

ADS Programming Project

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Implementation Details:

- *The Min-Heap data structure* has been implemented to store the ride details i.e., (rideNumber, rideCost, tripDuration) *ordered by the rideCost and tripDuration* (in case two rides have the same rideCost - given that every rideCost-tripDuration combination will be unique).
- *The Red-Black tree data structure* has been implemented to store the ride details i.e., (rideNumber, rideCost, tripDuration) *ordered by the rideNumber*.
- The implementation can handle only *one ride at a time*, for a *maximum of 2000 active ride requests*.
- *Operations supported* by the implementation and their time complexities:
(n = number of active rides, S = number of ride triplets printed)

<i>Print(rideNumber)</i>	Searches the Red-Black Tree for the given ride and prints it if the ride is found. [$O(\log(n))$]
<i>Print(rideNumber1, rideNumber2)</i>	Searches the Red-Black Tree for rides in the given range and prints them if any ride is found. [$O(\log(n)+S)$ time]
<i>Insert(rideNumber,rideCost,tripDuration)</i>	Inserts a ride with the given ride triplet values in the min-heap and the Red-Black tree, each having pointers to the other. [$O(\log(n))$ time]
<i>GetNextRide()</i>	Returns the ride at the root of the min-heap if the heap is not empty and deletes it from the min-heap and the red-black tree. [$O(\log(n))$ time]
<i>CancelRide(rideNumber)</i>	Deletes the ride having given rideNumber from the min-heap and red-black tree. [$O(\log(n))$ time]
<i>UpdateTrip(rideNumber, new_tripDuration)</i>	1. $\text{new_tripDuration} \leq \text{existing_tripDuration}$ – Deletes the existing ride and inserts a new ride in the min-heap and red-black tree with updated cost, and links them

2. $\text{existing_tripDuration} < \text{new_tripDuration} \leq 2 * (\text{existing_tripDuration})$ - Deletes the existing ride and inserts a new ride in the min-heap and red-black tree with updated cost as $(\text{currentCost} + 10)$, and links them
3. $\text{new_tripDuration} > 2 * (\text{existing_tripDuration})$ - Deletes the existing ride from the min-heap and red-black tree with
 - Deletes and inserts are performed in $O(\log(n))$ time.

- Implementation is in Java

Project directory structure:

<i>gatorTaxi.java</i>	<i>Driver code for the implementation that calls the min-heap and red-black tree functions as per the input.</i>
<i>MinHeap.java</i>	<i>Builds a min-heap data structure and includes functions for search, insert, delete min, delete key, and minheapify on the min-heap.</i>
<i>HeapNode.java</i>	<i>Data Structure to store a min-heap node with ride details and a pointer to the TreeNode of the red-black tree.</i>
<i>RedBlackTree.java</i>	<i>Builds a red-black tree data structure and includes functions for search, insert, delete, and corresponding red-black tree rotations and transformations.</i>
<i>TreeNode.java</i>	<i>Data Structure to store a red-black tree node with ride details and a pointer to the HeapNode of the min-heap.</i>
<i>output_file.txt</i>	<i>Output file generated by the program.</i>
<i>Makefile</i>	

Time and Space Complexity:

Min-Heap Operation	Time Complexity	Space Complexity
Insert	$O(\log(n))$, where $\log(n)$ is the number of levels in the heap we will traverse at max in the worst case to insert a node	$O(1)$, no additional space required

Delete Min	$O(1)$, since we are deleting the root directly	$O(1)$, no additional space required
Delete key	$O(\log(n))$, where $\log(n)$ is the number of levels in the heap we will traverse at max in the worst case to delete a node	$O(1)$, no additional space required
MinHeapify	$O(\log(n))$, where $\log(n)$ is the number of levels in the heap we will traverse at max in the worst case to balance the heap	$O(1)$, no additional space required
Swap	$O(1)$ to swap the min-heap nodes	$O(1)$, no additional space required

Red-Black Tree Operation	Time Complexity	Space Complexity
Insert [insert, fixInsert functions]	$O(\log(n))$, where $\log(n)$ is the height of the balanced search tree	$O(1)$, no additional space required
Delete [delete using deleteHelper, deleteFixup functions]	$O(\log(n))$, where $\log(n)$ is the height of the balanced search tree	$O(1)$, no additional space required
Search [search using searchHelper function]	$O(\log(n))$, where $\log(n)$ is the height of the balanced search tree	$O(1)$, no additional space required
leftRotate	$O(1)$ to perform node rotations, there is no recursion	$O(1)$, no additional space required
rightRotate	$O(1)$ to perform node rotations, there is no recursion	$O(1)$, no additional space required
rbTransform	$O(1)$ to perform tree transform, there is no recursion	$O(1)$, no additional space required
getRoot	$O(1)$ to just return the root value	$O(1)$, no additional space required

Function prototypes and program structure:

1. gatorTaxi : Driver class

Functions:

'public static void main (String args [])' method:

- It takes the input file name as a command line argument, processes the input as per the 6 different operations listed above, and writes the output to the 'output_file.txt' file.
- For performing the operations, the main method calls the respective 'MinHeap' and 'RedBlackTree' class functions.

2. HeapNode: Class defining the Node Structure of the Min-Heap

Constructor:

public HeapNode(int rideNumber, int rideCost, int tripDuration)

- Initializes the heap node with the ride triplet details when a new ride instance is created for the min-heap.
- Stores a pointer to a TreeNode of the red-black tree to maintain a link from the min-heap to the red-black tree.

3. TreeNode: Class defining the Node Structure of the Red-Black Tree

Constructor:

public TreeNode(int rideNumber, int rideCost, int tripDuration, HeapNode node)

- Initializes the red-black tree node with the ride triplet details when a new ride instance is created for the red-black tree.
- Stores a pointer to a HeapNode of the min-heap to maintain a link from the red-black tree to the min-heap.

4. MinHeap: Class implementing the Min-Heap Data Structure

Constructor:

public MinHeap(int size)

- Initializes a 'HeapNode' array with a maximum size of 2000(as given in the project description)

Functions:

private int parent(int i)

- Returns the index of the parent node for the node at index i in the HeapNode array

private int leftChild(int i)

- Returns the index of the left child node for the node at index i in the HeapNode array

private int rightChild(int i)

- Returns the index of the right child node for the node at index i in the HeapNode array

private boolean isLeaf(int i)

- Returns true if the node at index i in the HeapNode array is a leaf node, i.e., its right and left child are null.

private HeapNode insert(HeapNode element)

- Inserts ride in the min-heap based on rideCost comparisons, with the minimum rideCost ride being at the root of the min-heap.
- In case of the same ride costs of two rides, the ride having a smaller trip duration is put at the top of the min-heap.
- Returns the inserted HeapNode to set the corresponding red-black tree pointer in it in the driver class 'gatorTaxi'

public HeapNode remove()

- Remove the min-heap's root and replaces it with the last element in the min-heap.
- Performs minheapify operation(described below) to ensure it is a min-heap after the removal and replacement.
- Returns the root of the min-heap to the driver class to print it out.

public HeapNode deleteKey(int i)

- Deletes a specific ride having a certain rideNumber from the min-heap.
- Uses the 'idx' property in the HeapNode to delete the specific ride.
- Calls the decreaseKey function(described below) and remove() to delete the bubbled-up ride from the min-heap.
- Returns the deleted node copy to the driver class to delete the corresponding red-black tree node.

private void minHeapify(int i)

- Compares and swaps non-leaf node at index i with the minimum ride cost left or right child node, if the ride cost of any of the children is lesser.
- In case the node has the same cost as its left/right child, then the trip duration of the two nodes is compared.
- If the trip duration of the child node is lesser than the node at index i then the two nodes are swapped

private void decreaseKey(int i, HeapNode new_val)

- Bubbles up the ride having the idx value i to the top of the min-heap by replacing the node with the 'new_val' that has 'Integer.MIN_VALUE' rideCost.

private void swap(int x, int y)

- Swaps the two heap nodes present at indices x and y of the HeapNode array

5. Red-Black Tree: Class implementing the Red-Black Tree Data Structure

Constructor:

public RedBlackTree()

- Initializes the RedBlackTree instance with a 'TreeNode' root with TNULL i.e., a TreeNode(0,0,0,null), color=black and null left and right children.

Functions:

private TreeNode searchHelper(TreeNode node, int rideNumber)

- Checks if the rideNumber matches the current root node, if not, it recursively traverses the left/right subtree depending on if the rideNumber is lesser or greater than the current node value.
- Returns the TreeNode found for the given rideNumber or returns null if no TreeNode is found to the calling search method

private void deleteFixup(TreeNode x)

- Balances the red-black tree after the deletion of a ride from the tree considering the various red-black tree constraints.

private void rbTransform(TreeNode node1, TreeNode node2)

- Transform the red-black tree to satisfy the balanced red-black tree constraints.

private void deleteHelper(TreeNode node, int rideNumber)

- Helper method to delete the ride for the given rideNumber from the red-black tree.

private void insertFixup(TreeNode k)

- Balances the red-black tree after the insertion of a ride into the tree taking into account the various red-black tree constraints.

public search(int rideNumber)

- Calls a searchHelper function to recursively search for the given rideNumber in the tree
- Returns the TreeNode found for the given rideNumber or returns null if no TreeNode is found to the driver class

public TreeNode minimum(TreeNode node)

- Returns the minimum node linked to the passed node i.e., the left node

public void findNodesInRange(TreeNode curr, int rideNumber1, int rideNumber2)

- Recursively searches for nodes in the given ride number range.
- Writes all the nodes that fall in thxe range to the output file.

public void leftRotate(TreeNode x)

- Performs a left rotation to balance the red-black tree after insertions and deletions.

public void rightRotate(TreeNode x)

- Performs a right rotation to balance the red-black tree after insertions and deletions.

public TreeNode insert(int rideNumber, int rideCost, int tripDuration, HeapNode heapNode)

- Inserts a new TreeNode into the red-black tree with the given ride triplet details and the pointer to the corresponding HeapNode in the min-heap.
- Returns the inserted TreeNode to the driver class to set it in the pointer of the corresponding HeapNode in the min-heap.

public TreeNode getRoot()

- Returns the root node in the red-black tree to the driver class.

public void deleteNode(int rideNumber)

- Calls the deleteHelper method to delete the node having the given rideNumber from the red-black tree.