



POLITECNICO
MILANO 1863

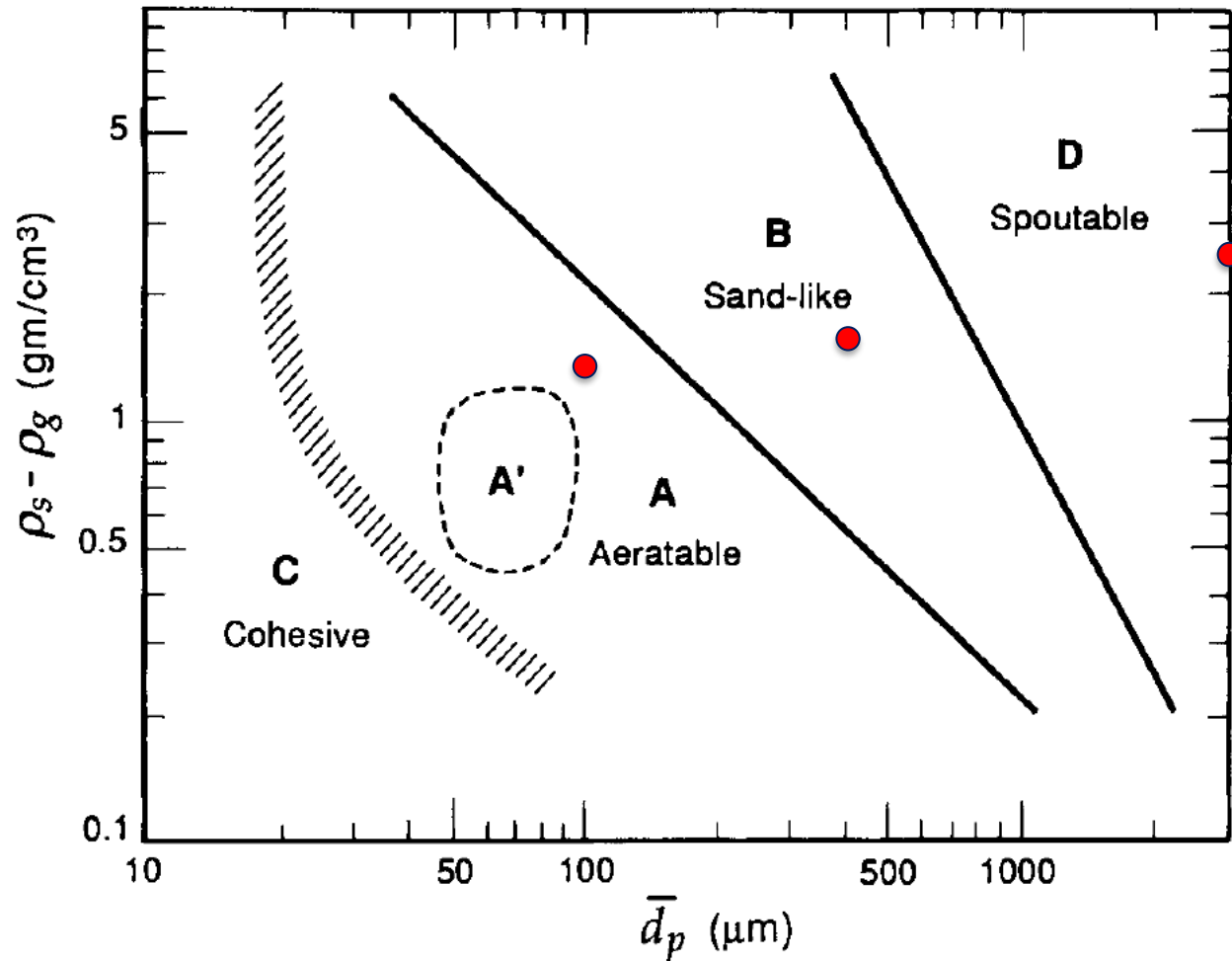
Chemical and Catalytic Reaction Engineering

Practical 10 (second part) – a.a. 2023-2024

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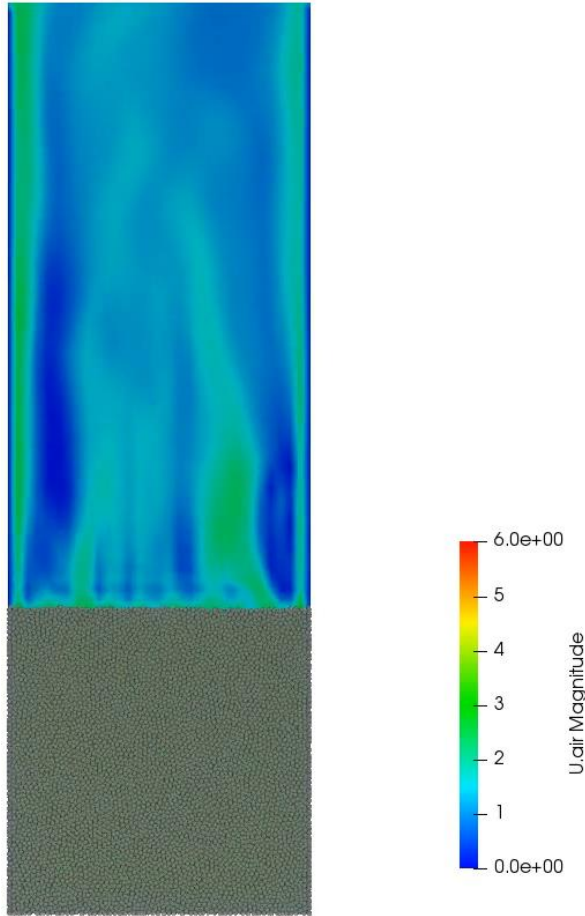
**Laboratory of Catalysis and Catalytic Processes –
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Particle Characteristic: Geldart Classification



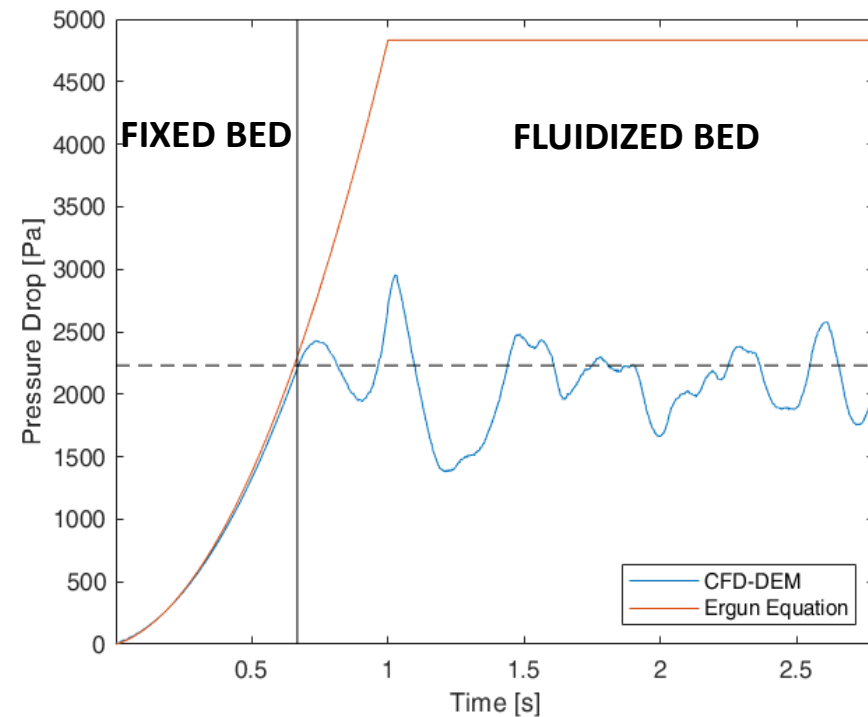
We will investigate three different kind of particles each one belonging to a different Geldart Class and reported in Figure by a red circle.

Geldart D particles



- **Large and dense particles.** The beds composed by these particles are **difficult to fluidize**, thus **high flow rates and minimum fluidization velocities are required** (in the order of m/s). Large bubbles are easily formed
- **Bubble rise velocity is lower than the one of the gas percolating through the emulsion**
- **They are undesirable for chemical operations** (high flow rate and poorer mixing with respect to finer particles) but **sometimes they cannot be avoided** when products are growing on the particles, e.g. in polymerizations

Geldart D particles



- The drag exerted by the gas on these kind of particles is prevalently related to **inertial forces**
- Therefore the Ergun equation shows a **parabolic dependence of reactor pressure drops on the inlet velocity** and in this case time (since velocity increases linearly with time from 0 to 1.5 U_{mf} in 1s in the plot at the left)

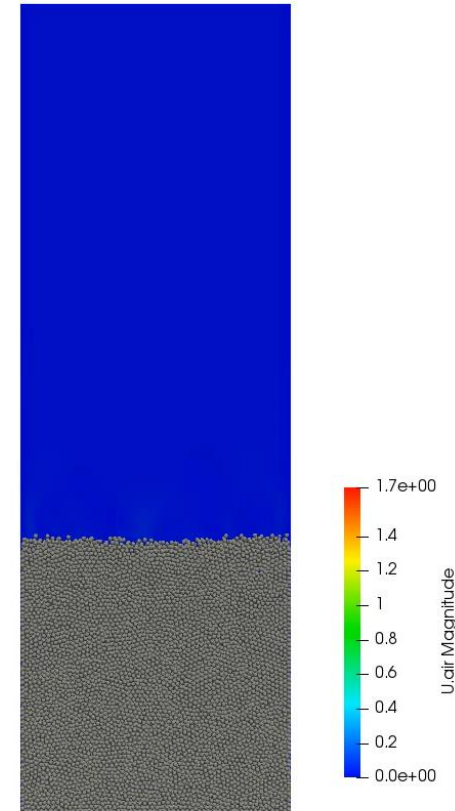
$$\Delta P = \frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed}$$

VISCOUS CONTRIBUTION
INERTIAL CONTRIBUTION

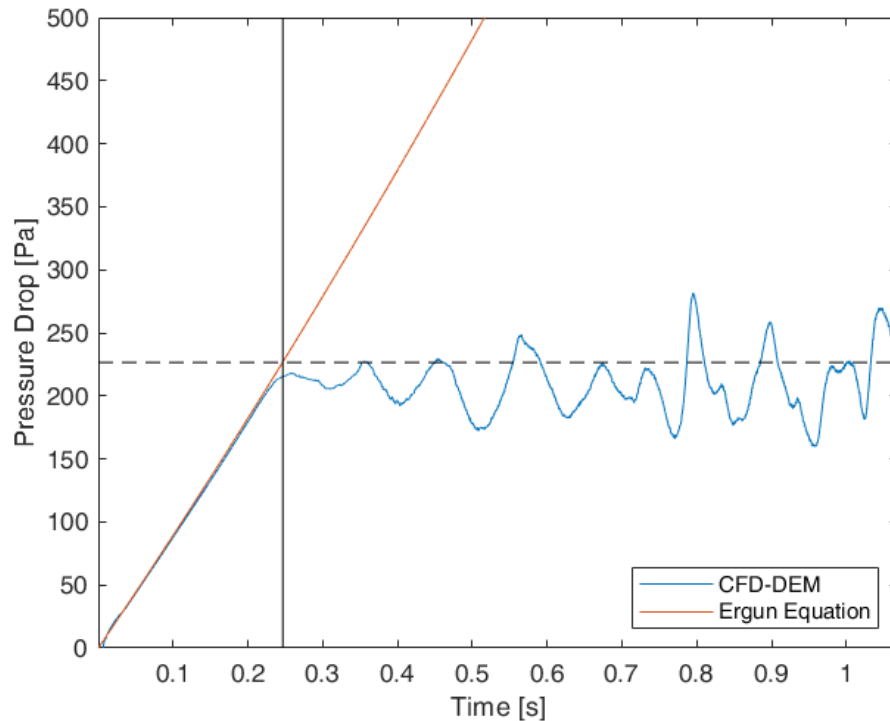
Class B particles

- **Fine «sand-like» particles.** The beds composed by these particles is easy to fluidize, thus **lower flow rates and minimum fluidization velocities are required** (in the order of few cm/s).
- **Bubble rise velocity is higher than the one of the gas percolating through the emulsion**
- **The bed starts to bubble as soon as minimum fluidization condition is achieved.** Bubble size grows roughly linearly with the distance from the inlet of the reactor. Smaller multiple bubbles are obtained with respect to D particles.
- **They are suitable for chemical operations**

Time
0.04 s
Velocity
0.016 m/s



Class B particles



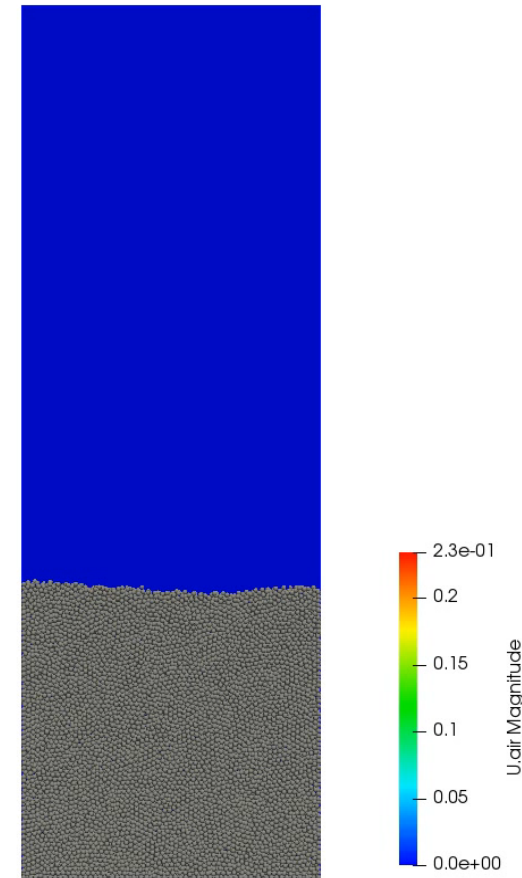
- **The drag exerted** by the gas on these kind of particles is prevalently related to **viscous forces**
- Therefore the Ergun equation shows a **linear dependence of reactor pressure drops on the inlet velocity** and in this case time (since velocity increases linearly with time from 0 to 6 Umf in 1s in the plot at the left)

$$\Delta P = \frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed}$$

VISCOUS CONTRIBUTION INERTIAL CONTRIBUTION

- **Fine aeratable particles.** The beds composed by these particles is easy to fluidize, thus **lower flow rates and minimum fluidization velocities are required** (in the order of few mm/s).
- Bubble rise velocity is higher than the one of the gas percolating through the emulsion
- **A higher number of smaller bubbles** are observable **with respect to B particles.** Moreover, **the bed first homogeneously expand** just above minimum fluidization and, **then, starts to bubble above minimum bubbling velocity.**
- **They are suitable for chemical operations**

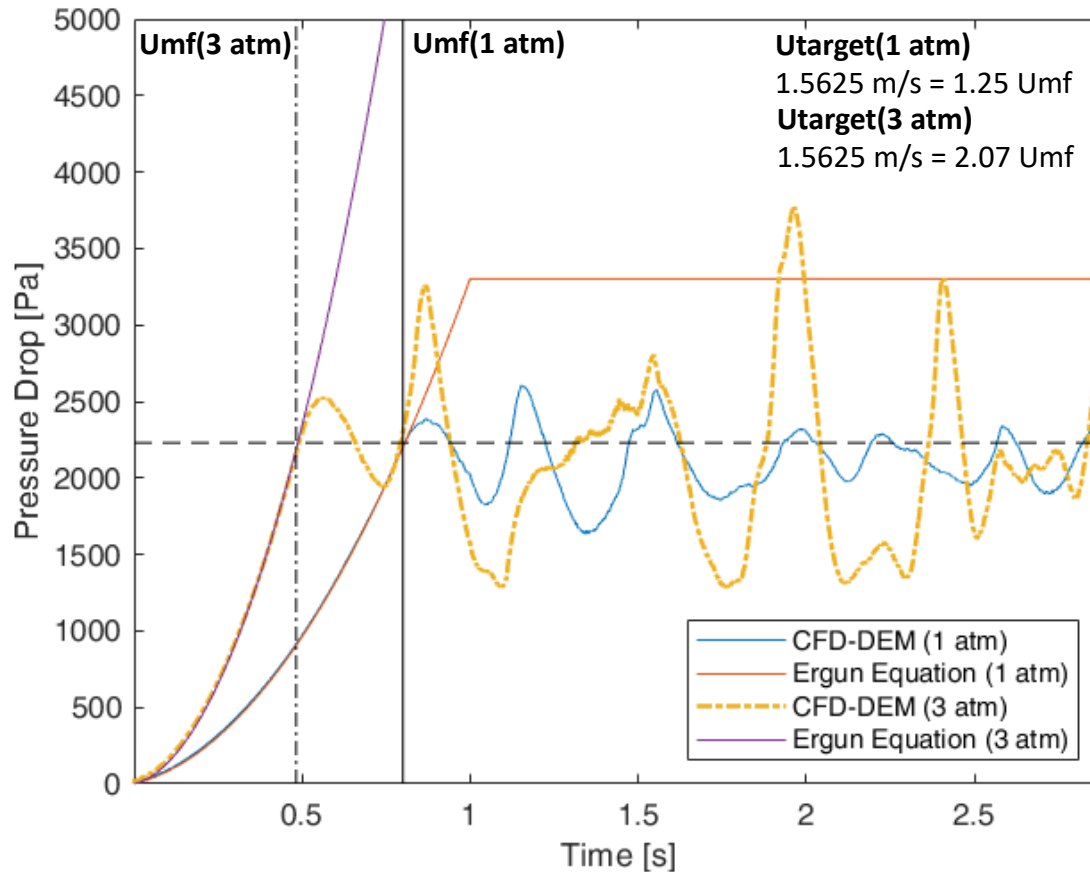
Time
0.00 s
Velocity
0.000 m/s



Minimum Fluidization Point (Geldart D): Pressure Dependence

$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed} = m_{cat}g/A$$

Minimum Fluidization Point (Geldart D): Pressure Dependence



$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed} = m_{cat}g/A$$

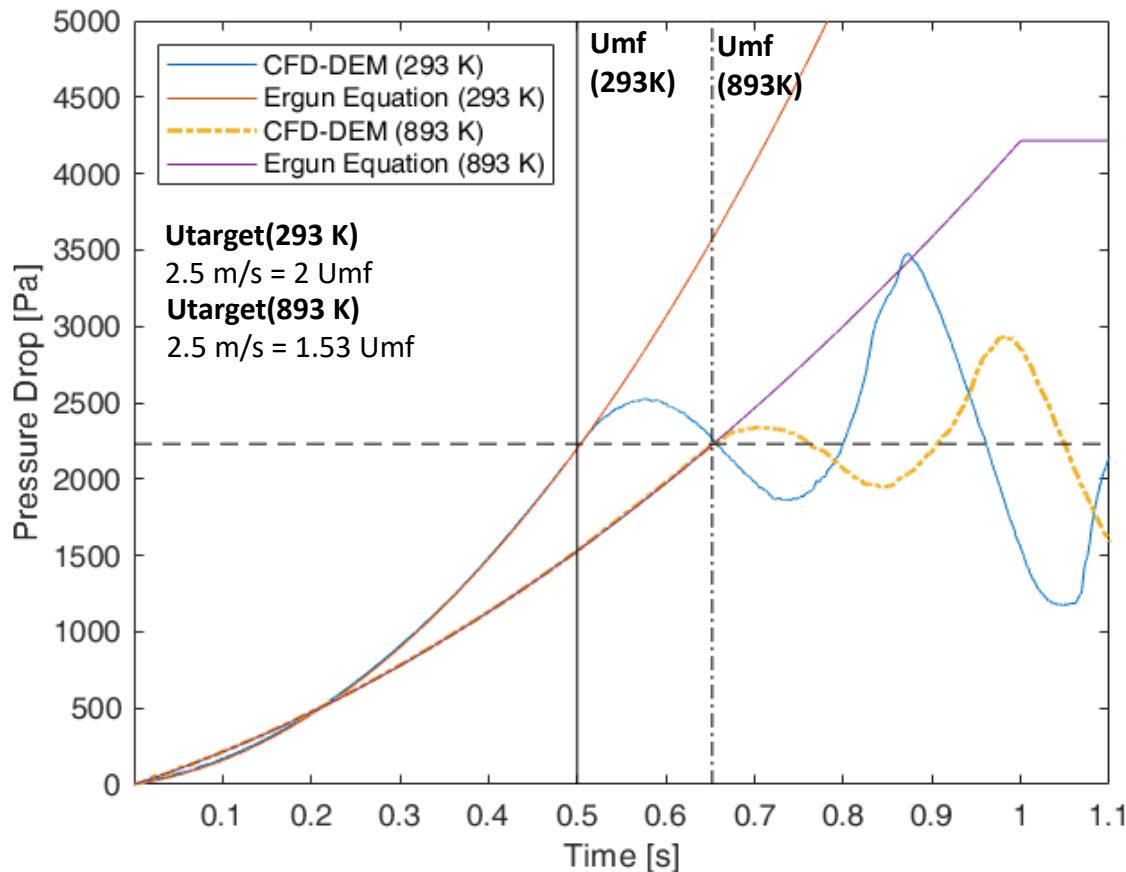
- The **weight** of the bed **does not change** with pressure
- The **density** of the gas **increases** linearly with pressure
- The **viscosity** of a gas is **poorly influenced by pressure**.

As a consequence the minimum fluidization velocity can only decrease with a pressure increment

Minimum Fluidization Point (Geldart D): Temperature Dependence

$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed} = m_{cat}g/A$$

Minimum Fluidization Point (Geldart D): Temperature Dependence



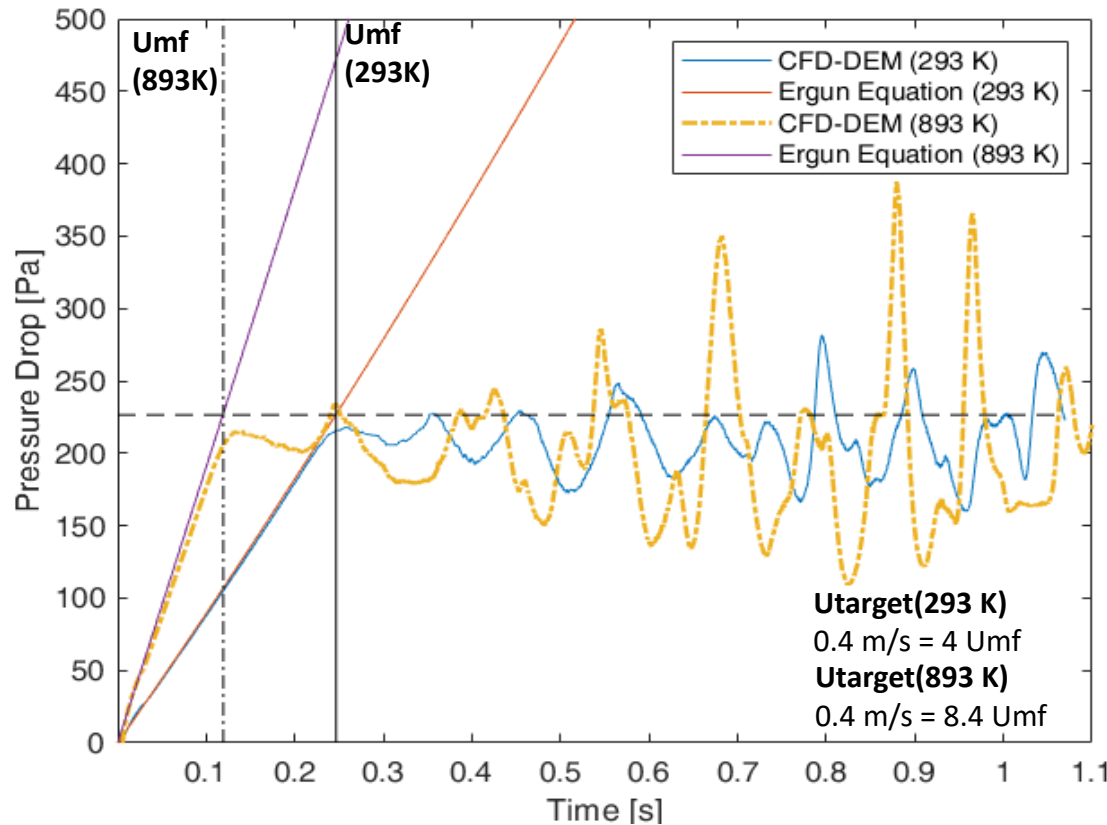
$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed} = m_{cat}g/A$$

- The **weight** of the bed **does not change** with temperature
- The **density** of the gas **decreases** with temperature (from 1.2 to 0.39 kg/m³)
- The **viscosity** of the gas **increases** with temperature (from 1.82e-5 to 3.965e-5 Pa*s)

As a consequence the minimum fluidization velocity increases with a temperature increment.

WHAT WILL HAPPEN IN CASE OF A GELDART B POWDER?

Minimum Fluidization Point (Geldart B): Temperature Dependence



$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed} = m_{cat}g/A$$

- The **weight** of the bed **does not change** with temperature
- The **density** of the gas **decreases** with temperature (from 1.2 to 0.39 kg/m³)
- The **viscosity** of the gas **increases** with temperature (from 1.82e-5 to 3.965e-5 Pa*s)

The effect of temperature on density and viscosity is the same as for Geldart D particles. However B particles are finer and dominated by viscous effects as shown by linear Ergun equation, thus

MINIMUM FLUIDIZATION DECREASES WITH TEMPERATURE!

Investigation of the minimum fluidization point in case of:

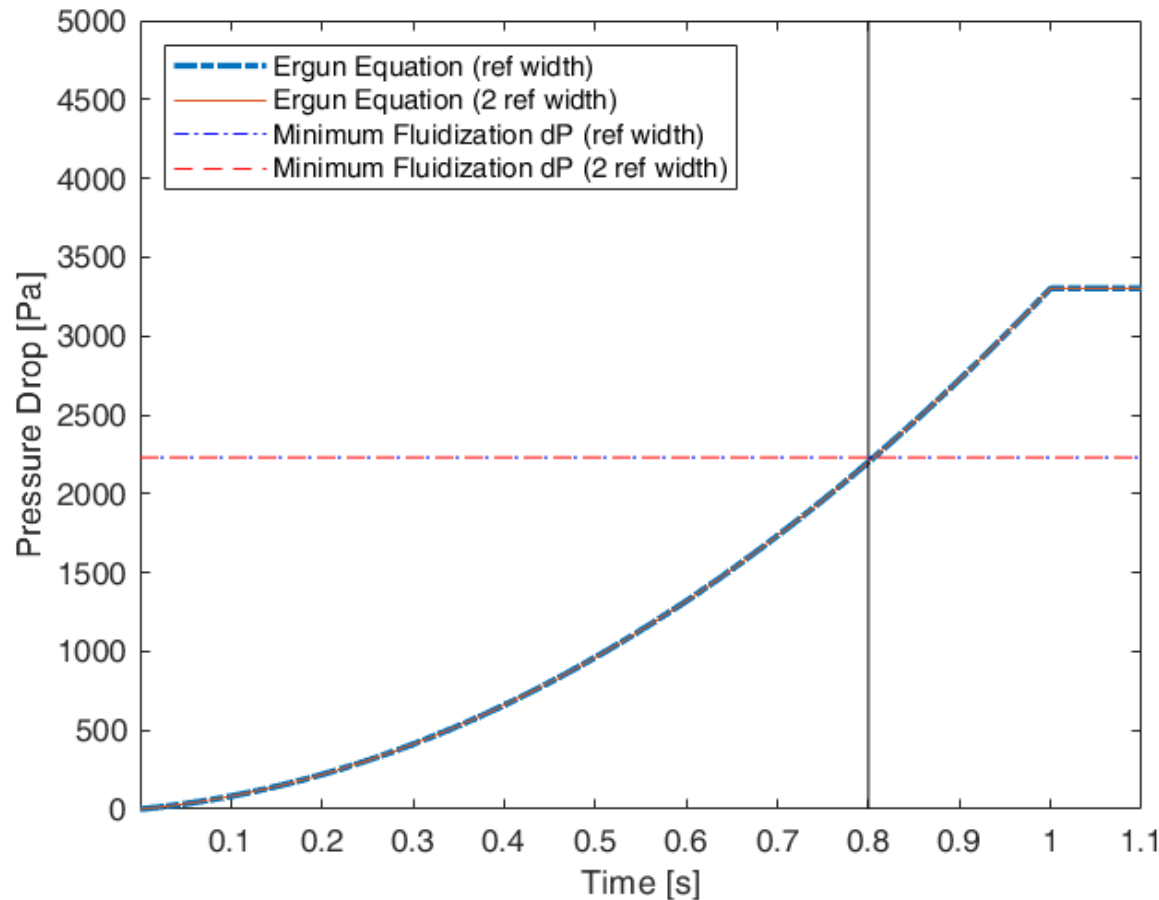
- a pseudo-2D reactor (D particles) which has 2 times the width of a reference test case
- a pseudo-2D reactor which has 2 times the packed bed height of a reference test case

Doubling the width

Reference Reactor

$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed} = m_{cat}g/A_{ref}$$

Doubling the width



Reference Reactor

$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed} = m_{cat}g/A_{ref}$$

New Reactor

$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed} = 2m_{cat}g/(2A_{ref})$$

No difference of Umf

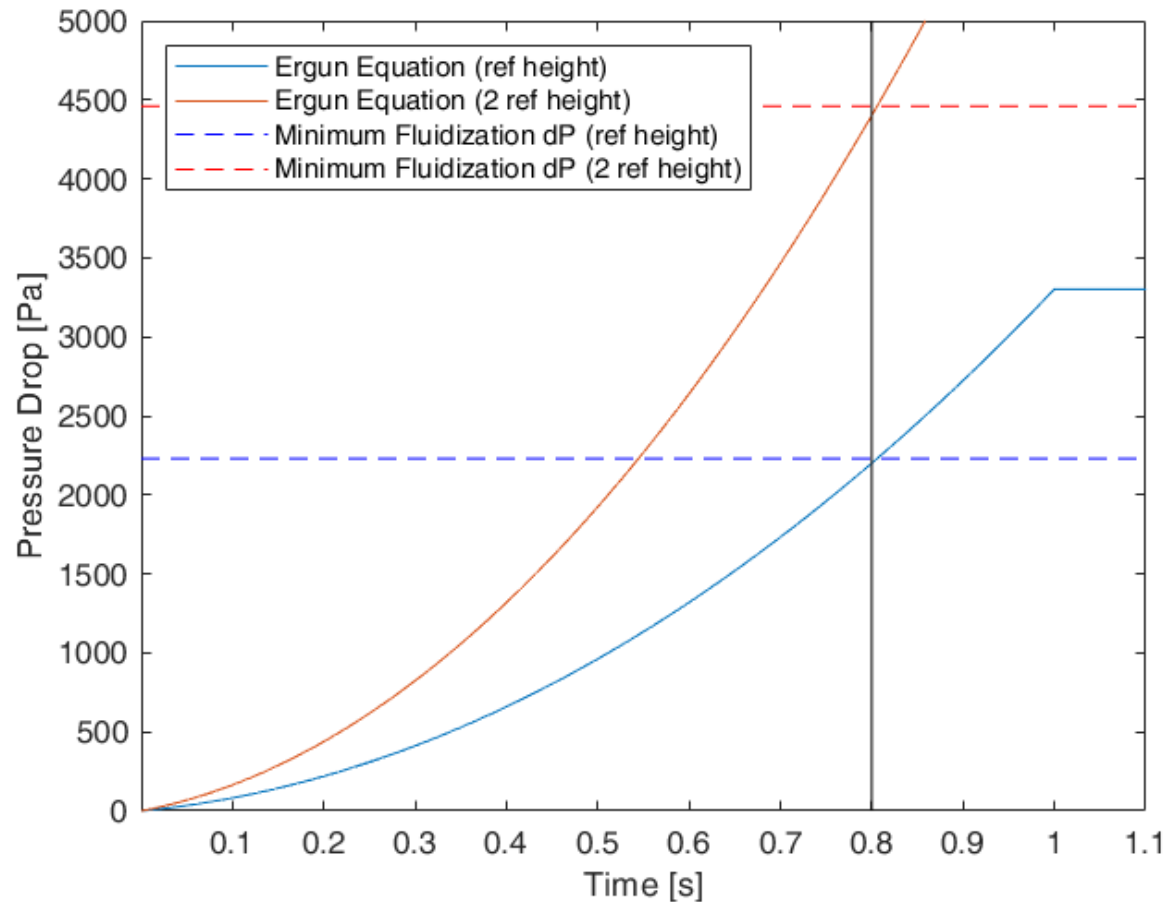
No difference of dp_{mf}

Doubling the height

Reference Reactor

$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed} = m_{cat}g/A_{ref}$$

Doubling the height



Reference Reactor

$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot H_{bed} = m_{cat}g/A_{ref}$$

New Reactor

$$\frac{1}{d_p} \cdot \frac{1-\varepsilon}{\varepsilon^3} \cdot \left(\frac{150(1-\varepsilon)\mu}{d_p} U + 1.75\rho_g U^2 \right) \cdot 2H_{bed} = 2m_{cat}g/A_{ref}$$

No difference of Umf

Different dp_{mf}