

Coverage for **diffusion2d.py**: 61%

82 statements

50 run

32 missing

0 excluded

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1  """
2  Solving the two-dimensional diffusion equation
3
4  Example acquired from https://scipython.com/book/chapter-7-matplotlib/examples/the-two-dimensional-diffusion-equation
5  """
6
7  import numpy as np
8  import matplotlib.pyplot as plt
9
10
11 class SolveDiffusion2D:
12     def __init__(self):
13         """
14         Constructor of class SolveDiffusion2D
15         """
16         # plate size, mm
17         self.w = None
18         self.h = None
19
20         # intervals in x-, y- directions, mm
21         self.dx = None
22         self.dy = None
23
24         # Number of discrete mesh points in X and Y directions
25         self.nx = None
26         self.ny = None
27
28         # Thermal diffusivity of steel, mm^2/s
29         self.D = None
30
31         # Initial cold temperature of square domain
32         self.T_cold = None
33
34         # Initial hot temperature of circular disc at the center
35         self.T_hot = None
36
37         # Timestep
38         self.dt = None
39
40     def initialize_domain(self, w=10., h=10., dx=0.1, dy=0.1):
41         assert type(w) == float, "variable w has to be of type float."
42         assert type(h) == float, "variable h has to be of type float."
43         assert type(dx) == float, "variable dx has to be of type float."
44         assert type(dy) == float, "variable dy has to be of type float."
45         self.w = w
46         self.h = h
47         self.dx = dx
48         self.dy = dy
49         self.nx = int(w / dx)
50         # self.nx = int(h / dx)
51         self.ny = int(h / dy)
52
53
54     def initialize_physical_parameters(self, d=4., T_cold=300., T_hot=700.):
55         assert type(d) == float
56         assert type(T_cold) == float
57         assert type(T_hot) == float
58         self.D = d
59         self.T_cold = T_cold
60         self.T_hot = T_hot
61
62         # Computing a stable time step
63         dx2, dy2 = self.dx * self.dx, self.dy * self.dy
64         self.dt = dx2 * dy2 / (2 * self.D * (dx2 + dy2))
65         # self.dt = dx2 * dy2 / (2 * self.D * (dx2 * dy2))
66
67         print("dt = {}".format(self.dt))
68
69     def get_initial_condition(self):
70         u = self.T_cold * np.ones((self.nx, self.ny))
71
72         # Initial conditions - circle of radius r centred at (cx,cy) (mm)
73         r, cx, cy = 2, 5, 5

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```

74         r2 = r ** 2
75         for i in range(self.nx):
76             for j in range(self.ny):
77                 p2 = (i * self.dx - cx) ** 2 + (j * self.dy - cy) ** 2
78                 # p2 = (i * self.dy - cx) ** 2 + (j * self.dx - cy) ** 2
79                 if p2 < r2:
80                     u[i, j] = self.T_hot
81
82         return u.copy()
83
84     def do_timestep(self, u_nml):
85         u = u_nml.copy()
86
87         dx2 = self.dx * self.dx
88         dy2 = self.dy * self.dy
89
90         # Propagate with forward-difference in time, central-difference in space
91         u[1:-1, 1:-1] = u_nml[1:-1, 1:-1] + self.D * self.dt * (
92             (u_nml[2:, 1:-1] - 2 * u_nml[1:-1, 1:-1] + u_nml[:-2, 1:-1]) / dx2
93             + (u_nml[1:-1, 2:] - 2 * u_nml[1:-1, 1:-1] + u_nml[1:-1, :-2]) / dy2)
94
95         return u.copy()
96
97     def create_figure(self, fig, u, n, fignum):
98         fignum += 1
99         ax = fig.add_subplot(220 + fignum)
100         im = ax.imshow(u.copy(), cmap=plt.get_cmap('hot'), vmin=self.T_cold, vmax=self.T_hot)
101         ax.set_axis_off()
102         ax.set_title('{:.1f} ms'.format(n * self.dt * 1000))
103
104         return fignum, im
105
106
107     def output_figure(fig, im):
108         fig.subplots_adjust(right=0.85)
109         cbar_ax = fig.add_axes([0.9, 0.15, 0.03, 0.7])
110         cbar_ax.set_xlabel('$T$ / K', labelpad=20)
111         fig.colorbar(im, cax=cbar_ax)
112         plt.show()
113
114
115     def main():
116         DiffusionSolver = SolveDiffusion2D()
117
118         DiffusionSolver.initialize_domain()
119
120         DiffusionSolver.initialize_physical_parameters()
121
122         u0 = DiffusionSolver.get_initial_condition()
123
124         # Number of timesteps
125         nsteps = 101
126
127         # Output 4 figures at these timesteps
128         n_output = [0, 10, 50, 100]
129
130         fig_counter = 0
131         fig = plt.figure()
132
133         im = None
134
135         # Time loop
136         for n in range(nsteps):
137             u = DiffusionSolver.do_timestep(u0)
138
139             # Create figure
140             if n in n_output:
141                 fig_counter, im = DiffusionSolver.create_figure(fig, u, n, fig_counter)
142
143             u0 = u.copy()
144
145         # Plot output figures
146         output_figure(fig, im)
147
148
149     if __name__ == "__main__":
150         main()

```

