

Computer Architecture
Spring 2019
Homework No. 4
(Due on May 8)

1.

| Iteration | Step | Multiplicand | Product |
|-----------|--|--------------|-----------|
| 0 | Initial | 0110 | 0000 1011 |
| 1 | Add multiplicand at front 4 bit (Last bit : 1) | 0110 | 0110 1011 |
| 1 | Shift right | 0110 | 0011 0101 |
| 2 | Add multiplicand at front 4 bit (Last bit : 1) | 0110 | 1001 0101 |
| 2 | Shift right | 0110 | 0100 1010 |
| 3 | Add nothing (Last bit : 0) | 0110 | 0100 1010 |
| 3 | Shift right | 0110 | 0010 0101 |
| 4 | Add multiplicand at front 4 bit (Last bit : 1) | 0110 | 1000 0101 |
| 4 | Shift right | 0110 | 0100 0010 |

2.

| Iteration | Step | Divisor | Remainder |
|-----------|---|---------|-----------|
| 0 | Initial | 0110 | 0000 1101 |
| 1 | Shift left | 0110 | 0001 101- |
| 1 | Subtract divisor | 0110 | 1011 101- |
| 1 | Negative: restore the front 4 bit, set last bit = 0 | 0110 | 0001 1010 |
| 2 | Shift left | 0110 | 0011 010- |
| 2 | Subtract divisor | 0110 | 1101 010- |
| 2 | Negative: restore the front 4 bit, set last bit = 0 | 0110 | 0011 0100 |
| 3 | Shift left | 0110 | 0110 100- |
| 3 | Subtract divisor | 0110 | 0000 100- |
| 3 | Positive: do nothing, set last bit = 1 | 0110 | 0000 1001 |
| 4 | Shift left | 0110 | 0001 001- |
| 4 | Subtract divisor | 0110 | 1011 001- |
| 4 | Negative: restore the front 4 bit, set last bit = 0 | 0110 | 0001 0010 |

Remainder: 0001

Quotient: 0010

3.

| Iteration | Step | Divisor | Remainder |
|-----------|----------------------------|---------|-----------|
| 0 | Initialize | 0110 | 0000 1101 |
| 1 | Positive value, shift left | 0110 | 0001 101- |
| 1 | Positive: subtract divisor | 0110 | 1011 101- |
| 1 | Negative: Last bit = 0 | 0110 | 1011 1010 |
| 2 | Negative value, shift left | 0110 | 0111 010- |
| 2 | Negative: Add divisor | 0110 | 1101 010- |
| 2 | Negative: Last bit = 0 | 0110 | 1101 0100 |
| 3 | Negative value, shift left | 0110 | 1010 100- |
| 3 | Negative: Add divisor | 0110 | 0000 100- |
| 3 | Positive: Last bit = 1 | 0110 | 0000 1001 |
| 4 | Positive value, shift left | 0110 | 0001 001- |
| 4 | Positive: subtract divisor | 0110 | 1011 001- |
| 4 | Negative: Set last bit = 0 | 0110 | 1011 0010 |
| 4 | Finally, Add Divisor | 0110 | 0001 0010 |

Remainder: 0001

Quotient: 0010

4.

Rewriting C3F00000 as binary, it is 1 10000111 1110000000000000000000. Therefore,

$$-1 * 2^8 * 1.111_2 = -(111100000)_2 = -(32 + 64 + 128 + 256) = -480$$