

**CADMIUM CELL-DEVS MODEL OF CO<sub>2</sub> AS A PROXY FOR COVID  
INFECTION WITHIN A DYNAMIC SETTING**

**SUMMARY**

**Term Project  
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## 1.0 Introduction

COVID-19 has become an ever-present worry in people's daily lives. Many guidelines have been put in place to reduce the risk of transmission and protect the population. For example, people are required to sanitise their hands before entering public locations to reduce contact transmission; wearing a mask has been enforced as a law in public locations since masks block the transmission of most airborne contagion droplets produced by talking, coughing, sneezing. Furthermore, the two-meter distancing rule has been put in place to limit airborne transmission since COVID-19 is largely transmitted via large droplets which are too heavy to float, dropping to the ground within two meters unless coughing or sneezing, in which case the large droplets can reach distances of up to six meters [1]. However, despite the multiple countermeasures that have been set in place, there is still a significant threat of transmission via the lesser produced small droplets that are light enough to float in the air for 15 minutes up to three hours [2]. Although the quantity of small droplets exhaled is very small, over time they accumulate in badly vented locations and can pose a serious threat to any occupant's health. This threat is especially prevalent in indoor settings since simply circulating the air with a fan will not remove the contagion; it requires ventilation to replace the air [2].

By combining and modifying "CO<sub>2</sub> Model with Moving Occupants" with "Model of CO<sub>2</sub> as a Proxy for Infection", this paper seeks to simulate the risk of COVID-19 transmission via aerosolized contagion in a dynamic indoor setting by simulating and analysing the concentration of CO<sub>2</sub> throughout.

## 2.0 Background

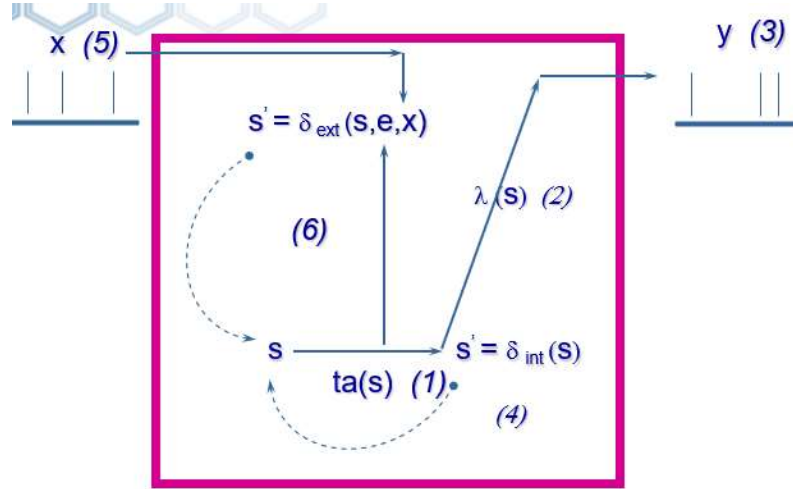
This project uses Cell-DEVS formalism to design and build the models. Cell-DEVS is a simulation using cellular automata, where each cell is a DEVS model that is connected to its neighbours.

DEVS offers a formalized modeling technique that functions in a modular, hierarchical manner. At its base, DEVS provides the framework for atomic models which can be as simple as a random number generator. This can then be coupled with other atomic models, creating coupled models. These coupled models can further be coupled, hence the modular hierarchical nature of the formalism. This leads to a very reusable and expandable modeling method since atomic models can be added, removed or modified individually. Furthermore, DEVS is easily validated since each aspect can be tested and validated individually or combined.

The atomic model is defined as an input, output, states, internal transition, external transition, output function and time advance (see Figure 1). Notably, an atomic model does not necessarily require any inputs. For example, it could be a variable generator for another atomic model. The state variable(s) are associated with the time advance function which determines the amount of time a model spends in a given state. When the time of the given state ends, the internal transition and output function are triggered. The internal transition function will change or remain in the state depending on its state variables. The output function will propagate the result of the model's current state on the output ports. Finally, when an input arrives at the input port(s)  $X$ , an external transition  $\delta_{\text{ext}}$  is triggered. It is the implementation of  $\delta_{\text{ext}}$  that determines what to do with the received information. The flow of a DEVS atomic model can be seen in Figure 2 below.

$$\text{DEVS atomic model} = \langle X, Y, S, \delta_{\text{ext}}, \delta_{\text{int}}, \lambda, \text{ta} \rangle$$

**Figure 1.** DEVS formal definition [3].  $X$  is the input port(s) and  $Y$  is the output port(s) of the model.  $S$  is the state variable(s) of the model which is associated with the time advance function  $\text{ta}$ .  $\delta_{\text{int}}$  and  $\lambda$  represent the internal transition and output function, respectively. The external transition is represented by  $\delta_{\text{ext}}$ .



**Figure 2.** DEVS atomic model transition flow

Cellular automata is a simulation technique comprised of a grid of cells that each have their own state and implementation. Each cell communicates with its assigned neighbours. When a cell's transport delay ( $dt$ ) is expended, it broadcasts its state information to its neighbours. The neighbours, upon receiving the input, will trigger their input computing function ( $\tau$ ). There is also an internal delay ( $di$ ) which is pre-emptive and meant to maintain the models timing despite interruptions such as receiving an input.

Cell-DEVS is the combination of cellular automata with DEVS formalism. Each cell is an atomic model that are coupled, creating a grid of atomic models which, together, comprise the Cell-DEVS model. For this paper, the Cadmium Cell-DEVS environment was used. Cadmium offers many different DEVS and Cell-DEVS features. Most importantly, it offers the use of multiple state variables within each cell atomic model. Cadmium is implemented in C++ and is built in a hierarchical manner of classes that each implement the functions of the model.

### 3.0 Base Model Background

Before discussing the model that was designed and implemented in this paper, understanding the base models upon which the model of interest was built is paramount. "CO<sub>2</sub> Model with Moving Occupants" and "Model of CO<sub>2</sub> as a Proxy for Infection", two models implemented in Cadmium Cell-DEVS, were combined and further expanded. They are both based on the original "Cell-Devs Models for CO<sub>2</sub> Sensors Locations in Closed Spaces" (CO<sub>2</sub>CS), implemented in CD++ [4], which modeled the dissipation of CO<sub>2</sub> in a closed environment to find the optimal location for CO<sub>2</sub> sensors to detect occupation. The two base models used for the expanded implementation, used the core principles of CO<sub>2</sub> dissipation rules and ventilation

established in CO<sub>2</sub>CS, implemented them in Cadmium Cell-DEVS and further added their own layers of complexity. This was possible due to the modular nature of Cell-DEVS. Both base models are part of the Simulation Everywhere – Cell DEVS CO<sub>2</sub> spread indoors GitHub [5].

### 3.1 CO<sub>2</sub> Model with Moving Occupants

As mentioned above, this model is based on the original CO<sub>2</sub>CS. However, this model adds an extra layer of complexity by adding a dynamic CO<sub>2</sub> generator. In the original CO<sub>2</sub>CS model, the CO<sub>2</sub> generator was static, spawning at its assigned location at the beginning of the simulation, and remaining there, producing CO<sub>2</sub>, until the simulation ended. However, in “CO<sub>2</sub> Model with Moving Occupants”, the CO<sub>2</sub> generators spawn at a predetermined location like a door, and travel around the setting.

“CO<sub>2</sub> Model with Moving Occupants” has 3 state variables: concentration, type, and count. The type state variable is associated with transport delay, defined as: 5 seconds if type is a CO<sub>2</sub> producer, and one otherwise; and concentration. A Vonnumen neighbourhood is used, meaning that the neighbourhood is comprised of itself and the 4 surrounding cells (ie. North, South, East, and West). Furthermore, the model has 3 lists: actionList, studentList, workstationList. These lists save the next cell to be traveled to, all of the CO<sub>2</sub> generator information and locations, and the CO<sub>2</sub> generator assigned workstation and its location, respectively. The behaviour of each individual cell depends on their state variables. Below in table one is pseudo code describing a cell's behaviour when it receives an input depending on its “type”.

**Table 1:** CO<sub>2</sub> Model with Moving Occupants  $\tau$  pseudocode

T(N) concentration	N = type
Concentration = average neighbourhood CO <sub>2</sub> concentration	Air: -100
If any action list position = this cell position $\rightarrow$ type = CO <sub>2</sub> source	
If spawn point and maximum students isn't reached $\rightarrow$ spawn a new student at the entrance every two seconds	
Concentration = average neighbourhood concentration + 12.16ppm	CO <sub>2</sub> _source: -200
Determine next action If do nothing $\rightarrow$ do nothing If move $\rightarrow$ type = Air and add action to action list	
Concentration = 0	
Concentration = 500	Door: -400
Concentration = 400	Window: -500
Concentration = 300	Vent: -600
Concentration = average neighbourhood CO <sub>2</sub> concentration	Workstation: -700

This model was tested in a setting representing a computer lab that contained ventilation along the walls, multiple rows of desks, and a big door. The simulation had multiple students (i.e. CO<sub>2</sub> sources) spawn at the door, travel to their assigned

workstation, wait a random amount of time, and then exit by the entrance. As the students traveled to their assigned workstations, a trail of CO<sub>2</sub> lingered behind. This trail was the minimal concentration. However, with many students entering the setting, the CO<sub>2</sub> concentration quickly climbed to very high levels.

The dynamic feature of the CO<sub>2</sub> sources means that the CO<sub>2</sub> spread through the room much faster than it would have if the CO<sub>2</sub> generators were static. Furthermore, since CO<sub>2</sub> is slow to dissipate, it quickly increased in concentration, reaching alarmingly high levels.

### 3.2 Model of CO<sub>2</sub> as a Proxy for Infection

“Model of CO<sub>2</sub> as a Proxy for Infection” is also built upon the CO<sub>2</sub>CS model. However, it retains little of the original model. Although maintaining static CO<sub>2</sub> sources, it adds an extra layer of complexity to the dissipation of CO<sub>2</sub> and further introduces a new “type” state variable: susceptible CO<sub>2</sub> source. These changes serve to simulate the CO<sub>2</sub> sources that become at risk should CO<sub>2</sub> carry the COVID-19 contagion inside a room with an air current.

**Table 2:** Model of CO<sub>2</sub> as a Proxy for Infection  $\tau$  pseudocode

T(N) concentration	N = type
<p>If X_wind == neighbor relative position[X] and Y_wind == neighbor relative position[Y] → flow concentration = (neighbors' concentration*wind)</p> <p>Else → concentration += neighbors' concentration</p> <p>If flow concentration != 0 → Concentration = (1-wind)*concentration/(num_neighbors-1) + flow concentration</p> <p>Else → Concentration = average neighbourhood concentration</p> <p>If flow concentration != 0 → concentration = (1 -1 flow weight)*average concentration of all but upwind neighbour + flow concentration</p> <p>Else → concentration = average neighbourhood concentration</p>	Air: -100
<p>If X_wind == neighbor relative position[X] and Y_wind == neighbor relative position[Y] → flow concentration = (neighbors' concentration*wind)</p> <p>Else → concentration += neighbors' concentration</p>	CO <sub>2</sub> source: -200

<p>If flow concentration <math>\neq 0 \rightarrow \text{Concentration} = (1 - \text{wind}) * \text{concentration} / (\text{num\_neighbors} - 1) + \text{flow concentration} + 12.16\text{ppm}</math></p> <p>Else <math>\rightarrow \text{Concentration} = \text{average neighbourhood concentration} + 12.16\text{ppm}</math></p> <p>If in threshold quantity of CO<sub>2</sub> <math>\rightarrow \text{count}++</math>  If exposure time = risky time <math>\rightarrow \text{type} = \text{susceptible CO}_2 \text{ source}</math> and add next action to susceptible action list</p> <p>If count = time active <math>\rightarrow \text{type} = \text{workstation}</math></p>	
Concentration = 0	Wall: -300
Concentration = 500	Door: -400
Concentration = 400	Window: -500
Concentration = 300	Vent: -600
<p>If X_wind == neighbor relative position[X] and Y_wind == neighbor relative position[Y] <math>\rightarrow \text{flow concentration} = (\text{neighbors' concentration} * \text{wind})</math></p> <p>Else <math>\rightarrow \text{concentration} += \text{neighbors' concentration}</math></p> <p>If flow concentration <math>\neq 0 \rightarrow \text{Concentration} = (1 - \text{wind}) * \text{concentration} / (\text{num\_neighbors} - 1) + \text{flow concentration}</math></p> <p>Else <math>\rightarrow \text{Concentration} = \text{average neighbourhood concentration}</math></p> <p>If start time <math>\rightarrow \text{type} = \text{CO}_2 \text{ source}</math></p>	Workstation: -700
<p>If X_wind == neighbor relative position[X] and Y_wind == neighbor relative position[Y] <math>\rightarrow \text{flow concentration} = (\text{neighbors' concentration} * \text{wind})</math></p> <p>Else <math>\rightarrow \text{concentration} += \text{neighbors' concentration}</math></p> <p>If flow concentration <math>\neq 0 \rightarrow \text{Concentration} = (1 - \text{wind}) * \text{concentration} / (\text{num\_neighbors} - 1) + \text{flow concentration}</math></p> <p>Else <math>\rightarrow \text{Concentration} = \text{average neighbourhood concentration}</math></p> <p>If concentration &lt; risky concentration <math>\rightarrow \text{type} = \text{CO}_2 \text{ source}</math> and exposure time = 0</p>	Susceptible CO <sub>2</sub> source: -800

If count = time active → type = workstation	
---------------------------------------------	--

The first major change to the model is the addition of an air current. The air current is implemented by adding two new configuration values, X and Y, which denote the direction of the air current. For example, if the air current values are  $X = 1$  and  $Y = 0$ , then there is a very strong wind in the north direction only. This is translated in CO<sub>2</sub> dissipation by increasing the average concentration in the same direction as the wind.

A subsequent addition to the model which can be seen in table two is the new “type” state variable: susceptible CO<sub>2</sub> source, which has a type value of -800. A regular CO<sub>2</sub> source can become susceptible if they remain in a threshold concentration of CO<sub>2</sub> for a predetermined amount of time. Once susceptible, the susceptible CO<sub>2</sub> source then stops producing CO<sub>2</sub>. However, they can return to being a regular CO<sub>2</sub> source if the CO<sub>2</sub> concentration drops below the susceptible threshold. After a time active, both regular and susceptible CO<sub>2</sub> sources will de-spawn at which point, the simulation ends.

This model was tested using the same computer lab setting as “CO<sub>2</sub> Model with Moving Occupants” used. It further configured an air current value of  $X = 1$  and  $Y = 0$ . The simulation demonstrated that the CO<sub>2</sub> sources downwind became susceptible the fastest since the CO<sub>2</sub> from all other sources accumulated downwind. Eventually, all CO<sub>2</sub> sources became susceptible. However, all the CO<sub>2</sub> sources upwind became susceptible from their own CO<sub>2</sub> dissipation.

#### 4.0 Model Description

The model designed in this paper was built by combining and modifying the two models described above. This process was completed in three steps, such that the models could each be tested and validated before the addition of a new feature. The first step was combining both models in their simplest forms to create a dynamic susceptible model. This model used the susceptible type presented by “Model of CO<sub>2</sub> as a Proxy for Infection” along with the dynamic CO<sub>2</sub> sources implemented in “CO<sub>2</sub> Model with Moving Occupants”. After successfully validating the dynamic susceptible model, a dynamic infected model was implemented. This model further introduced a new “type” state variable: infected CO<sub>2</sub> source, seeking to simulate the risk of becoming susceptible in a setting with a confirmed COVID-19 infected person. Finally, a dynamic infected complex model was produced. This model reintroduced the air current from the “CO<sub>2</sub> as a Proxy for Infection” model along with a susceptible risk based on distance of the source. This is the final form of the model presented in this paper; it seeks to simulate the risk of becoming susceptible if a COVID-19 infected person is introduced to the closed setting in a more realistic way than its predecessor models.

##### 4.1 Dynamic Susceptible Model

The dynamic susceptible model is the first iteration. It was built by combining both base models in their simplest forms, using the dynamic implementation of the CO<sub>2</sub> sources along with the extra “type” state variable: susceptible CO<sub>2</sub> source. However, in this model, when a CO<sub>2</sub> source becomes susceptible, they continue producing CO<sub>2</sub> and can never return to the regular CO<sub>2</sub> source type.



**Table 3: Dynamic Susceptible Model  $\tau$  pseudocode**

T(N) concentration	N = type
Concentration = average neighbourhood CO <sub>2</sub> concentration	Air: -100
If any action list position = this cell position → type = CO <sub>2</sub> source	
If any susceptible action list position = this cell position → type = susceptible CO <sub>2</sub> source	
If spawn point and maximum students isn't reached → spawn a new student at the entrance every two seconds	
Concentration = average neighbourhood concentration + 12.16ppm	CO <sub>2</sub> source: -200
Determine next action If do nothing → do nothing If move → type = Air and add action to action list	
If in threshold quantity of CO <sub>2</sub> → count++ If count = risky time → type = susceptible CO <sub>2</sub> source and add next action to susceptible action list	
Concentration = 0	Wall: -300
Concentration = 500	Door: -400
Concentration = 400	Window: -500
Concentration = 300	Vent: -600
Concentration = average neighbourhood CO <sub>2</sub> concentration	Workstation: -700
Concentration = average neighbourhood CO <sub>2</sub> concentration + 12.16ppm	Susceptible CO <sub>2</sub> source: -800
Determine next action If do nothing → do nothing If move → type = Air and add action to susceptible action list	

As it can be in table three that the air current seen in the “CO<sub>2</sub> as a Proxy for Infection” model is not implemented in this iteration. This is because it was an extra layer of complexity that would have complicated the validation of the combined base model. Another interesting change that can be observed in the pseudo code above is the addition of a susceptible action list. This allows air cells to know whether to become a CO<sub>2</sub> source or a susceptible CO<sub>2</sub> source since the asynchronous nature of Cell-DEVSE means that the CO<sub>2</sub> source may have de-spawned before the air cell could check the surrounding types.

As mentioned above, the dynamic susceptible model is the combination of both base models in their simplest forms. Pulling aspects from both models, the dynamic susceptible model models the worst-case scenario of COVID-19 infection by assuming

that every CO<sub>2</sub> generator may transmit COVID-19 through their CO<sub>2</sub> emissions. However, as seen in “CO<sub>2</sub> as a Proxy for Infection”, it is possible for a regular CO<sub>2</sub> source remaining at their workstation for an extended period to make themselves into a susceptible CO<sub>2</sub> source. This is a shortcoming of the current model. That being said, it still serves as a good baseline model of the worst-case scenario in an enclosed space.

#### 4.2 Dynamic Infected Model

The dynamic infected model is the second iteration, built off of the model described in Section 4.1. In this iteration, a new type state variable along with modified CO<sub>2</sub> dissipation rules were added. The infected CO<sub>2</sub> source is a third CO<sub>2</sub> source type added to the model, representing a confirmed COVID-19 infected person. The purpose of this model is to simulate the risk of becoming infected should a confirmed COVID-19 infected person be introduced in a closed space. This provides a more realistic risk analysis compared to the worst-case analysis of the dynamic susceptible model.

**Table 4: Dynamic Infected Model  $\tau$  pseudocode**

T(N) concentration	N = type
Concentration = average neighbourhood CO <sub>2</sub> concentration  If any action list position = this cell position → type = CO <sub>2</sub> source  If any susceptible action list position = this cell position → type = susceptible CO <sub>2</sub> source  If any susceptible action list position = this cell position → type = infected CO <sub>2</sub> source If spawn point and maximum students isn't reached → If infected maximum isn't reached → spawn a new infected student at the entrance every two seconds Else → spawn a new student at the entrance every two seconds	Air: -100
Concentration = average neighbourhood CO <sub>2</sub> concentration  Determine next action If do nothing → do nothing If move → type = Air and add action to action list  If in threshold quantity of CO <sub>2</sub> → count++ If count = risky time → type = susceptible CO <sub>2</sub> source and add next action to susceptible action list	CO <sub>2</sub> source: -200
Concentration = 0	Wall: -300
Concentration = 500	Door: -400
Concentration = 400	Window: -500
Concentration = 300	Vent: -600
Concentration = average neighbourhood CO <sub>2</sub> concentration	Workstation: -700

Concentration = average neighbourhood CO <sub>2</sub> concentration  Determine next action If do nothing → do nothing If move → type = Air and add action to susceptible action list	Susceptible CO <sub>2</sub> source: -800
Concentration = average neighbourhood CO <sub>2</sub> concentration + 12.16ppm  Determine next action If do nothing → do nothing If move → type = Air and add action to infected action list	Infected CO <sub>2</sub> source: -900

Apart from the addition of a new state variable type, the dissipation of CO<sub>2</sub> rules was also changed. This is reflected in table 4, where the infected CO<sub>2</sub> source produces CO<sub>2</sub>. All other CO<sub>2</sub> sources simply calculate their concentration like the air type cell does. This allows for the exclusive modelling of CO<sub>2</sub> that can carry COVID-19 as an airborne contagion following the same rules of infection as in the previous iteration. Furthermore, a third action list for the infected CO<sub>2</sub> source was added to allow the air cells to know which type of CO<sub>2</sub> source it should become.

The changes between this iteration and the previous one are minimal. However, the quantity of new information is large. The dynamic susceptible model modeled a worst-case scenario where every source could infect another or even themselves. The dynamic infected model simulates the specific risk of being infected by airborne COVID-19 contagion in a closed space. The dynamic infected model can be used to analyze ventilation and workstation placement to find the optimal solution for minimal infection. However, the model still lacks the complexity of the real world, despite providing a useful simple setting analysis.

### 4.3 Dynamic Infected Complex Model

The dynamic infected complex model is the final iteration of the model presented in this paper. It is built upon the dynamic infected model, adding two new features to create more realistic model. The previous model only simulated the infection of COVID-19 through small droplet airborne contagion. Small droplets have a lower viral load, meaning a person requires longer exposure to be bombarded with enough contagion. However, at a two-meter proximity to the source, large droplets are possibly present, containing a higher viral load. This means that a person can be exposed for a shorter amount of time before becoming at risk.

In the new iteration, the two-meter rule is implemented. If a regular CO<sub>2</sub> source is within two meters of the infected CO<sub>2</sub> source, the time to become susceptible is reduced significantly. However, since the CO<sub>2</sub> sources are dynamic, a trail of the higher infection cells are left in the infected CO<sub>2</sub> sources wake for thirty seconds, simulating the time frame in which large droplets can remain airborne. The second new feature is the re-addition of airflow within the model. Even in closed spaces, there is often an air current. This is a step towards producing a more realistic and usable model.

**Table 5:** Dynamic Infected Complex Model  $\tau$  pseudocode

T(N) concentration	N = type
<p>If X_wind == neighbor relative position[X] and Y_wind == neighbor relative position[Y] <math>\rightarrow</math> flow concentration = (neighbors' concentration*wind)</p> <p>Else <math>\rightarrow</math> concentration += neighbors' concentration</p> <p>If flow concentration != 0 <math>\rightarrow</math> Concentration = (1-wind)*concentration/(num_neighbors-1) + flow concentration</p> <p>Else <math>\rightarrow</math> Concentration = average neighbourhood CO<sub>2</sub> concentration</p> <p>If any action list position = this cell position <math>\rightarrow</math> type = CO<sub>2</sub> source</p> <p>If any susceptible action list position = this cell position <math>\rightarrow</math> type = susceptible CO<sub>2</sub> source</p> <p>If any susceptible action list position = this cell position <math>\rightarrow</math> type = infected CO<sub>2</sub> source</p> <p>If spawn point and maximum students isn't reached <math>\rightarrow</math>            If infected maximum isn't reached <math>\rightarrow</math> maybe spawn a new infected student at the entrance every two seconds            Else <math>\rightarrow</math> spawn a new student at the entrance every two seconds</p> <p>If neighbours' risky distance larger than risky distance <math>\rightarrow</math> risky distance = neighbours' risky distance - 1</p> <p>If risky distance counter == 30 and risky distance larger than 0 <math>\rightarrow</math> risky distance - 1 and counter = 0            Else if risky distance larger than 0 <math>\rightarrow</math> counter +1</p>	<p>Air: -100</p>
<p>If X_wind == neighbor relative position[X] and Y_wind == neighbor relative position[Y] <math>\rightarrow</math> flow concentration = (neighbors' concentration*wind)</p> <p>Else <math>\rightarrow</math> concentration += neighbors' concentration</p> <p>If flow concentration != 0 <math>\rightarrow</math> Concentration = (1-wind)*concentration/(num_neighbors-1) + flow concentration</p>	<p>CO<sub>2</sub> source: -200</p>

<p>Else → Concentration = average neighbourhood CO<sub>2</sub> concentration</p> <p>Determine next action</p> <p>    If do nothing → do nothing</p> <p>    If move → type = Air and add action to action list</p> <p>If in threshold quantity of CO<sub>2</sub> →</p> <p>    If risky distance between 3 and 4 → count += 4</p> <p>    Else if between 1 and 2 → count += 2</p> <p>    Else → count += 1</p> <p>    If count = risky time → type = susceptible CO<sub>2</sub> source and add next action to susceptible action list</p> <p>If neighbours' risky distance larger than risky distance → risky distance = neighbours' risky distance - 1</p> <p>If risky distance counter == 30 and risky distance larger than 0 → risky distance – 1 and counter = 0</p> <p>Else if risky distance larger than 0 → counter +1</p>	
Concentration = 0	Wall: -300
Concentration = 500	Door: -400
Concentration = 400	Window: -500
Concentration = 300	Vent: -600
<p>If X_wind == neighbor relative position[X] and Y_wind == neighbor relative position[Y] → flow concentration = (neighbors' concentration*wind)</p> <p>Else → concentration += neighbors' concentration</p> <p>If flow concentration != 0 → Concentration = (1-wind)*concentration/(num_neighbors-1) + flow concentration</p> <p>Else → Concentration = average neighbourhood concentration</p> <p>If neighbours' risky distance larger than risky distance → risky distance = neighbours' risky distance - 1</p> <p>If risky distance counter == 30 and risky distance larger than 0 → risky distance – 1 and counter = 0</p> <p>Else if risky distance larger than 0 → counter +1</p>	Workstation: -700
<p>If X_wind == neighbor relative position[X] and Y_wind == neighbor relative position[Y] → flow concentration = (neighbors' concentration*wind)</p>	Susceptible CO <sub>2</sub> source: -800

<p>Else → concentration += neighbors' concentration</p> <p>If flow concentration != 0 → Concentration = (1-wind)*concentration/(num_neighbors-1) + flow concentration</p> <p>Else → concentration = average neighbourhood CO<sub>2</sub> concentration</p> <p>Determine next action            If do nothing → do nothing            If move → type = Air and add action to susceptible action list</p> <p>If neighbours' risky distance larger than risky distance            → risky distance = neighbours' risky distance - 1</p> <p>If risky distance counter == 30 and risky distance larger than 0 → risky distance – 1 and counter = 0            Else if risky distance larger than 0 → counter +1</p>	
<p>If X_wind == neighbor relative position[X] and Y_wind == neighbor relative position[Y] → flow concentration = (neighbors' concentration*wind)</p> <p>Else → concentration += neighbors' concentration</p> <p>If flow concentration != 0 → Concentration = (1-wind)*concentration/(num_neighbors-1) + flow concentration + 12.16ppm</p> <p>Else → Concentration = average neighbourhood concentration + 12.16ppm</p> <p>Determine next action            If do nothing → do nothing            If move → type = Air and add action to susceptible action list</p> <p>If neighbours' risky distance larger than risky distance            → risky distance = neighbours' risky distance - 1</p> <p>If risky distance counter == 30 and risky distance larger than 0 -&gt; risky distance – 1 and counter = 0            Else if risky distance larger than 0 -&gt; counter +1</p>	<p>Infected CO<sub>2</sub> source: -900</p>

The two new features, namely the two-meter rule (risky distance) and the air current, have been added to the cell types: Air, Workstation, CO<sub>2</sub> source, Susceptible CO<sub>2</sub> source and Infected CO<sub>2</sub> source. The wind strength is determined in the configuration json file as a percentage. Although unconventional, it is a simple way of determining the weight each cell will carry and contribute to the average concentration. Since the model uses a Vonnumen neighbourhood, the air current can only come from the North, South, East and West exclusively – to model a crosswind, the model would require a Moors neighbourhood. The neighbouring upwind cell of a cell calculating its CO<sub>2</sub> concentration will be multiplied by the wind modifier, while the all the other neighbouring cells are multiplied by one minus the wind modifier, meaning the upwind cell experiences a larger effect from the cell down wind from its position.

The two-meter rule is the second feature added. If a neighbouring cell has a risk level above zero, the current cell's risk level will be the neighbours risk level minus one since its one farther from the source. After thirty seconds, the risk level is reduced by one until it returns to zero. The maximum risk level is four since the two meters are represented by 4 cells. The Cell an infected CO<sub>2</sub> source passes through becomes a level 4 risk. All bordering cells become a level 3, and so on until the threat level reaches 0. If a CO<sub>2</sub> source is within one meter of an infected source or its path within 30 seconds of their passing, risk level 3 or 4 cell, the CO<sub>2</sub> source will become susceptible four times faster. Within a two-meter distance, meaning a risk level between one and two, the time to infection is doubled comparatively to the common time and half as long as the highest risk level. This serves to simulate the increase in risk proportional to the distance of the infected CO<sub>2</sub> source.

The air current and the two-meter rule are two features that serve to complicate the model's model of infection, allowing it to serve as a more realistic model of infection than the dynamic infection model. However, it is still far from the real system. The iterative method of development allows to test each feature individually and ensure that it will serve as a sturdy base model for future work.

## 5.0 Experimental Framework and Results

Three subsequent interactions were produced and tested, each before producing the next. This allowed for the testing and validation of each new feature to ensure a strong base for the next iteration to build upon. In this section the tests and results of each model simulation will be discussed in chronological order.

To allow cross analysis, each model was simulated over the same period of 1,000 time units. Each setting was tested using the same settings and configurations when possible. Furthermore, Figure 3 shows the colour legend of the CO<sub>2</sub> concentrations used in every simulation. By ensuring that the models are tested in the most similar fashion possible, previous iterations can be used to validate the behaviour of the next one.

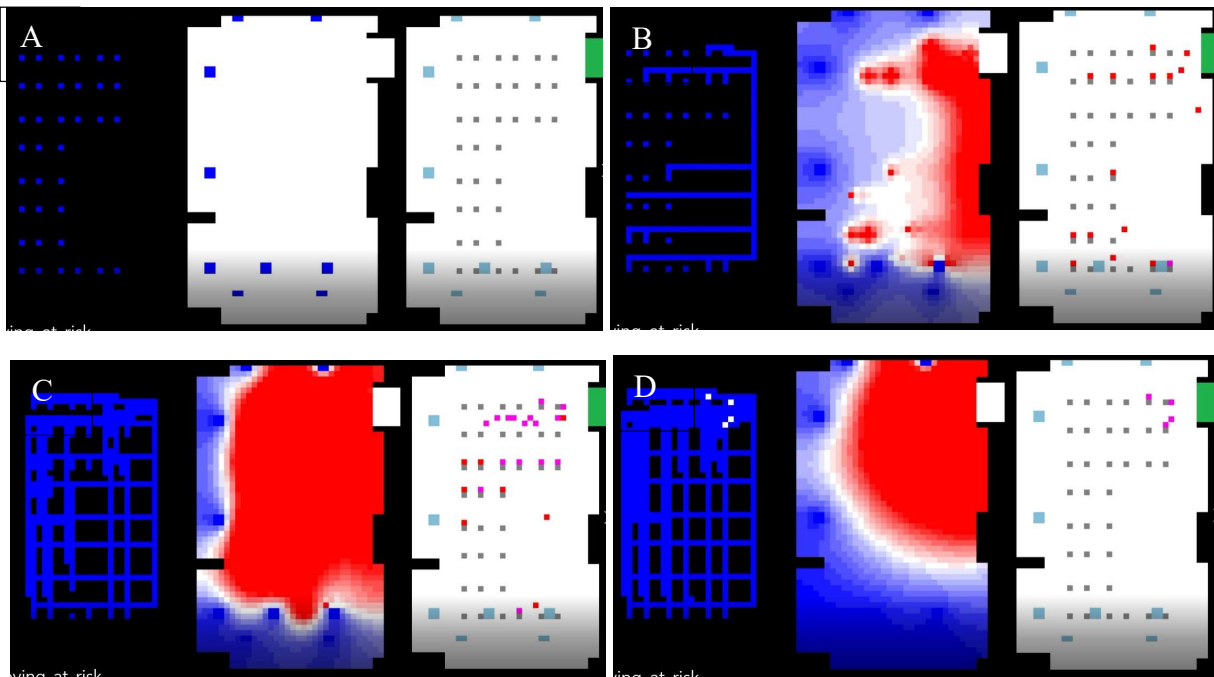


**Figure 3.** Color legend of CO<sub>2</sub> concentration in ppm [4]

### 5.1 Dynamic Susceptible Model Simulation

The dynamic susceptible model is the culmination of combining “Model of CO<sub>2</sub> as a Proxy for Infection” and “CO<sub>2</sub> Model with Moving Occupants” in their simplest forms. The purpose was to both create a solid base for the next iteration, but also model the worst-case possibility of becoming infected with COVID-19 from airborne contagion, assuming everyone could transmit it.

Figure 4 illustrated the visualization of the simulation using the computer lab scenario presented in the base models. The computer lab has a large door on the East side, ventilation along the North, West, and South walls, and a series of workstations in the center of the room. CO<sub>2</sub> sources spawn at the door and travel to their randomly assigned workstations, remain for a random amount of time, and then return to the door and de-spawn. A regular CO<sub>2</sub> source is red and becomes purple if it becomes a susceptible CO<sub>2</sub> source type.



**Figure 4. Dynamic susceptible model computer lab simulation.** The simulation has 3 visualization windows. The window on the left demonstrates the path taken by CO<sub>2</sub> sources. The window in the middle is the levels of CO<sub>2</sub> in ppm, and the window on the right is the position of the CO<sub>2</sub> sources.

Looking at the visualization it can be determined that the dynamic nature of the CO<sub>2</sub> sources spreads CO<sub>2</sub> quickly along the path of travel as the concentration of CO<sub>2</sub> reaches very high levels. One of the CO<sub>2</sub> sources in the bottom right corner has become susceptible in image B. In image C, all CO<sub>2</sub> sources have spawned, and many are headed back to the exit. From this, it is clear that the ventilation in the computer lab, although numerous, has little effect on the levels of concentration of the CO<sub>2</sub>. Despite the lack of presence in the bottom left corner of the workstations, the CO<sub>2</sub> levels remain high. At the end of the simulation, most CO<sub>2</sub> sources have exited the lab, and the ventilation is finally starting to dissipate the CO<sub>2</sub> concentration. Although not demonstrated in the



visualization, every CO<sub>2</sub> source in the simulation became susceptible before leaving their workstations.

The first purpose of this simulation visualization is to validate the model. Looking at the visualization, the CO<sub>2</sub> sources reliably spawn at the door until the maximum number of sources is reached. Each CO<sub>2</sub> source travels to their designated workstation and becomes susceptible when exposed to high concentrations. The second point of interest for validation are the susceptible CO<sub>2</sub> source rules. When a regular CO<sub>2</sub> source is exposed to the risky concentration (600 ppm in this simulation) for the risky duration (40 seconds in this simulation), they become susceptible. Once susceptible, they maintain the behaviour of a regular CO<sub>2</sub> source and return to the exit. The behaviour demonstrated in the visualization above is as expected and validates it based on the expected outcome.

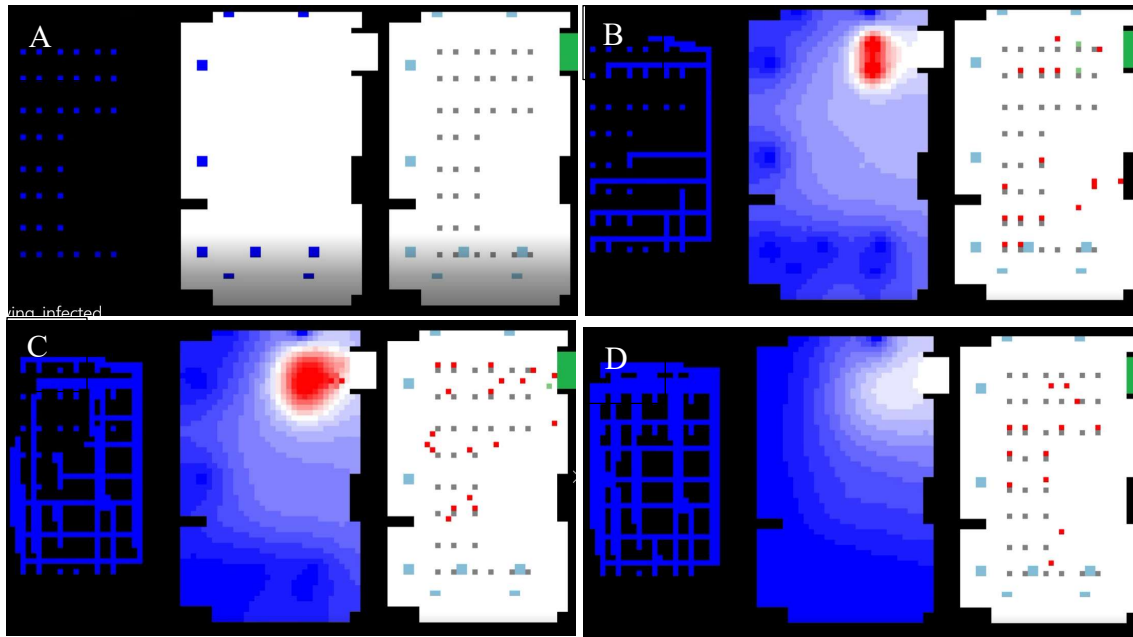
The second purpose of the simulation is to conduct a risk analysis of the worst-case scenario. Considering that every CO<sub>2</sub> source in the simulation became susceptible, the risk of becoming susceptible is 100% with this model. This brings to light two important problems. The first is the ventilation in the setting. Since the ventilation is only on three of the four walls, it allows CO<sub>2</sub> to accumulate in concerning high concentration on the side without ventilation. Ventilation should be placed in the center of the room to further improve its efficiency by dissipating the CO<sub>2</sub> on all four sides of the unit rather than only the side facing the CO<sub>2</sub>. The second important problem of the model is the fact that CO<sub>2</sub> sources can infect themselves. Every CO<sub>2</sub> source only became susceptible when at their workstation. This means they likely submitted themselves to a high concentration and the surrounding CO<sub>2</sub> sources only expedited the process (i.e. they did not definitively cause the transition to being susceptible).

The simulation of the dynamic susceptible model demonstrated that the model was successfully combined and produces an acceptable worst-case scenario for airborne infection.

## **5.2 Dynamic Infected Model Simulation**

The dynamic infected model is the second iteration, built upon the dynamic susceptible model after it was validated. The dynamic infected model seeks to model the risk of being infected by COVID-19 if an infected person is introduced to a closed setting. It models the aerosolized contagion, specifically the small droplets contagion traveling with the CO<sub>2</sub> emissions.

Once again, this model was simulated in the computer lab setting. The same amount of CO<sub>2</sub> sources spawned, however two of them were infected CO<sub>2</sub> sources. As described in the model description, only the infected CO<sub>2</sub> source produce CO<sub>2</sub> in the simulation. The other CO<sub>2</sub> sources simply act as air cells, tracking the concentrations they are exposed to and becoming susceptible cells if exposed to too much for too long.

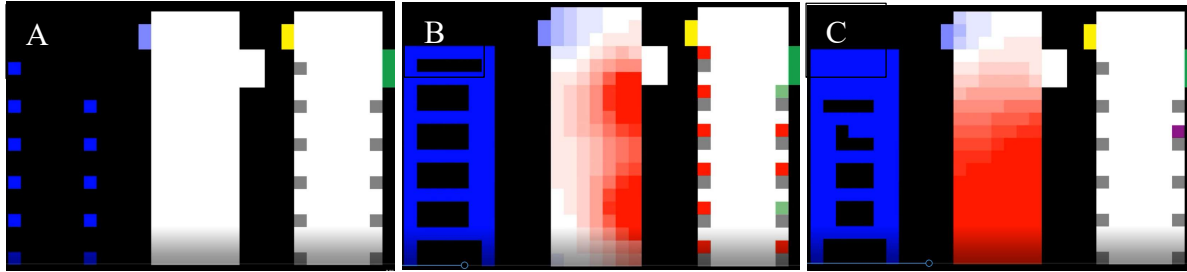


**Figure 5. Dynamic infected model computer lab simulation.** Infected CO<sub>2</sub> sources are denoted by a light green. When an air cell becomes susceptible, it is denoted in purple.

As in the previous iteration, all CO<sub>2</sub> sources regardless of being regular, susceptible, or infected, have the same behaviour. They spawn at the door, travel to a workstation, return to the door, and de-spawn. Maintaining the configurations across the iteration tests is important for both validation and cross analysis. It can be seen in image B that both infected CO<sub>2</sub> sources have spawned and reached their randomly assigned desks. It is noticeable that the ventilation is keeping the concentration of CO<sub>2</sub> very isolated to the individual in question. In image C, both infected CO<sub>2</sub> sources leave their workstation and are headed for the door. The CO<sub>2</sub> has expanded, but the workstations are spread too far apart for any regular CO<sub>2</sub> source to be exposed to high concentration.

During the simulation, no CO<sub>2</sub> source became susceptible. This is likely because the workstations were too far apart, and the ventilation within the room was adequate to keep emissions from both infected CO<sub>2</sub> sources under control. For this reason, a new setting was introduced to further test the model.

The new setting is a representation of a bus (see Figure 6). The only sources of ventilation present in the bus are a window and the door at the front. CO<sub>2</sub> sources spawn at the door until every seat is filled. They travel to their seat, sit for a random amount of time the return to the door and de-spawn. This simulation is meant to represent a tighter closed environment where distancing is limited. Again, two infected CO<sub>2</sub> sources are introduced to the system.



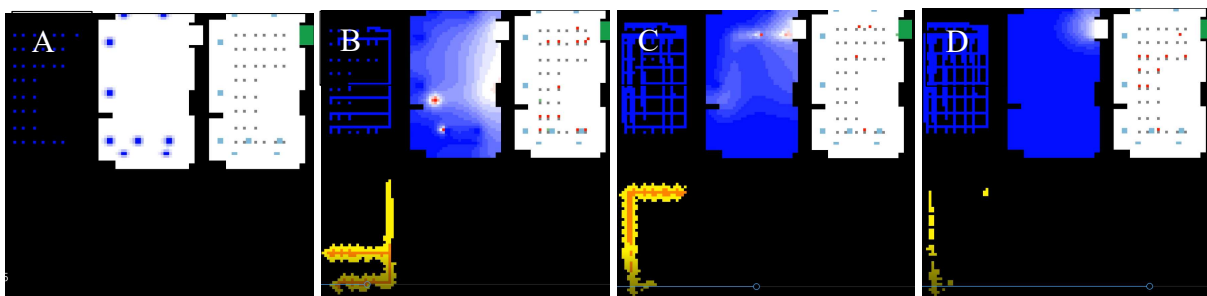
**Figure 6. Dynamic infected model bus simulation.** Two sources of ventilation are present on the bus, namely a window (yellow) and a door (green). The infected CO<sub>2</sub> sources are depicted in green and the regular CO<sub>2</sub> sources are depicted in red. Once a regular CO<sub>2</sub> source becomes susceptible, it is shown in purple.

The lack of ventilation is noticeable since the CO<sub>2</sub> concentration quickly rises. Both infected sources are sitting on the same side of the bus, however by image C, the entire occupied space is enveloped in their emissions. By the end of the simulation, five regular CO<sub>2</sub> sources – all CO<sub>2</sub> sources in the infected column along with two others in the same row as the infected sources – became susceptible. This demonstrates that proximity plays a large role in COVID-19 transmission since almost all sources in the opposing column remained unsusceptible. The second simulation setting served to validate the functioning of the dynamic infected model, and further highlights the importance of ventilation in closed spaces to circulate the air containing the airborne pathogen.

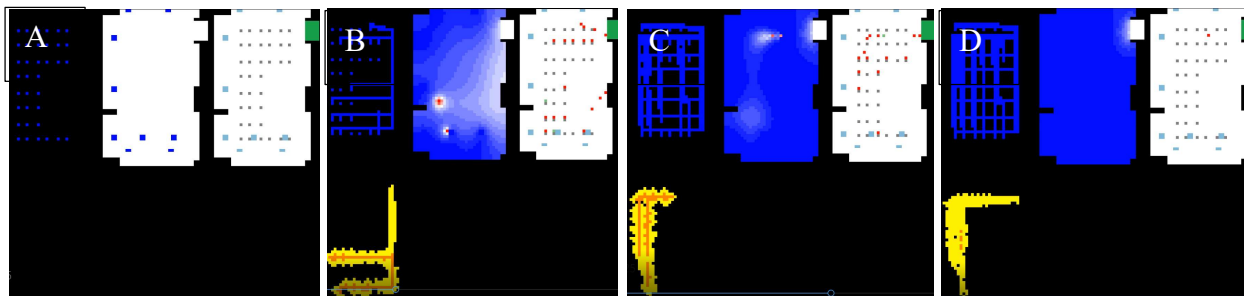
### 5.3 Dynamic Infected Complex Model Simulation

The dynamic infected complex model is the final iteration of the model presented in this paper. It seeks to model the risk of being infected by COVID-19 if an infected person is introduced to a closed setting using a more complex set of rules. It models both the small and large droplets exhaled in the CO<sub>2</sub> of the infected CO<sub>2</sub> sources.

This model was tested and simulated in two parts. First, the computer lab configuration with winds of 25% from the North and West was used. Next, the bus configuration with winds of 25% from the North and West and winds of 75% from the North was tested. The increased north wind within the bus configuration simulates the bus driving with an open window at the front, allowing a strong draft wind into the bus. The remaining parameters set in the configuration file are the same as the dynamic infected model simulations. However, a new block on the bottom left of each image was added to track the risk level of each cell. Black is the basic a risk level of zero, yellow is a risk level of one to two, and orange is a risk level of three to four. Finally, for ease of analysis, the infected CO<sub>2</sub> sources were always assigned the same workstations throughout each simulation.



**Figure 7. Dynamic infected complex model lab simulation with a West wind of 25%.**



**Figure 8. Dynamic infected complex model lab simulation with a North wind of 25%.**

Above is the visualisation of the dynamic infected complex model with both a West and North wind, respectively. As mentioned above, the infected CO<sub>2</sub> sources were assigned to the same workstation in both simulations. This leads to a very similar pathing, which explains the near identical cell risk level path.

As in the second iteration test in the lab, no regular CO<sub>2</sub> source becomes susceptible. This is because the air current introduced into the system improved the efficiency of the ventilation by quickly dissipating the CO<sub>2</sub>. In the simulation of the dynamic infected model, the concentration of CO<sub>2</sub> in the middle right of the lab is a lighter blue comparatively to the simulation of the dynamic infected complex model. This indicates that the air current allows the ventilation to cycle air in much less ventilated locations of the closed space. Although simply circulating the air using a fan doesn't remove the infection contagion, it allows the clean air from the ventilation to better dissipate the CO<sub>2</sub> and therefore the contagion. This demonstrates the importance of air circulation.

The higher risk cells did not change the outcome of this simulation since the room is likely too large, meaning that CO<sub>2</sub> sources do not come on close enough contact for any significant change. Therefore, the analysis of a more confined space like the bus configuration is important.

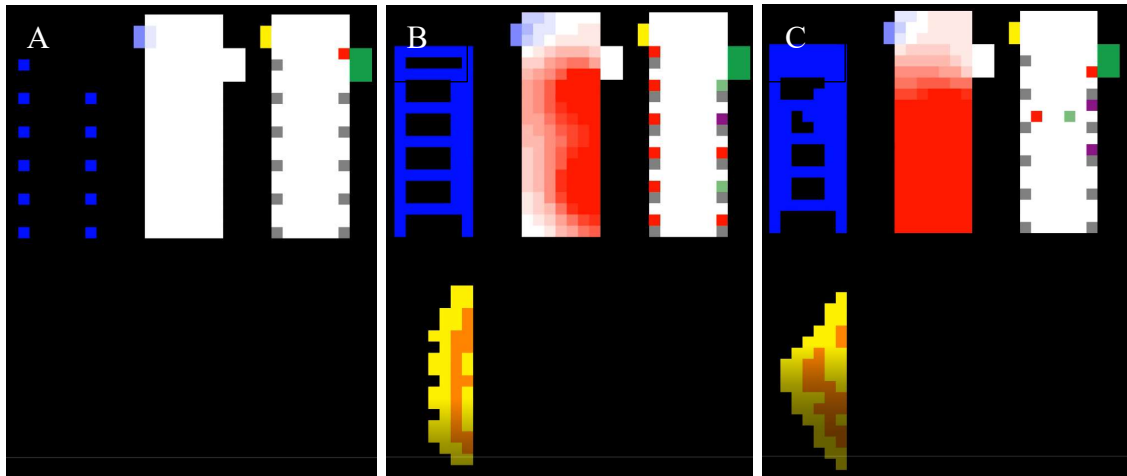


Figure 9. Dynamic infected complex model bus simulation with a West wind of 25%.

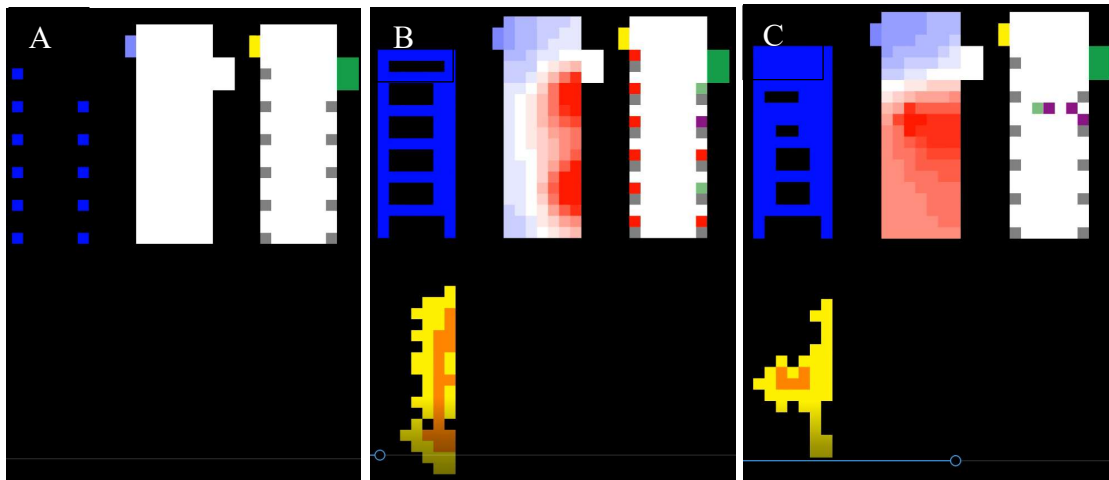


Figure 10. Dynamic infected complex model bus simulation with a North wind of 25%.

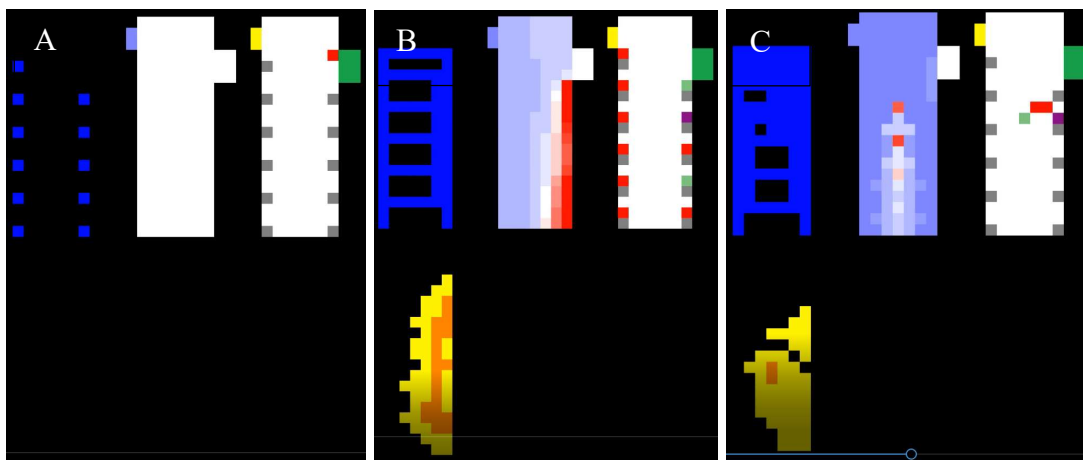


Figure 11. Dynamic infected complex model bus simulation with a North wind of 75%.

The visualization of the dynamic infected bus simulation and the complex bus with a West wind of 25% are very similar. However, the difference is that the wind allowed the CO<sub>2</sub> to spread in the bus much more efficiently. The concentration of CO<sub>2</sub> in previously low concentration areas such as the left side of the bus are much higher when a wind is present, despite blowing in the opposite direction. This demonstrates that with a lack of ventilation, an air current improved rather than inhibited the spread of infected CO<sub>2</sub>.

However, this observation was short lived and likely a special circumstance since, in the bus simulation with a North wind of 25%, the concentration of CO<sub>2</sub> remains very controlled. The concentration of CO<sub>2</sub>, despite all the other configurations being the same, is much lower than both the dynamic infected model lab simulation and the West wind simulation. This is likely because the wind is pushing the clean lower concentration air from the window and door, down into the bus where it maintains a relatively low infected CO<sub>2</sub> level.

The final simulation completed in this model is with a North wind of 75%. This was intended to simulate a bus traveling with an open window. In this simulation, the wind is so strong that the CO<sub>2</sub> can only expand directly behind the CO<sub>2</sub> source. Furthermore, the lower infected concentration air dispersed through the bus much faster, eventually overpowering all CO<sub>2</sub> emissions which can be seen in the third window of Figure 11.

Finally, the risk cell level is relatively similar across all three simulation with only slight variations due to the pathing. The number of susceptible CO<sub>2</sub> did not increase from the dynamic infected model. This is likely because the wind feature helped dissipate the CO<sub>2</sub> more efficiently. The inclusion of wind in the simulations helped reduce the number of susceptible CO<sub>2</sub> sources at the end of the model. This further suggests that air flow in enclosed spaces is essential to ensure proper ventilation and reduce the possibility for COVID-19 infection.

## **6.0 Future Work**

Despite the iterative fashion of implementation, there are still many shortcomings of the model that require further improvement. Two aspects in particular affect the realism of the model: the pathing of the CO<sub>2</sub> sources and the rules for infection. Currently, the CO<sub>2</sub> source pathing functions by having a priority direction based on the position of its objective. This works great in the lab simulation yet has problems with the bus configuration. The bus configuration has workstations, represented by seats, spanning along both walls. This causes problems since the priority direction pathing sometimes sends CO<sub>2</sub> sources along the right wall, under a chair, before traveling up to the door, where they remain stuck because the pathing algorithm either wants to travel up or to the right, but the only option is to move to the left away from its objective. This could be fixed in future iterations by designating certain cells as path cells, where the CO<sub>2</sub> sources will attempt to follow the path until it needs to defer to attain its objective. This would also reduce the sporadic nature of the CO<sub>2</sub> sources, rendering a more realistic flow of movement.

The second improvement is to establish more concrete and realistic rules of infection. Currently, a CO<sub>2</sub> source must be within a threshold concentration for a set exposure time. This

models the need to attain a high enough viral load to overwhelm the antibodies and render a person sick. However, the time and rate at which a person must be exposed is different for each individual, and the configuration used in the simulation doesn't represent a realistic average exposure concentration and time. This would require further analysis of the average concentration of contagion exhaled while breathing, followed by the average exposure time and concentration needed. This data is out of the scope of the project but remains a shortcoming of the model.

Finally, the model's validity is based on the expected behaviour of implementation, rather than its realism. This model requires further testing against known systems and behaviour, to validate its authenticity to a real system. The model is representative of the preliminary research and expected outcomes but is not tested against a known system. This, however, can only be undertaken once the pathing and realistic rules for infection are implemented.

## **7.0 Conclusion**

The iterative implementation of the model allowed for the establishment of a strong foundation by individually testing each new feature to confirm proper functioning. The first iteration, dynamic susceptible model, is comprised of "CO<sub>2</sub> Model with Moving Occupants" and "Model of CO<sub>2</sub> as a Proxy for Infection", both of which are built upon the original CO<sub>2</sub>CS model from [4]. The dynamic susceptible model models the worst-case scenario for COVID-19 infection, assuming that all CO<sub>2</sub> emissions carry contagion. It functioned as expected but demonstrated a serious shortcoming where CO<sub>2</sub> models could infect themselves. The second iteration addressed the previous iteration's shortcoming by adding two new features. The introduction of the infected CO<sub>2</sub> source allowed for the modelling of only the CO<sub>2</sub> that could contain contagion. However, using the lab configuration, the CO<sub>2</sub> sources were too spread out and the ventilation was too efficient for anyone to become susceptible. For this reason, a new setting of a bus was introduced. This much more confined setting with a lack of ventilation proved to be dangerous for its occupants since many CO<sub>2</sub> sources became susceptible. The final iteration and model, the dynamic infected complex model, added a layer of complexity and realism to the model. The third iteration now modeled both large and small droplet contagion by establishing a risk level to air cells based on their distance from the infected sources. Within a meter, a CO<sub>2</sub> source became 4 time more likely to become infected, and within two meters, they were twice as likely, modeling the higher quantity of contagion within large droplets and its higher risk. The second addition was wind. The introduction of an air current inhibited CO<sub>2</sub> containing the contagion to spread reliably in an enclosed setting, and further improved the efficiency of ventilation. This established a large emphasis on the importance of air flow within closed spaces to ensure that all of the air in a room is properly ventilated, instead of just the local air around the ventilation unit.

The final model of the dynamic infected complex model models the risk of COVID-19 infection via aerosolized contagion in an indoor dynamic setting by combining and modifying "CO<sub>2</sub> Model with Moving Occupants" along with "Model of CO<sub>2</sub> as a Proxy for Infection". The model is, however, still far from being realistic and requires the changes described in the Future Work section to produce a more applicable model and simulation.

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- [5] [https://github.com/SimulationEverywhere-Models/Cell-DEVS-CO2\\_spread\\_indoor/tree/f5847a80f04e7d7b663d16a49824fb63dd2562be](https://github.com/SimulationEverywhere-Models/Cell-DEVS-CO2_spread_indoor/tree/f5847a80f04e7d7b663d16a49824fb63dd2562be)