### Lecture 12 Generative Models

sgc

March 24, 2022

## 1 Supervised vs Unsupervised Learning

Supervised Learning: Sample (data + labels) Examples: Classification, regression, object, detection, semantic segmentation, image captioning, etc.

Unsupervised Learning: Sample (data, no labels) Learn Hidden Structure Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

# 2 Generative Modeling

Given training data. generate new samples from same distribution: Learn  $p_model$  that approximates  $p_data$ .

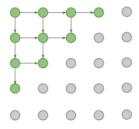
Can learn important features to reconstruct data set.

#### 3 PixelRNN and PixelCNN

FVBN: maximize likelihood of training data  $p(x) = \prod_{i=1}^{n} p(x_i|x_1,...,x_{i-1}) x_i$  is pixel No.i.

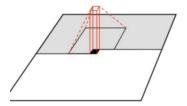
Explicit Model: Explicitly compute likelihood.

PixelRNN generate image start from the corner. Depend on previous pixels.



But it is slow.

PixelCNN: Still start from corner, but now suing a CNN over context region.

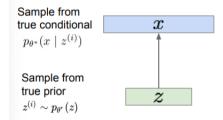


Relatively faster but still slow

#### 4 Variational Autoencoders VAE

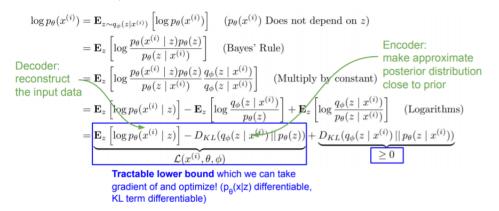
Autoencoders reconstruct data through latent z that represents the most meaningful features.

Autoencoders can be used to make a supervised model more efficient. Variational Autoencoders:

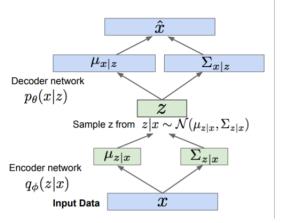


x is an image, and z is latent factors to generate x: Choose p(z) to be simple, p(x-z) is complex (neural network).

Maximize likelihood:  $p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z)$ , but it is intractable. Use distribution  $q_{\phi}(x|z)$  to approximate  $p_{\theta}(x|z)$ 



Optimizing TLB.



Encoder network is used to lessen KL divergence, and Decoder network is used to maximize Expectation. For every minibatch of input data: compute this forward pass, and then backprop.

After training, just sample z from prior and use decoder network.

## 5 Generative Adversarial Networks (GANs)

GANs is a Two-player game consists of the Discriminator network that tries to distinguish between real and fake images and the Generator network that tries to fool the discriminator by generating real-looking images.

Objective function:

Minimax objective function:

Discriminator outputs likelihood in (0,1) of real image

$$\min_{\theta_g} \max_{\theta_d} \left[ \mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$
Discriminator output for for real data x Discriminator output generated fake data G(z)

- Discriminator  $(\theta_d)$  wants to **maximize objective** such that D(x) is close to 1 (real) and D(G(z)) is close to 0 (fake)
- Generator  $(\theta_g)$  wants to **minimize objective** such that D(G(z)) is close to 1 (discriminator is fooled into thinking generated G(z) is real)

Alternate between:

1. Gradient ascent on discriminator

$$\max_{\theta_d} \left[ \mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

2. Instead: Gradient ascent on generator, different objective

$$\max_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(D_{\theta_d}(G_{\theta_g}(z)))$$



Use Gradient ascent get higher gradient for bad samples and works better.

for number of training iterations do

for k steps do

• Sample minibatch of m noise samples  $\{ \boldsymbol{z}^{(1)}, \dots, \boldsymbol{z}^{(m)} \}$  from noise prior  $p_g(\boldsymbol{z})$ .
• Sample minibatch of m examples  $\{ \boldsymbol{z}^{(1)}, \dots, \boldsymbol{z}^{(m)} \}$  from data generating distribution  $p_{
m data}(m{x}).$ • Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^{m} \left[ \log D_{\theta_d}(x^{(i)}) + \log(1 - D_{\theta_d}(G_{\theta_g}(z^{(i)}))) \right]$$

 $\begin{array}{l} \textbf{end for} \\ \bullet \ \text{Sample minibatch of } m \ \text{noise samples} \ \{ \pmb{z}^{(1)}, \dots, \pmb{z}^{(m)} \} \ \text{from noise prior} \ p_g(\pmb{z}). \\ \bullet \ \text{Update the generator by ascending its stochastic gradient (improved objective):} \\ \dots \end{array}$ 

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log(D_{\theta_d}(G_{\theta_g}(z^{(i)})))$$

end for

Some find k==1 more stable.