Adversarial examples in deep learning

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Machine learning Supervised learning



Machine learning is a subfield of artificial intelligence.

Intuitively We want to learn from and make predictions on data.

Technically We want to build a model that approximate well (e.g. minimize a loss function) an unknown function.

It is important to note that the function we want to approximate may or may not have a closed form.

Regression

Polynomial
$$(x, y, z) \rightarrow f(x, y, z)$$

House price (surface, nb rooms, city)
$$\rightarrow$$
 price

Classification

Image classification pixel values
$$\rightarrow$$
 cat or dog

Text classification $list of words \rightarrow spam or valid email$

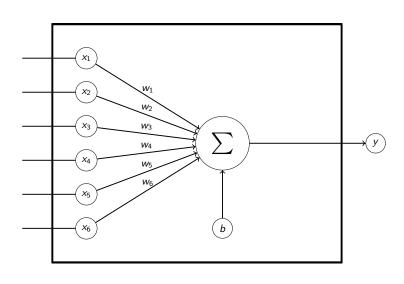
Deep learning



Deep learning is a subfield of machine learning in which we use artificial neural networks to make predictions.

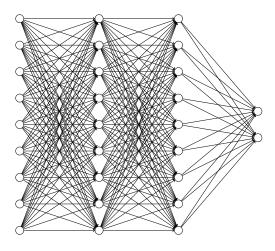
An artificial neural networks is a computation model loosely based on the human brain. It aims to mimic electric signals travelling through neurons in order to make computations.



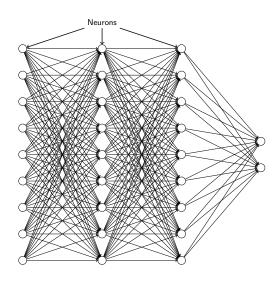


$$y = w_1x_1 + w_2x_2 + w_3x_3 + w_4x_4 + w_5x_5 + w_6x_6 + b$$

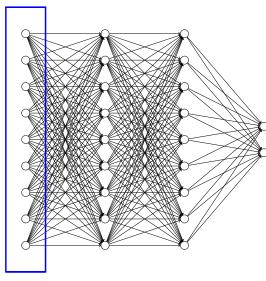




DISAITER

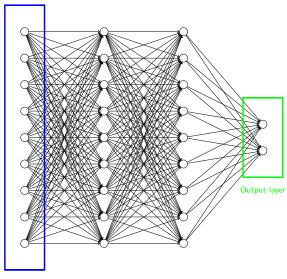


DISAITEK



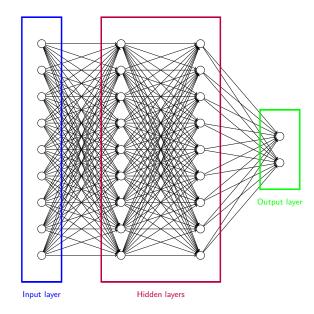
Input layer

DISAITEK



Input layer





Problem with this definition



We now have a quite complicated framework to compute linear functions.

Neuron linear function

Neural network linear combination of neuron outputs

To approximate non linear functions, we would like to have a non linear model.

Problem with this definition



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Neuron linear function

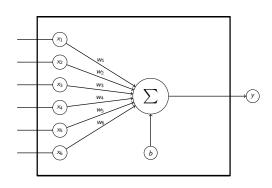
Neural network linear combination of neuron outputs

To approximate non linear functions, we would like to have a non linear model.

Solution: add nonlinearity to neurons.

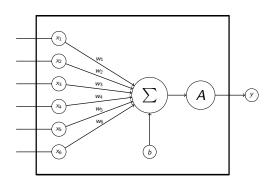
Neuron with activation





Neuron with activation

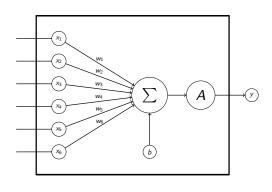




$$A(x) = \begin{cases} 0 & \text{if } x < 0 \\ 1 & \text{otherwise} \end{cases}$$

Neuron with activation



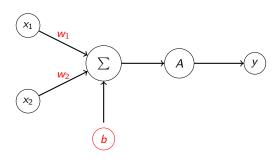


$$A(x) = \begin{cases} 0 & \text{if } x < 0 \\ 1 & \text{otherwise} \end{cases}$$

$$y = A(w_1x_1 + w_2x_2 + w_3x_3 + w_4x_4 + w_5x_5 + w_6x_6 + b)$$



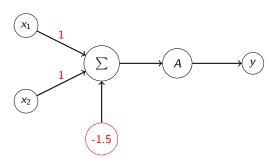
Binary AND gate



$$A(w_1x_1 + w_2x_2 + b) = x_1 \text{ AND } x_2$$



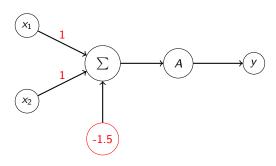
Binary AND gate



$$A(w_1x_1 + w_2x_2 + b) = x_1 \text{ AND } x_2$$



Binary AND gate

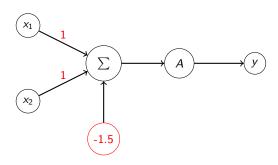


$$A(w_1x_1 + w_2x_2 + b) = x_1 \text{ AND } x_2$$

$$x_1 = 0, x_2 = 1.$$
 $y = A(0 + 1 - 1.5) = A(-0.5) = 0$



Binary AND gate



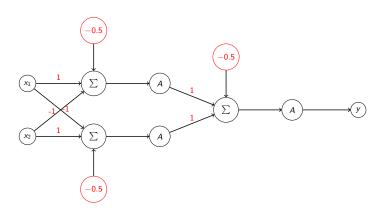
$$A(w_1x_1 + w_2x_2 + b) = x_1 \text{ AND } x_2$$

$$x_1 = 0, x_2 = 1.$$
 $y = A(0 + 1 - 1.5) = A(-0.5) = 0$

$$x_1 = 1, x_2 = 1.$$
 $y = A(1 + 1 - 1.5) = A(0.5) = 1$

Computation example Binary XOR gate







One way to measure the complexity of a neural network is its number of parameters.



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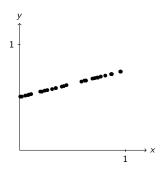
- XOR network: 9 parameters
- 1000 classes image classification (VGG16 network): 138,357,544 parameters

We should probably look for a way to tune these parameters automatically otherwise it is going to get *really* boring *really* quickly.

Parameter tuning Line approximation



We have a few sample points and we want to find a line that approximate these points.



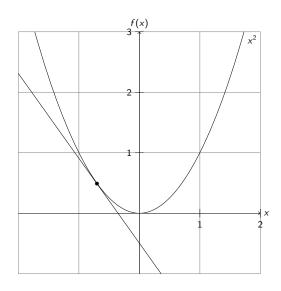
Our model is just a line

$$y_{pred} = ax + b$$

We want to find a and b to best match our samples.

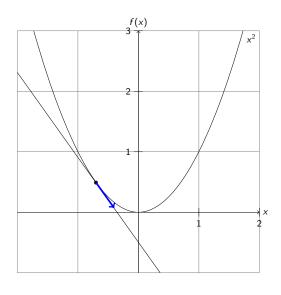
Parameter tuning Gradient descent concept





Parameter tuning Gradient descent concept





Optimization



First we have a define a loss that measures how good our predictions are.

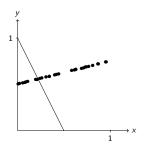
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

and now, we compute how the loss is affected by small changes of a and b:

$$\frac{dI}{da} = 2x(ax + b - y) \qquad \qquad \frac{dI}{db} = 2(ax + b - y)$$



We start with random values: a = -2 and b = 1



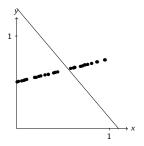
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = -2.00$$
 $b = 1.00$ $\frac{\overline{dI}}{da} = -1.07$ $\frac{\overline{dI}}{db} = -1.37$ $\overline{I(x, y, a, b)} = 0.860367$



We start with random values: a = -2 and b = 1



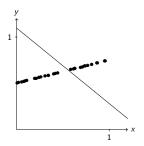
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = -1.18$$
 $b = 1.30$ $\frac{\overline{dl}}{da} = -0.17$ $\frac{\overline{dl}}{db} = 0.09$ $\overline{l(x, y, a, b)} = 0.159420$



We start with random values: a = -2 and b = 1



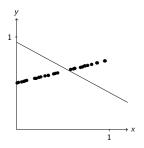
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = -0.82$$
 $b = 1.10$ $\frac{\overline{dl}}{da} = -0.13$ $\frac{\overline{dl}}{db} = 0.07$ $\overline{l(x, y, a, b)} = 0.088204$



We start with random values: a = -2 and b = 1



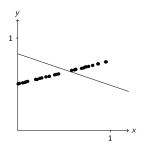
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = -0.54$$
 $b = 0.94$ $\frac{\overline{dl}}{da} = -0.09$ $\frac{\overline{dl}}{db} = 0.05$ $\overline{l(x, y, a, b)} = 0.048802$



We start with random values: a = -2 and b = 1



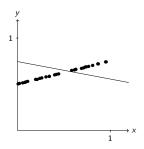
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = -0.34$$
 $b = 0.83$ $\frac{\overline{dl}}{da} = -0.07$ $\frac{\overline{dl}}{db} = 0.04$ $\overline{l(x, y, a, b)} = 0.027001$



We start with random values: a = -2 and b = 1

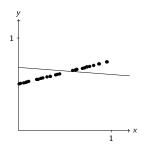


$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = -0.19$$
 $b = 0.75$ $\frac{\overline{dl}}{da} = -0.05$ $\frac{\overline{dl}}{db} = 0.03$ $\overline{l(x, y, a, b)} = 0.014939$

We start with random values: a = -2 and b = 1



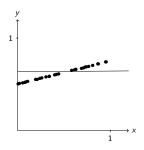
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = -0.08$$
 $b = 0.68$ $\frac{\overline{dl}}{da} = -0.04$ $\frac{\overline{dl}}{db} = 0.02$ $\overline{l(x, y, a, b)} = 0.008266$



We start with random values: a = -2 and b = 1



$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.01$$
 $b = 0.64$ $\frac{\overline{dl}}{da} = -0.03$ $\frac{\overline{dl}}{db} = 0.02$ $\overline{l(x, y, a, b)} = 0.004573$



We start with random values: a = -2 and b = 1



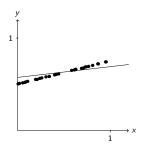
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.07$$
 $b = 0.60$ $\frac{\overline{dl}}{da} = -0.02$ $\frac{\overline{dl}}{db} = 0.01$ $\overline{l(x, y, a, b)} = 0.002530$



We start with random values: a = -2 and b = 1



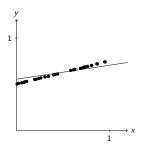
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.12$$
 $b = 0.58$ $\frac{\overline{dl}}{da} = -0.02$ $\frac{\overline{dl}}{db} = 0.01$ $\overline{l(x, y, a, b)} = 0.001400$



We start with random values: a = -2 and b = 1

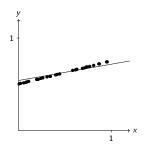


$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.15$$
 $b = 0.56$ $\frac{\overline{dl}}{da} = -0.01$ $\frac{\overline{dl}}{db} = 0.01$ $\overline{l(x, y, a, b)} = 0.000775$

We start with random values: a = -2 and b = 1



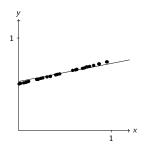
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.18$$
 $b = 0.54$ $\frac{\overline{dl}}{da} = -0.01$ $\frac{\overline{dl}}{db} = 0.00$ $\overline{l(x, y, a, b)} = 0.000429$



We start with random values: a = -2 and b = 1



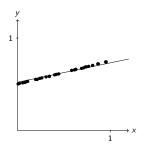
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.19$$
 $b = 0.53$ $\frac{\overline{dl}}{da} = -0.01$ $\frac{\overline{dl}}{db} = 0.00$ $\overline{l(x, y, a, b)} = 0.000237$



We start with random values: a = -2 and b = 1



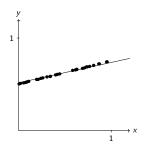
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.21$$
 $b = 0.52$ $\frac{\overline{dl}}{da} = 0.00$ $\frac{\overline{dl}}{db} = 0.00$ $\overline{l(x, y, a, b)} = 0.000131$



We start with random values: a = -2 and b = 1

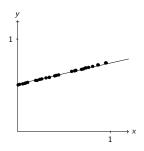


$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.22$$
 $b = 0.52$ $\frac{\overline{dl}}{da} = 0.00$ $\frac{\overline{dl}}{db} = 0.00$ $\overline{l(x, y, a, b)} = 0.000073$

We start with random values: a = -2 and b = 1

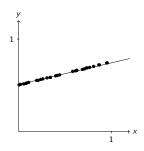


$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.23$$
 $b = 0.51$ $\frac{\overline{dl}}{da} = 0.00$ $\frac{\overline{dl}}{db} = 0.00$ $\overline{l(x, y, a, b)} = 0.000040$

We start with random values: a = -2 and b = 1



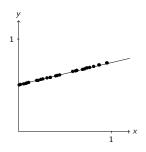
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.23$$
 $b = 0.51$ $\frac{dI}{da} = 0.00$ $\frac{dI}{db} = 0.00$ $\overline{I(x, y, a, b)} = 0.000022$



We start with random values: a = -2 and b = 1



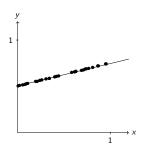
$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.24$$
 $b = 0.51$ $\frac{\overline{dl}}{da} = 0.00$ $\frac{\overline{dl}}{db} = 0.00$ $\overline{l(x, y, a, b)} = 0.000012$



We start with random values: a = -2 and b = 1

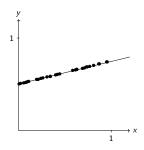


$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.24$$
 $b = 0.51$ $\frac{\overline{dl}}{da} = 0.00$ $\frac{\overline{dl}}{db} = 0.00$ $\overline{l(x, y, a, b)} = 0.000007$

We start with random values: a = -2 and b = 1



$$I(x, y, a, b) = (y - y_{pred})^2 = (y - (ax + b))^2$$

Then, we compute the average of the gradient along all (x, y) couples

$$a = 0.24$$
 $b = 0.50$ $\frac{\overline{dl}}{da} = 0.00$ $\frac{\overline{dl}}{db} = 0.00$ $\overline{l(x, y, a, b)} = 0.000004$

Parameter tuning Problem with ANN



Using gradient descent, we know how to minimize (or at least reach a local minima) a differentiable function.

Parameter tuning



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Problem: The function computed by our neural network is not differentiable because of the activation function.

$$A(x) = \begin{cases} 0 & \text{if } x < 0 \\ 1 & \text{otherwise} \end{cases}$$

Parameter tuning Problem with ANN



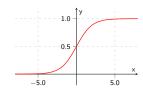
Using gradient descent, we know how to minimize (or at least reach a local minima) a differentiable function.

Problem: The function computed by our neural network is not differentiable because of the activation function.

$$A(x) = \begin{cases} 0 & \text{if } x < 0 \\ 1 & \text{otherwise} \end{cases}$$

Solution: We replace it by a differentiable function that does the same job.

$$A(x) = \frac{1}{1 + e^{-x}}$$



What is an adversarial example?

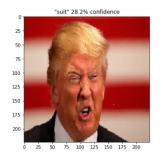


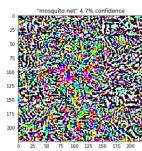
An adversarial example is a sample of input data which has been modified very slightly in a way that is intended to cause a machine learning classifier to misclassify it.

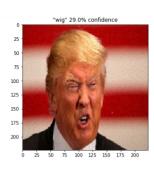
What is an adversarial example?



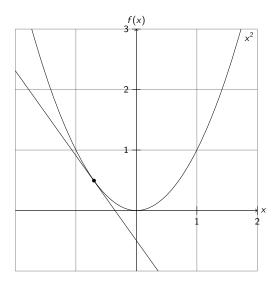
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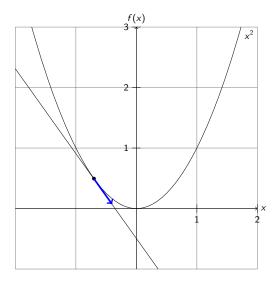






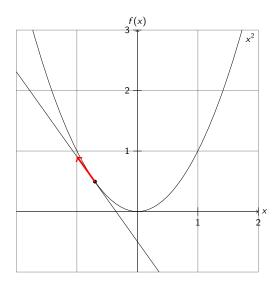






Optimization





De-optimization

Being evil



In our previous example, we have modified the model in order to minimize the loss.

$$y = ax + b$$

Being evil

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$$y = ax + b$$

Now suppose we are an attacker who wants to maximize the loss of a model, its parameters being fixed. The only thing we can modify are the inputs.

$$L(x, y, a, b) = (y - (ax + b))^{2}$$

Being evil



In our previous example, we have modified the model in order to minimize the loss.

$$y = ax + b$$

Now suppose we are an attacker who wants to maximize the loss of a model, its parameters being fixed. The only thing we can modify are the inputs.

$$L(x, y, a, b) = (y - (ax + b))^{2}$$

In order to do this, we compute how the loss is affected by small changes of the input.

$$\frac{\mathrm{d}L}{\mathrm{d}x} = 2a(ax + b - y)$$

We can now make imperceptible changes to an input that will increase the loss value.

Neural networks



Everything works the same way when working with a neural network on an image classification task.

We also have a differentiable *loss function* (often *categorical cross entropy*), model *parameters* (the *weights* of the neural network) and *inputs* (*pixel values* in the case of images) that we can modify to increase the loss.

The ultimate goal is to make our input cross the decision boundary.

Random noise perturbation

DISAITEK

Do we really need to do that?

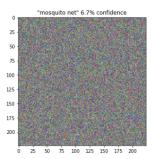


Random noise perturbation



Yep, we really do











Let x be the original image, θ the parameters of the model, y the target associated with x and $L(\theta, x, y)$ the loss function.

We compute the gradient of the loss function according to the input pixels.

$$\nabla_{x}L(\theta,x,y)$$

The perturbation is the signs of these derivatives multiplied by a small number ε .

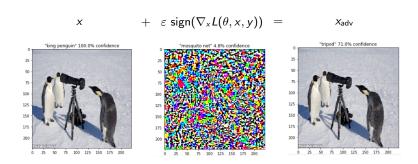
$$\eta = \varepsilon \operatorname{sign}(\nabla_{\mathsf{x}} L(\theta, \mathsf{x}, \mathsf{y}))$$

The final adversarial sample is the sum of the original image and the perturbation.

$$x_{adv} = x + \eta$$

Fast Gradient Sign Method VGG16 network





Black-box attack [Papernot et al. 2016] or good luck getting gradients out of your self-driving car







Transferability of adversarial samples

We can train a new model M' to solve the same classification task as the target model M.



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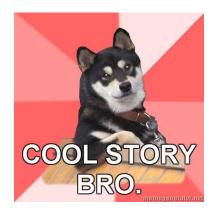
What if we do not have a training set for the target network? Well... build one using M predictions.

"After labeling 6,400 synthetic inputs to train our substitute (an order of magnitude smaller than the training set used by MetaMind) we find that their DNN misclassifies adversarial examples crafted with our substitute at a rate of 84.24%"

- Papernot et al., about their attack on the MetaMind deep neural network.

Adversarial examples in the physical world [Kurakin et al. 2017] or good luck attacking a self-driving car with your USB flash drive



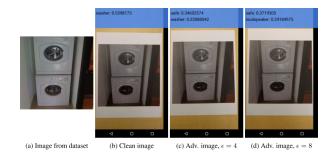


Adversarial examples in the physical world [Kurakin et al. 2017]



In real world scenarios, the target network does not take our image files as input. It acquires the data by the network's system (e.g. a camera).

It also works, for free.



"We used images taken from a cell-phone camera as a input to an Inception v3 image classification neural network. We showed that in such a set-up, a significant fraction of adversarial images crafted using the original network are misclassified even when fed to the classifier through the camera."

- Kurakin et al

White-box defense Adversarial training



We can generate adversarial samples and train the network to produce the correct classification on these new data points.

- Works against FGSM
- Expensive
- Does not defend subtler white-box attacks (e.g. I-FGSM or RAND+FGSM)
- Does not defend against <u>black-box attack</u>

Black-box defense



Ensemble adversarial training [Tramèr et al. May 2017]

Augment training data with adversarial inputs from a number of fixed pre-trained models.

- Best defense so far against black-box adversary
- Does not defend subtle white-box attacks

Error rate from 15.5% to 3.9% between adversarial trained and ensemble adversarial trained model on MNIST for a black-box attack.

Defending machine learning Wide open problem



"Most defenses against adversarial examples that have been proposed so far just do not work very well at all, but the ones that do work are not adaptive. This means it is like they are playing a game of whack-a-mole: they close some vulnerabilities, but leave others open."

- Ian Goodfellow, Nicolas Papernot, February 2017

References



Research papers:

- Goodfellow, I. J., Shlens, J., & Szegedy, C. (2014). Explaining and harnessing adversarial examples. arXiv preprint arXiv:1412.6572.
- Papernot, N., McDaniel, P., Goodfellow, I., Jha, S., Celik, Z. B., & Swami, A. (2016). Practical black-box attacks against deep learning systems using adversarial examples. arXiv preprint arXiv:1602.02697.
- Kurakin, A., Goodfellow, I., & Bengio, S. (2016). Adversarial examples in the physical world. arXiv preprint arXiv:1607.02533.
- Tramèr, F., Kurakin, A., Papernot, N., Boneh, D., & McDaniel, P. (2017). Ensemble Adversarial Training: Attacks and Defenses. arXiv preprint arXiv:1705.07204.
- Tramèr, F., Papernot, N., Goodfellow, I., Boneh, D., & McDaniel, P. (2017). The Space of Transferable Adversarial Examples. arXiv preprint arXiv:1704.03453.

Implementations:

- github.com/tensorflow/cleverhans
- github.com/rodgzilla/machine_learning_adversarial_examples

Papernot algorithm



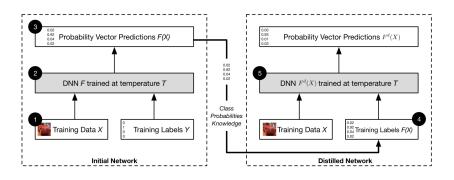
This algorithm iteratively computes the adversarial saliency value S(x,t)[i] of pixel i of the image x according to the class t.

$$S(x,t)[i] = \begin{cases} 0 & \text{if } \frac{\mathrm{d}L_t}{\mathrm{d}x_i}(x) < 0 & \text{or } \sum_{j \neq t} \frac{\mathrm{d}L_j}{\mathrm{d}x_i}(x) > 0 \\ \frac{\mathrm{d}L_t}{\mathrm{d}x_i}(x) \left| \sum_{j \neq t} \frac{\mathrm{d}L_j}{\mathrm{d}x_i}(x) \right| & \text{otherwise.} \end{cases}$$

and use it iteratively to produce x_{adv} classified as t by the network.

Defensive distillation





Training a network with explicit relative information about classes prevents models from fitting too tightly to the data.

Papernot, N., McDaniel, P., Wu, X., Jha, S., & Swami, A. (2016). Distillation as a defense to adversarial perturbations against deep neural networks. In Security and Privacy (SP), 2016 IEEE Symposium on (pp. 582-597). IEEE.