Practical 10

Fluidized Bed Reactor

Exercise 1

Maleic Anhydride (MA) is industrially produced by the oxidation of the n-butene. The n-butene diluted in air is fed to a fluidized bed reactor filled with Geldart A particles. In this condition, the solid particles are well mixed into the system allowing isothermal operations. As a first approximation, assume a CSTR behavior of the gas in the emulsion phase. Details of the configuration, catalysts, and operating conditions are given below. The reaction network is given by the following three reactions:

R1:
$$C_4H_{10} + 3.5O_2 \rightarrow C_4H_2O_3 + 4H_2O$$

R2:
$$C_4H_{10} + 5.5O_2 \rightarrow 2CO + 5H_2O + 2CO_2$$

R3:
$$C_4H_2O_3 + O_2 \rightarrow 4CO + H_2O$$

The system can be considered a mixture of ideal gases.

Considering a three-phase Kunii-Levenspiel model:

- 1) Calculate the value of the minimum fluidization velocity and the maximum fluidization ratio that can be adopted for this system.
- 2) Calculate the pressure drops across the reactor.
- 3) Calculate the fraction of the molar gas flow rate in the bubble phase.
- 4) Report the mass fraction profile of the n-butene in the bubble, cloud, and emulsion phases along the tube (report the qualitative graph with the values at 0.5, 1, 2, and 2.5 m).
- 5) Assess if slugging mode can occur in the reactor.
- 6) Assess what would be the impact on the outlet conversion in case the gas in the emulsion is considered to be static.

Data:

Reaction kinetics (partial pressures in atm, reaction rate in mol/kg_{cat}/s):

$$r_1 = k_1 \frac{p_{C_4 H_{10}}^{0.54}}{1 + k_{c_4 H_2 O_3} p_{c_4 H_2 O_3}}$$
$$r_2 = k_2 p_{c_4 H_{10}}$$

$$r_3 = k_3 \frac{p_{c_4 H_2 O_3}}{\left(1 + k_{c_4 H_2 O_3} p_{c_4 H_2 O_3}\right)^2}$$

With:

$$\begin{split} k_1 &= 2.2 \cdot 10^{-3} \exp \left(\frac{60}{T_{ref} R_{gas}} \left(1 - \frac{T_{ref}}{T_{in}} \right) \right) \quad [\frac{mol}{kg_{cat} \, s \, atm^{0.4}}] \\ k_2 &= 0.3 \cdot 10^{-3} \exp \left(\frac{45}{T_{ref} R_{gas}} \left(1 - \frac{T_{ref}}{T_{in}} \right) \right) \quad [\frac{mol}{kg_{cat} \, s \, atm^{0.4}}] \\ k_3 &= 0.22 \cdot 10^{-2} \exp \left(\frac{190}{T_{ref} R_{gas}} \left(1 - \frac{T_{ref}}{T_{in}} \right) \right) \quad [\frac{mol}{kg_{cat} \, s \, atm}] \\ k_{C_4 H_2 O_3} &= 185 \, [atm^{-1}] \\ T_{ref} &= 673 \, [K] \\ R_{gas} &= 0.008314 \, [\frac{kJ}{mol}] \end{split}$$

Operating conditions:

Outlet pressure = 1 atm

Feed Temperature = 430 °C

Diluted conditions: n-butene to air ratio (v/v) 4% (LFL 1.8%)

Inlet gas flowrate = 25 cm/s

Reactor configuration:

Reactor diameter = 5 m

Gamma bubble = 0.005

 $f_w = 0.2$

Catalyst:

Sphere diameter = 125 micron

Catalyst density = 1200 kg/m^3

Mass of catalyst = 27318 kg

$$\varepsilon_{mf} = 0.42$$

Mixture properties:

Diffusion coefficient = $3 \cdot 10^{-5} \text{ m}^2/\text{s}$

Viscosity: 3.28 10⁻⁵ Pa s

Ergun equation:

$$\frac{\Delta P}{L} = 150 \frac{(1-\varepsilon)^2}{\varepsilon^3} \frac{\mu v_g}{d_p^2} + 1.75 \frac{(1-\varepsilon)}{\varepsilon^3} \frac{\rho v_g^2}{d_p}$$

Correlations:

$$v_{single\ bubble} =\ 0.711 (gd_{bubble})^{0.5}$$

$$v_{bubble} = (v_{in} - v_{mf}) + v_{single\ bubble}$$

$$f_{cl} = 3 \frac{\frac{v_{mf}}{\varepsilon_{mf}}}{v_{bubble} - \frac{v_{mf}}{\varepsilon_{mf}}}$$

$$\delta = \frac{\left(v_{in} - v_{mf}\right)}{\left(v_{bubble} - \left(1 + \left(f_{cl} + f_{w}\right)\right)v_{mf}\right)}$$

$$\gamma_{cloud} = (1 - \epsilon_{mf})(f_{cl} + f_{w})$$

$$\gamma_{emulsion} = (1 - \epsilon_{mf}) * \frac{(1 - \delta)}{\delta} - \gamma_{cloud}$$

$$\epsilon_{bed} = 1 - (\delta * \text{Gamma bubble} + (1 - \delta) * (1 - \epsilon_{mf}))$$

$$\label{eq:loss} \mathcal{L} = \frac{m_{cat}}{rho_{cat}(Area_{reactor})(1-\varepsilon_{\mathrm{bed}})}$$

$$K_{bc} = 4\left(\frac{v_{mf}}{d_{bubbles}}\right) + 5.85(D_{mix}^{0.5} * \frac{g^{0.25}}{d_{bubbles}^{\frac{5}{4}}})$$

$$K_{ce} = 6.77 \left(\frac{D_{mix} \varepsilon_{mf} v_{bubble}}{d_{bubbles}^3} \right)^{0.5}$$

$$d_{bubble,max} = 0.652 \left(\frac{\pi d_{reactor}^2}{4} (v_{in} - v_{mf}) \right)^{0.4} [cm]$$

$$v_{terminal} = \frac{d_{particle}^2 g(\rho_{particle} - \rho_{gas})}{18 \mu}$$