

Coverage for **diffusion2d.py**: 59%

79 statements 47 run 32 missing 0 excluded

```

1  """
2  Solving the two-dimensional diffusion equation
3
4  Example acquired from https://scipython.com/book/chapter-7-matplotlib/examples/the-two-dimensional-diffusion-equation
5  """
6
7  import numpy as np
8  import matplotlib.pyplot as plt
9
10
11 class SolveDiffusion2D:
12     def __init__(self):
13         """
14         Constructor of class SolveDiffusion2D
15         """
16         # plate size, mm
17         self.w = None
18         self.h = None
19
20         # intervals in x-, y- directions, mm
21         self.dx = None
22         self.dy = None
23
24         # Number of discrete mesh points in X and Y directions
25         self.nx = None
26         self.ny = None
27
28         # Thermal diffusivity of steel, mm^2/s
29         self.D = None
30
31         # Initial cold temperature of square domain
32         self.T_cold = None
33
34         # Initial hot temperature of circular disc at the center
35         self.T_hot = None
36
37         # Timestep
38         self.dt = None
39
40     def initialize_domain(self, w=10., h=10., dx=0.1, dy=0.1):
41         assert isinstance(w, float)
42         assert isinstance(h, float)
43         assert isinstance(dx, float)
44         assert isinstance(dy, float)
45
46         self.w = w
47         self.h = h
48         self.dx = dx
49         self.dy = dy
50         #self.nx = int(w / dx)
51         self.nx = int(h / dx)
52         self.ny = int(h / dy)
53
54
55     def initialize_physical_parameters(self, d=4., T_cold=300., T_hot=700.):
56         self.D = d
57         self.T_cold = T_cold
58         self.T_hot = T_hot
59
60         #assert isinstance(d, float) and isinstance(T_cold, float)
61         #assert isinstance(T_hot, float)
62
63         # Computing a stable time step
64         dx2, dy2 = self.dx * self.dx, self.dy * self.dy
65         #self.dt = dx2 * dy2 / (2 * self.D * (dx2 + dy2))
66         self.dt = dx2 * dy2 / (2 * self.D * (dx2 + dy2)) * 100
67
68         print("dt = {}".format(self.dt))
69
70
71     def set_initial_condition(self):
72         u = self.T_cold * np.ones((self.nx, self.ny))
73
74         # Initial conditions - circle of radius r centred at (cx,cy) (mm)
75

```

```

76         r, cx, cy = 2, 5, 5
77         r2 = r ** 2
78         for i in range(self.nx):
79             for j in range(self.ny):
80                 p2 = (i * self.dx - cx) ** 2 + (j * self.dy - cy) ** 2
81                 if p2 < r2:
82                     #u[i, j] = self.T_hot
83                     u[i, j] = self.T_hot + 1
84
85         return u.copy()
86
87     def do_timestep(self, u_nml):
88         u = u_nml.copy()
89
90         dx2 = self.dx * self.dx
91         dy2 = self.dy * self.dy
92
93         # Propagate with forward-difference in time, central-difference in space
94         u[1:-1, 1:-1] = u_nml[1:-1, 1:-1] + self.D * self.dt * (
95             (u_nml[2:, 1:-1] - 2 * u_nml[1:-1, 1:-1] + u_nml[:-2, 1:-1]) / dx2
96             + (u_nml[1:-1, 2:] - 2 * u_nml[1:-1, 1:-1] + u_nml[1:-1, :-2]) / dy2)
97
98         return u.copy()
99
100    def create_figure(self, fig, u, n, fignum):
101        fignum += 1
102        ax = fig.add_subplot(220 + fignum)
103        im = ax.imshow(u.copy(), cmap=plt.get_cmap('hot'), vmin=self.T_cold, vmax=self.T_hot)
104        ax.set_axis_off()
105        ax.set_title('{:.1f} ms'.format(n * self.dt * 1000))
106
107        return fignum, im
108
109
110    def output_figure(fig, im):
111        fig.subplots_adjust(right=0.85)
112        cbar_ax = fig.add_axes([0.9, 0.15, 0.03, 0.7])
113        cbar_ax.set_xlabel('$T$ / K', labelpad=20)
114        fig.colorbar(im, cax=cbar_ax)
115        plt.show()
116
117
118    def main():
119        DiffusionSolver = SolveDiffusion2D()
120
121        DiffusionSolver.initialize_domain()
122
123        DiffusionSolver.initialize_physical_parameters()
124
125        u0 = DiffusionSolver.set_initial_condition()
126
127        # Number of timesteps
128        nsteps = 101
129
130        # Output 4 figures at these timesteps
131        n_output = [0, 10, 50, 100]
132
133        fig_counter = 0
134        fig = plt.figure()
135
136        im = None
137
138        # Time loop
139        for n in range(nsteps):
140            u = DiffusionSolver.do_timestep(u0)
141
142            # Create figure
143            if n in n_output:
144                fig_counter, im = DiffusionSolver.create_figure(fig, u, n, fig_counter)
145
146            u0 = u.copy()
147
148        # Plot output figures
149        output_figure(fig, im)
150
151
152    if __name__ == "__main__":
153        main()

```

