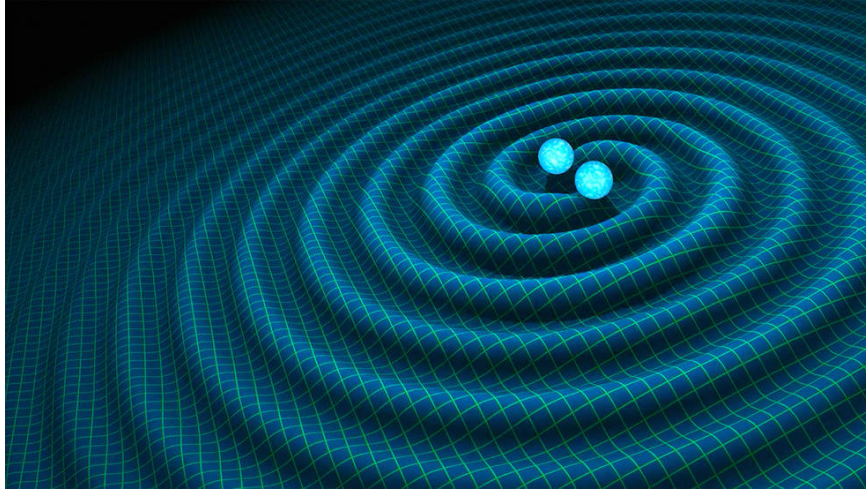
Over 20 years later in 1936, Albert Einstein and Nathan Rosen submitted a manuscript famously contradicting their theory of gravitational waves. This is because gravitational waves were theoretically possible, though they were thought to be physically impossible.

Gravitational waves were later proved to be existent, though it was determined that their effect by the time they reached us would be so weak, detecting them would be nearly impossible. However, in 2015, the Laser Interferometer Gravitational-Wave Observatory (LIGO) detected gravitational waves from the collision of two black holes.

Gravitational waves are formed by, as an example, also described above, two black holes orbiting each other, both getting closer and closer together until they collide.

2.3.1 Gravitational Wave Visualization

Gravitational waves are a very difficult concept to visualize. The following image is a basic visualization of gravitational waves. The two light-blue spheres are, for example, black holes. Their circulation around each other leaves ripples in spacetime.



2.4 Matter Waves

Matter waves are a central part of the theory of quantum mechanics, being an example of wave-particle duality. All matter exhibits wave-like behavior. The matter waves describes the relationship between momentum and wavelength.

3 Light

3.1 Wave Velocity

The speed of an electromagnetic wave (therefore light waves) is dependant on the wave length and freuency. The measure of the waves velocity can be calculated by the following equation: $v = \lambda f$ where v is the velocity, λ is the wave length, and f is the frequency. The units of velocity are meters per second (m/s).

3.2 Components

A light wave is made up of two components: electric and magnetic fields. These components can also be represented as vertical and horizontal vectors. These

vectors later appear in the polarization of light waves.

3.3 Films

Films allow the light wave to refract and reflect along the innerds of the film. This causing the reflecting light wave (the wave hitting the screen) to either constructively or destructively interfere.

3.4 Polarization

The polarization of a light wave allows for either the vertical or horizontal components of a wave to be eliminated. This elimination removes a minimum of 50% of the lights' brightness.

3.5 Gravitational Lensing

Following Einstein's [Theory of General Relativity](#), light can be bent by gravity. This bending is known as gravitational lensing. Through gravitational lensing, lights path around the electromagnetic field of an extensively large mass (eg. a neutron star) is curved.

3.5.1 Gravitational Micro-Lensing

Gravitational micro-lensing allows astronomers to detect objects that would otherwise be hidden in our vast universe (ie. a black hole). To detect a black hole, taken from a discovery by astronomers in 2019, the light of a star was observed to be distorted by the gravitational lensing of a black hole.

3.5.2 So how does it work?

The best way to describe gravitational lensing is through the visualization of a bowling bowl circulating a pit. Because of the momentum of the bowling

ball and the curvature of the pit, the ball doesn't just simply fall into the pit, instead, it curves around it. (ie. light around an object of extensively large mass which forms a distortion in space-time) See [Theory of General Relativity](#)

3.6 Light - A Particle and Wave

Not only is light a wave, but it is also a particle. This is known as wave-particle duality which is an essential theory derived from electromagnetics in quantum mechanics.

3.6.1 Light as a Wave

Combatting Isaac Newton's belief that light is a particle was Christiaan Huygens who had instead proposed that light was a wave. At the time Huygens wasn't able to prove his theory. It wasn't until 123 years later (1678 to 1801) that Thomas Young proved light was a wave through his Double Slit experiment.

3.6.2 Light as a Particle

Albert Einstein's quantum theory of light proposes that light is a series of [photons](#), and the flow of [photons](#) is a wave. Einstein's essential point is that light's energy is directly related to its [oscillation](#) frequency.

4 Planck's Constant

5 Neutron Stars

5.1 Pulsars

6 Black Holes

6.1 Formation

6.2 Light vs Black Holes

The gravitational pull of a black hole is so powerful that not even light can escape its grasp. However, while light cannot escape a black hole, its extreme gravity warps space around it, which allows light to bend around the object.

See [Gravitational Lensing](#)

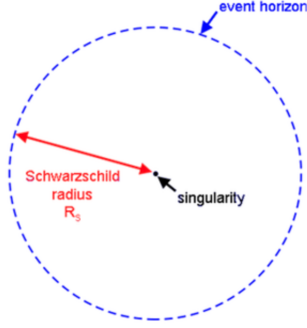
6.3 Schwarzschild Radius

6.3.1 What is it?

The Schwarzschild radius is the radius at which a mass has an escape velocity (the velocity required to escape a planets atmosphere) equal to the speed of light. Any object that is smaller than its Schwarzschild radius is a black hole. This is because any object with an escape velocity greater than the speed of light is a black hole.

6.4 Visualization

The following image is a visualization of a black hole and it's Schwarzschild radius.



6.4.1 Schwarzschild Radius Equation

The Schwarzschild radius is calculated using the equation: $R_S = \frac{2GM}{c^2}$ where R_S is the Schwarzschild radius, G is the gravitational constant ($6.67 \times 10^{-11} \frac{Nm^2}{kg^2}$), M is the mass of the object, and c is the speed of light ($\approx 299,792,458 \frac{m}{s}$). The units of the Schwarzschild radius are meters (m).

6.5 Gravitational Force

The gravitational force of a black hole can be calculated using the equation: $F_g = \left(\frac{G \times M}{r^2}\right)$ where F_g is the gravitational force, G is Newtons gravitational constant ($6.67 \times 10^{-11} \frac{Nm^2}{kg^2}$), M is the mass of the black hole, and r is the radius of the black hole (found using the [Schwarzschild Radius Equation](#)). The units for gravitational force in this solution are Newtons per Kilogram ($\frac{N}{kg}$).

6.6 Solving for the Gravitational Force

6.6.1 Variables

- *Given* : $G = 6.67 \times 10^{-11} \frac{Nm^2}{kg^2}$
- *Given* : $M = 1.989 \times 10^{30} kg$
- *Solved for* : $R_S = 2.95 \times 10^3 m$

- Find : $F_g = \left(\frac{G \times M}{r^2}\right)$

6.6.2 Solve for Schwarzschild Radius

$$\therefore R_S = \frac{2GM}{c^2} = \frac{2(6.67 \times 10^{-11})(1.989 \times 10^{30})}{(299,792,458)^2} \approx 2.95 \times 10^3 \text{ m}$$

\therefore The Schwarzschild Radius (R_S) is approximately $2.95 \times 10^3 \text{ m}$

\therefore The Black Hole Radius (r) is approximately $< 2.95 \times 10^3 \text{ m}$

6.6.3 Solve for Gravitational Force

$$\therefore F_g = \left(\frac{G \times M}{r^2}\right) = \left(\frac{(6.67 \times 10^{-11})(1.989 \times 10^{30})}{(2.949 \times 10^3)^2}\right) \approx 4.5 \times 10^{13} \frac{N}{kg}$$

\therefore The Gravitational Force (F_g) is approximately $4.5 \times 10^{13} \frac{N}{kg}$

6.7 Gravity of a Black Hole vs Earth

The gravitational force (F_g) in a black hole is approximately $4.5 \times 10^{13} \frac{N}{kg}$ whereas the gravitational force here on earth is approximately $9.81 \frac{N}{kg}$. This means that the gravitational force in a black hole is approximately $4.6 \times 10^{12} \frac{N}{kg}$ times greater than the gravitational force here on earth.

6.8 Singularities

6.9 Quarks in Black Holes

6.10 Event Horizon

6.11 Hawking Radiation

6.12 Black Hole Information Paradox

7 White Holes

8 Worm Holes

9 String Theory

10 Constants

- Speed of Light: $c \approx 299,792,458 \frac{m}{s}$
- Gravitational Constant: $G \approx 6.67 \times 10^{-11} \frac{Nm^2}{kg^2}$

11 Word Bank

11.1 Oscillation

The movement back and forth at a regular speed. Regular variation in magnitude or position around a central point.

11.2 Photons

A packet of electromagnetic energy with no mass nor any charge. A photon is a particle. A photon is the smallest unit of light.