

# Advanced Computer Vision

## Exercise Sheet 11

Winter Term 2022  
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Available: 30.01.2023  
Hand in until: 06.02.2023, until 23:59  
Exercise session: 09.02.2023

### Task 1 – A graph neural network forward pass

[20 points]

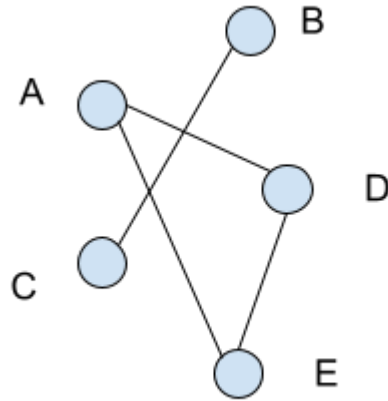


Figure 1: Graph neural network

Figure 1 shows a graph neural network topology with nodes indicated by alphabetical letters. The edges show the connectivity between the nodes. Given, the input features and weight matrices at input layer  $l = 0$ , the task is to compute the forward pass to obtain the node embeddings for  $l = 1$ .

The input features  $h_A^0$  to  $h_E^0$  ( superscript 0 refers to the layer  $l = 0$  ) respectively are :  $h_A^0 = [2, 1]^T$ ,  $h_B^0 = [0.03, 2]^T$ ,  $h_C^0 = [4, 1.75]^T$ ,  $h_D^0 = [-6.78, 1.02]^T$  and  $h_E^0 = [-1, 1]^T$ .

Following the notations in the lecture ( see slides 19 – 26 ), the weight matrices are :

- $W_0 = \begin{bmatrix} 1 & 2.01 \\ 2.3 & 3.4 \\ 1.7 & -0.91 \end{bmatrix}$
- $B_0 = \begin{bmatrix} -1.13 & 0.05 \\ 3.46 & 1.14 \\ -2.72 & 0.002 \end{bmatrix}$

Compute the node embeddings  $h_A^1$  to  $h_E^1$  using the equation specified on slide 20 of the lecture slides.. This task can be performed even without using a package like tensorflow or pytorch, using only numpy. Please note that there is no sample notebook for this task.

**HINT:** Try to be creative. Think of how you can achieve the computations using elementary matrix operations in a succinct way using numpy.

**Task 2 – A graph neural network with different aggregation functions** [30 points]

In this task, you will use the same network structure as in figure 1 with the same input features as specified in task-1. However, instead of computing the mean of node embeddings for neighborhood nodes, you will compute the sum. With these changes, compute the node embeddings for  $l = 1$  to  $l = 5$  such that  $W_1 = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & -1 \\ -1 & 0 & 1 \end{bmatrix}$ ,  $B_1 = \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 1 \\ 0 & -1 & 1 \end{bmatrix}$  and for  $l > 1$ ,  $W_{l+1} = W_l X W_l^T$  and  $B_{l+1} = B_l X B_l^T$ . Here  $X$  denotes matrix multiplication.