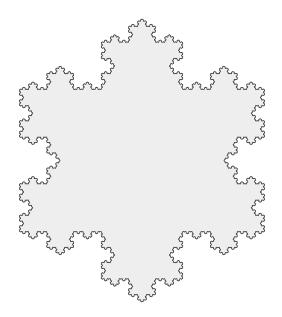
#### Fractal animation introduction

Grégory Châtel

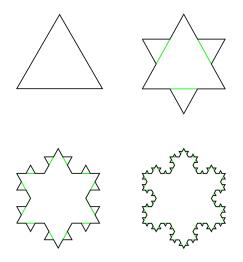
@rodgzilla github.com/rodgzilla

October 18th, 2018

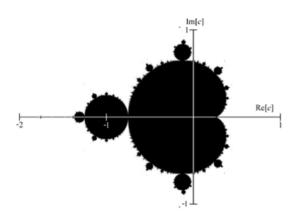
## What are fractals?



## Koch snowflake



# Pythagora's tree demo



Complex numbers and complex plane

$$c = ai + b$$
$$i^2 = -1$$

The modulus of a complex number is its euclidiean distance to 0:

$$c = ai + b$$
$$|c| = \sqrt{a^2 + b^2}$$

```
In [1]: c = complex(1, 2)
In [2]: c
Out[2]: (1+2j)
In [3]: c + complex(0,3)
Out[3]: (1+5j)
In [4]: c * c
Out[4]: (-3+4j)
```

#### Function to iterate

The formula that generates everything is the following one:

$$z_0 = c$$
$$z_{n+1} = z_n^2 + c$$

For each pixel (x, y) of the screen, we compute the corresponding complex number  $c_{x,y}$ .

Now we compute a fixed number of terms of the sequence above starting with  $z_0 = c_{x,y}$ .

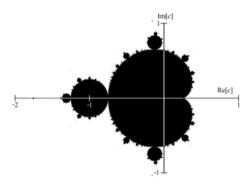
$$z_0 = c_{x,y}$$
  
 $z_1 = c_{x,y}^2 + c_{x,y}$   
 $z_2 = z_1^2 + c_{x,y} = (c_{x,y}^2 + c_{x,y})^2 + c_{x,y}$   
...  
 $z_{100} = z_{99}^2 + c_{x,y}$ 

In Python:

 $mandelbrot_function = lambda z, c: z ** 2 + c$ 

From the formula to the drawing

While we are iterating the formula for a pixel (x, y), if we find a step i for which  $|z_i| > 2$  then we draw the (x, y) pixel white, otherwise we draw it black.



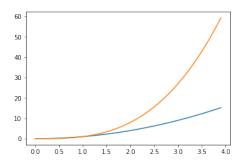
Source code

```
def draw_mandelbrot(f, max_iter, width, height):
    for y in range (height):
        for x in range(width):
            real = 3 * x / width - 2
            imag = 2 * y / height - 1
            c = complex(real, imag)
            z = c
            for i in range(max_iter):
                z = f(z, c)
                if z.real ** 2 + z.imag ** 2 > 4:
                     pixel(x, y, 'white')
                    break
            else:
                pixel(x, y, 'black')
```

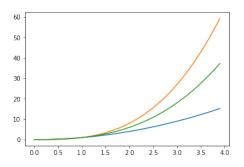
## Mandelbrot set zoom animation

## Function interpolation with Python

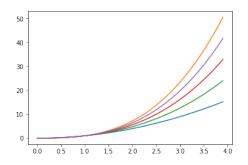
```
f_square = lambda x: x ** 2
f_cube = lambda x: x ** 3
```



### Function interpolation with Python



### Function interpolation with Python



## Mandelbrot set formula animations