

# Recurrent Neural Network and LSTMs

Neural Network Design Seminar  
Presentation

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# Why Recurrent Neural Network?

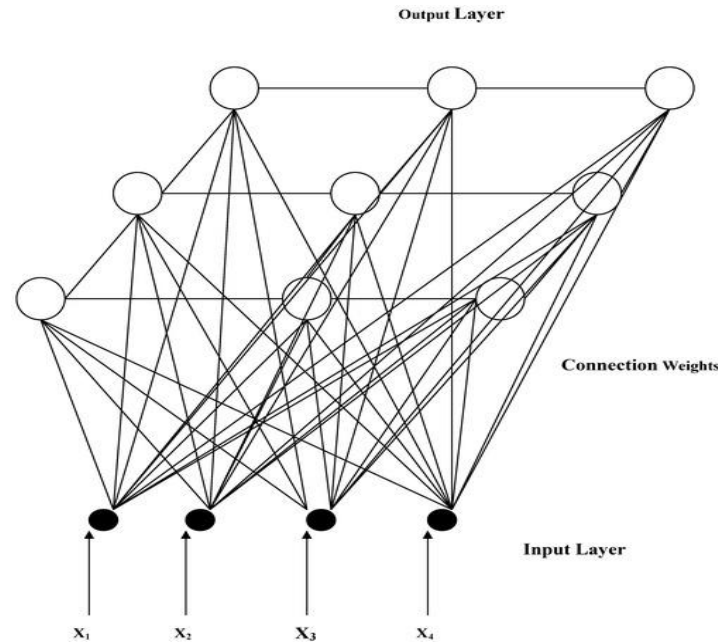
- In feed-forward networks, data is assumed to be independent.
- Many kind of data in the real world are not independent of each other and are like an interconnected chain.
- Feed-forward networks are not suitable for sequential data where each data's current value depends on previous data.
- Data such as stock indexes, the letters of the alphabet in words, and the words themselves in the larger set that make up sentences, audio data, frames of a video, and so on.



99 Sur la base de la grande statue de Zeus, à Olympie, Phidias avait représenté les Douze Dieux. Entre le Soleil (Hélios) et la Lune (Séléné) les douze divinités, groupées deux à deux, s'ordonnaient en six couples : un dieu-une déesse. Au centre de la frise, en surmonture, les deux divinités (féminine et masculine) qui président aux unions : Aphrodite et Éros<sup>99</sup>. Dans cette série de huit couples divins, il en est un qui fait problème : Hermès-Hestia. Pourquoi les appairer ? Rien dans leur généalogie ni dans leur légende qui puisse justifier cette association. Ils ne sont pas mari et femme (comme Zeus-Héra, Poséidon-Amphitrite, Héphestos-Charis), ni frère et sœur (comme Apollon-Artémis, Hélios-Séléné), ni père et fils (comme Aphrodite-Éros), ni protectrice et protégé (comme Athéna-tétrarches). Quel lien unissait donc, dans l'esprit de Phidias, un dieu et une déesse qui semblent étrangers l'un à l'autre ? On ne saurait alléguer une fantaisie personnelle du sculpteur. Quand il exécute une œuvre sacrée, l'artiste ancien est tenu de se conformer à certains modèles : son initiative s'exerce dans le cadre des schémas imposés par la tradition. Hestia – nom propre d'une déesse mais aussi nom commun désignant le foyer – se prêtait moins que les autres dieux grecs à la représentation anthropomorphe. On la voit rarement figurée. Quand elle l'est, c'est souvent, comme Phidias l'avait sculptée, faisant couple avec Hermès<sup>1</sup>. De règle dans l'art plastique, l'association Hermès-Hestia

# History of Recurrent Neural Networks

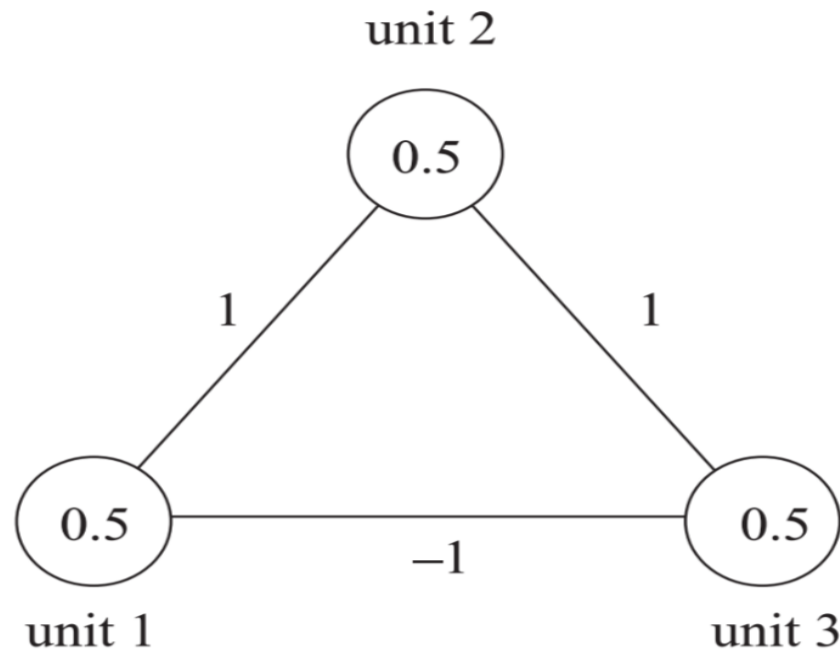
- + The first recurrent neural network was introduced in 1977 as the fully recurrent neural network by Anderson and Cohen.



(Yuan et al., 2009)

# History of Recurrent Neural Networks

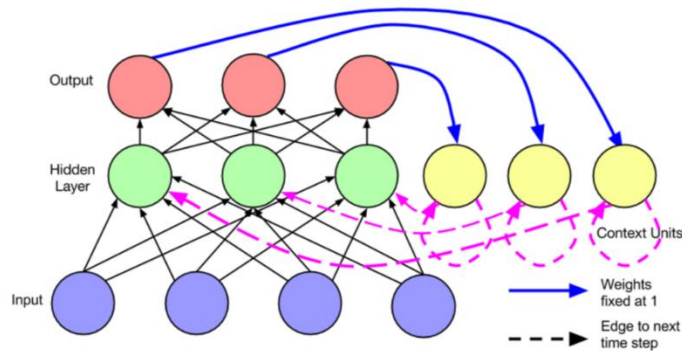
+ In 1982, the Hopfield network was introduced by John Hopfield.



(Rojas, 1996)

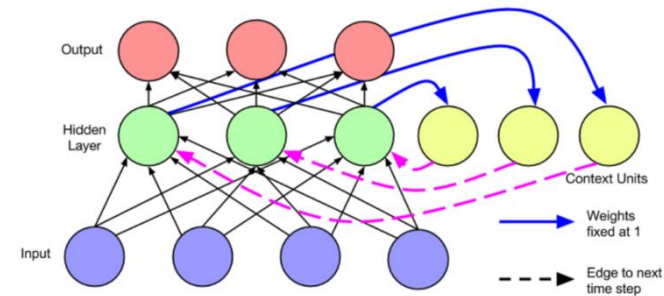
# History of Recurrent Neural Networks

- + Michael Jordan invented the Jordan Network in 1986. Like other networks, it was a feed network that had a hidden layer and a special layer called the state unit.



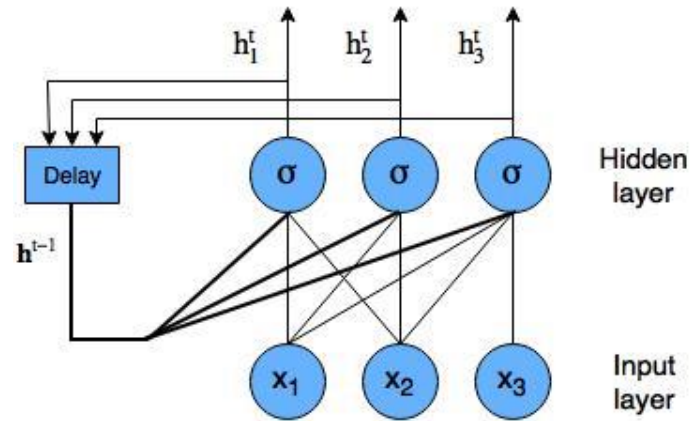
Jordan's network, with recurrent edges of output neurons

- + The architecture proposed by Elman in 1990 was simpler than Jordan's original architecture. Corresponding to each neuron in the hidden layer there is a context unit.

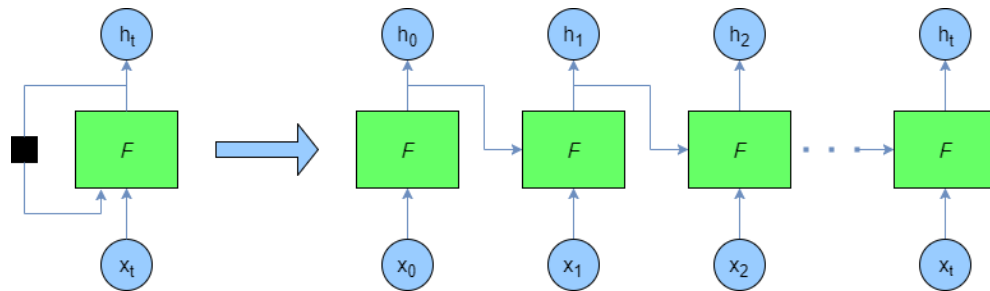


Elman Network , with recurrent edges of context layer's neurons

# Vanilla Recurrent Neural Network Mechanism and Architecture



Vanilla recurrent neural network with three input neurons



An unrolled recurrent neural network

$$z_t = w^{xh}x_{t-1} + w^{hh}h_{t-1} + b_h$$

Hidden layer output :  $h_t = \tanh(z_t)$

$$y_t = w^{hy}h_t + b_y$$

Expected output :  $p_t = \text{softmax}(y_i)$

$$\hat{y}_k = \frac{e^{a_k}}{\sum_{k'=1}^K e^{a_{k'}}} \text{ for } k = 1 \text{ to } k = K.$$



# Backpropagation Through the Time (BPT)

loss function (cross entropy)

$$C = - \sum_p^n \sum_k^o d_{pk} \ln y_{pk} + (1 - d_{pk}) \ln(1 - y_{pk})$$

calculate the amount of error with respect to the weight of the hidden layer to the hidden layer

$$\frac{\partial J_t}{\partial \mathbf{W}^{hh}} = \sum_{k=0}^t \frac{\partial J_t}{\partial \mathbf{h}_t} \frac{\partial \mathbf{h}_t}{\partial \mathbf{h}_k} \frac{\partial \mathbf{h}_k}{\partial \mathbf{z}_k} \frac{\partial \mathbf{z}_k}{\partial \mathbf{W}^{hh}}$$

Cost function

$$\mathbf{J}_t = \text{crossentropy}(\mathbf{p}_t, \text{labels}_t)$$

Output error respect to current time step

$$\delta_o = - \frac{\partial J_t}{\partial p_t} \frac{\partial p_t}{\partial y_t}$$

Calculate the amount of error with respect to the weight of the input neuron to the hidden layer neuron

$$\frac{\partial J_t}{\partial \mathbf{W}^{xh}} = \sum_{k=0}^t \frac{\partial J_t}{\partial \mathbf{h}_t} \frac{\partial \mathbf{h}_t}{\partial \mathbf{h}_k} \frac{\partial \mathbf{h}_k}{\partial \mathbf{z}_k} \frac{\partial \mathbf{z}_k}{\partial \mathbf{W}^{xh}}$$

hidden state error in the current time step

$$\delta_h = - \sum \frac{\partial J_t}{\partial p_t} \frac{\partial p_t}{\partial y_t} \frac{\partial y_t}{\partial h_t} \frac{\partial h_t}{\partial z_t}$$

calculate hidden state error in one backward step

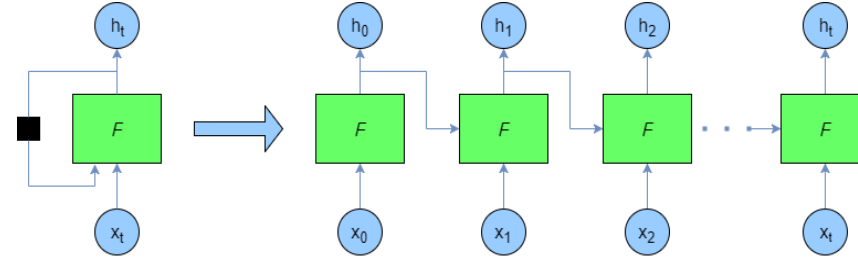
$$\delta_h(t-1) = - \sum \delta_h(t) * w_t^{hh} * \hat{f}'(h(t-1))$$

Calculate the amount of error with respect to the weight of the hidden layer to the output

$$\frac{\partial J_t}{\partial \mathbf{w}^{hy}} = \sum \frac{\partial J_t}{\partial p_t} \frac{\partial p_t}{\partial y_t} \frac{\partial y_t}{\partial \mathbf{w}^{hy}}$$

# Example of calculating the error changes in the third time step relative to the model parameters

$$\frac{\partial J_3}{\partial W^{hy}} = \frac{\partial J_3}{\partial p_3} \frac{\partial p_3}{\partial y_3} \frac{\partial y_3}{\partial W^{hy}}$$



$$\begin{aligned} \frac{\partial J_3}{\partial W^{hh}} &= \frac{\partial J_3}{\partial p_3} \frac{\partial p_3}{\partial y_3} \frac{\partial y_3}{\partial h_3} \frac{\partial h_3}{\partial z_3} \frac{\partial z_3}{\partial W^{hh}} \\ &+ \frac{\partial J_3}{\partial p_3} \frac{\partial p_3}{\partial y_3} \frac{\partial y_3}{\partial h_3} \frac{\partial h_3}{\partial z_3} \frac{\partial h_2}{\partial z_2} \frac{\partial z_2}{\partial W^{hh}} \\ &+ \frac{\partial J_3}{\partial p_3} \frac{\partial p_3}{\partial y_3} \frac{\partial y_3}{\partial h_3} \frac{\partial h_3}{\partial z_3} \frac{\partial h_2}{\partial z_2} \frac{\partial z_2}{\partial h_1} \frac{\partial h_1}{\partial z_1} \frac{\partial z_1}{\partial W^{hh}} \end{aligned}$$

$$\begin{aligned} \frac{\partial J_2}{\partial W^{hh}} &= \frac{\partial J_2}{\partial p_2} \frac{\partial p_2}{\partial y_2} \frac{\partial y_2}{\partial h_2} \frac{\partial h_2}{\partial z_2} \frac{\partial z_2}{\partial W^{hh}} \\ &+ \frac{\partial J_2}{\partial p_2} \frac{\partial p_2}{\partial y_2} \frac{\partial y_2}{\partial h_2} \frac{\partial h_2}{\partial z_2} \frac{\partial h_1}{\partial z_1} \frac{\partial z_1}{\partial W^{hh}} \end{aligned}$$

$$\frac{\partial J_1}{\partial W^{hh}} = \frac{\partial J_1}{\partial p_1} \frac{\partial p_1}{\partial y_1} \frac{\partial y_1}{\partial h_1} \frac{\partial h_1}{\partial z_1} \frac{\partial z_1}{\partial W^{hh}}$$

$$\begin{aligned} \frac{\partial J_3}{\partial W^{xh}} &= \frac{\partial J_3}{\partial p_3} \frac{\partial p_3}{\partial y_3} \frac{\partial y_3}{\partial h_3} \frac{\partial h_3}{\partial z_3} \frac{\partial z_3}{\partial W^{xh}} \\ &+ \frac{\partial J_3}{\partial p_3} \frac{\partial p_3}{\partial y_3} \frac{\partial y_3}{\partial h_3} \frac{\partial h_3}{\partial z_3} \frac{\partial h_2}{\partial z_2} \frac{\partial z_2}{\partial W^{xh}} \\ &+ \frac{\partial J_3}{\partial p_3} \frac{\partial p_3}{\partial y_3} \frac{\partial y_3}{\partial h_3} \frac{\partial h_3}{\partial z_3} \frac{\partial h_2}{\partial z_2} \frac{\partial z_2}{\partial h_1} \frac{\partial h_1}{\partial z_1} \frac{\partial z_1}{\partial W^{xh}} \end{aligned}$$

$$\begin{aligned} \frac{\partial J_2}{\partial W^{xh}} &= \frac{\partial J_2}{\partial p_2} \frac{\partial p_2}{\partial y_2} \frac{\partial y_2}{\partial h_2} \frac{\partial h_2}{\partial z_2} \frac{\partial z_2}{\partial W^{xh}} \\ &+ \frac{\partial J_2}{\partial p_2} \frac{\partial p_2}{\partial y_2} \frac{\partial y_2}{\partial h_2} \frac{\partial h_2}{\partial z_2} \frac{\partial h_1}{\partial z_1} \frac{\partial z_1}{\partial W^{xh}} \end{aligned}$$

$$\frac{\partial J_1}{\partial W^{xh}} = \frac{\partial J_1}{\partial p_1} \frac{\partial p_1}{\partial y_1} \frac{\partial y_1}{\partial h_1} \frac{\partial h_1}{\partial z_1} \frac{\partial z_1}{\partial W^{xh}}$$

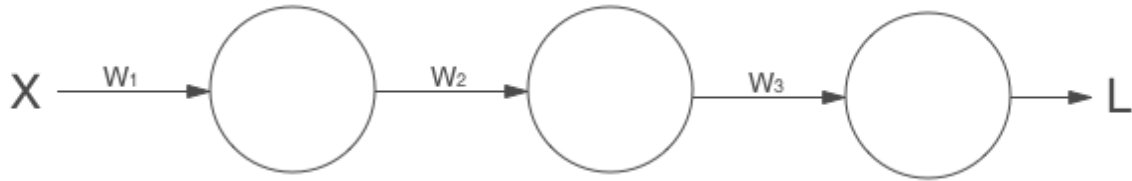


# Steps of vanilla recurrent neural network training

1. For each training sequence  $X = (x_1, x_2, \dots, x_k)$  where  $x_1$  and  $x_k$  are the sequences' symbol for the start and end, respectively. Do the second step to the last step.
2. Set the value of the latent neuron activators to 0.5 and the value of the latent state of the previous step for the input of the first time step ( $x_1$ ) to zero ( $h_0 = 0$ )
3. Follow step 4 to the last step to reach the end of the sequence
4. Apply the vector  $x_i$  to the network and present the vector  $x_{i+1}$  as the target response to the output units.
5. Calculate the activation value of latent and output neurons
6. Calculate the cost function in terms of network output and actual output.
7. Calculate the BPT
8. Update network weights
9. Check the stop condition (reaching the desired error threshold or ending Epochs)

(Werbos, 1990, Pascanu et al., 2013)

# The problem of gradient vanishing and gradient explosion



If we take the weight between zero and one, then consecutive multiplying will make it insignificant, and this will reduce the effects of the primary layers of the network and make network training difficult. The same can be said from the opposite point of view; if we chose weights with values greater than one, consecutive multiplying would greatly increase the cost function.

$$\frac{\partial Loss}{\partial W_3} = \frac{\partial Loss}{\partial f(z_3)} \cdot \frac{\partial f(z_3)}{\partial W_3} = \frac{\partial Loss}{\partial f(z_3)} \cdot f'(z_3) \cdot W_3$$

$$\begin{aligned} \frac{\partial Loss}{\partial W_1} &= \frac{\partial Loss}{\partial f(z_3)} \cdot \frac{\partial f(z_3)}{\partial f(z_2)} \cdot \frac{\partial f(z_2)}{\partial f(z_1)} \cdot \frac{\partial f(z_1)}{\partial W_1} \\ &= \frac{\partial Loss}{\partial f(z_3)} \cdot f'(z_3) \cdot W_3 \cdot f'(z_2) \cdot W_2 \cdot f'(z_1) \cdot W_1 \end{aligned}$$

# What are solutions???

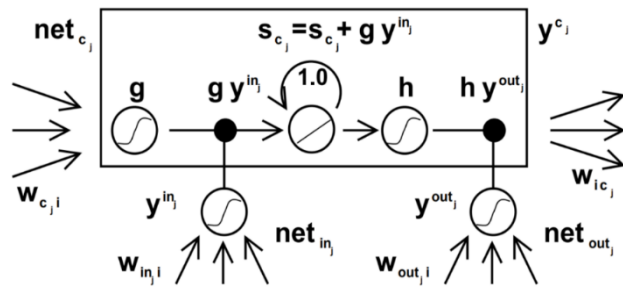
## Gradian Vanishing

- Using RELU activator
- Using metaheuristic methods
- LSTMs

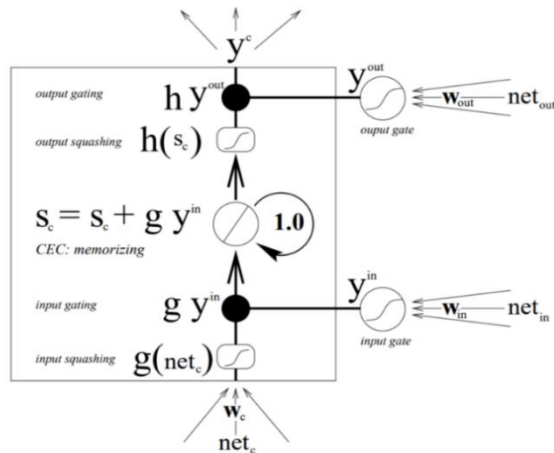
## Gradian Explosion

- Using RELU activator
- Cutting the gradian
- Liming the amount of sequences
- LSTMs

# Long Short Term Memory (LSTM)

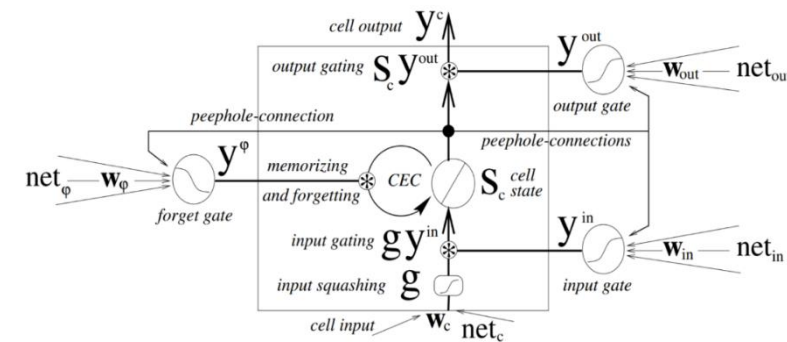


The first generation of LSTM networks (Hochreiter and Schmidhuber, 1997)



The second generation of LSTM networks (Gers et al., 1999)

- First Generation LSTM Networks (1995-1997): These networks had two input and output gates, as well as a recurrent edge, activation function, and an identity function.
- Second Generation LSTM Introduce forget gate (1999)
- Third Generation: Introducing Peephole Connection (2000)
- It has been going on since 2000 ...



Third Generation LSTM Networks (Gers and Schmidhuber, 2000)

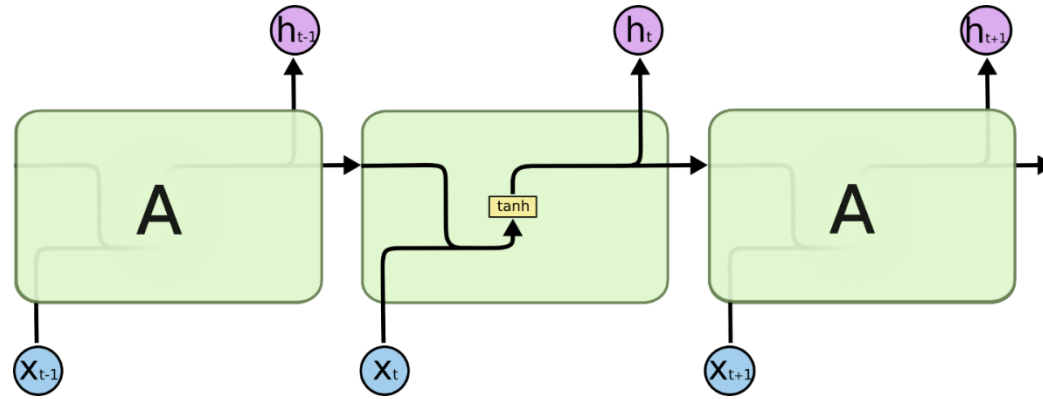
# Comparison of LSTM network performance with vanilla recurrent networks

Method	Delay $p$	Learning rate	# weights	% Successful trials	Success after
RTRL	4	1.0	36	78	1,043,000
RTRL	4	4.0	36	56	892,000
RTRL	4	10.0	36	22	254,000
RTRL	10	1.0-10.0	144	0	> 5,000,000
RTRL	100	1.0-10.0	10404	0	> 5,000,000
BPTT	100	1.0-10.0	10404	0	> 5,000,000
CH	100	1.0	10506	33	32,400
<b>LSTM</b>	<b>100</b>	<b>1.0</b>	<b>10504</b>	<b>100</b>	<b>5,040</b>

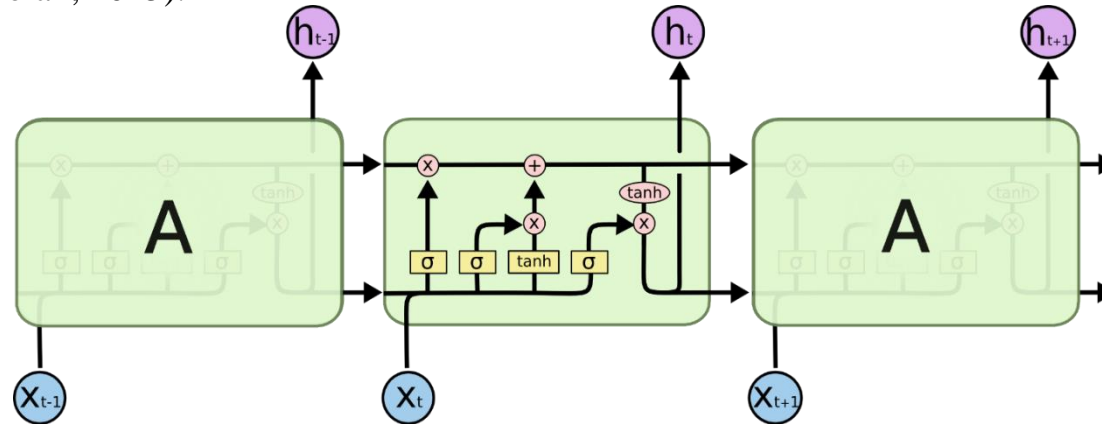
(Hochreiter and Schmidhuber, 1997)



# LSTM Networks' Mechanism



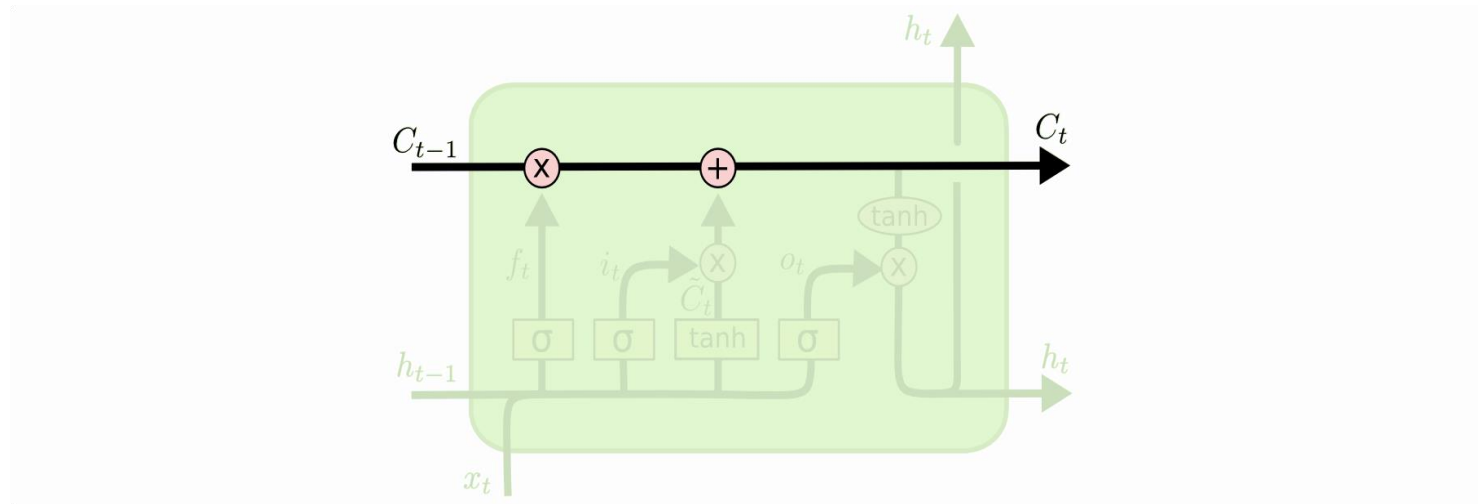
Repetitive modules in vanilla recursive neural networks have only one layer (colah, 2015).



“The repeating module in an LSTM contains four interacting layers” (colah, 2015)

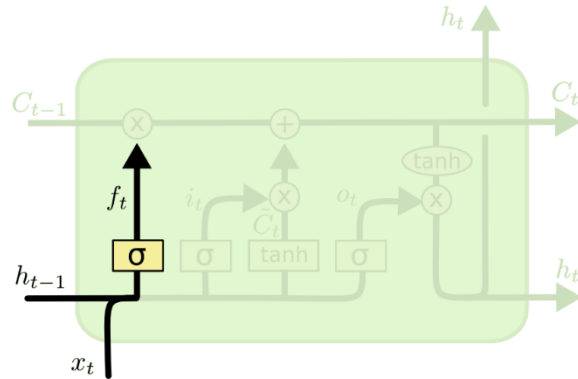
# LSTM Networks' Mechanism

The main element of LSTMs is the state cell, which is actually a horizontal line at the top of the shape. The state cell can be thought of as a conveyor belt that moves from the beginning to the end of a sequence or chain with partial linear interactions (its structure is very simple and little change occurs in it).



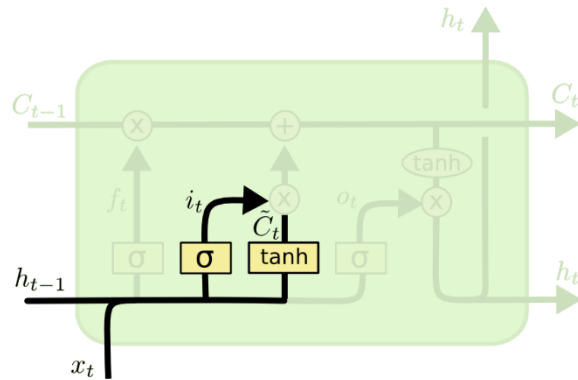
# LSTM Networks' Mechanism

The first step in LSTM is deciding on the information we want to clear from the state cell. This decision is made by a sigmoid layer called the forget gate.



$$f_t = \sigma(W_f \cdot [h_{t-1}, x_t] + b_f)$$

The next step is to decide what new information we want to store in the state cell.

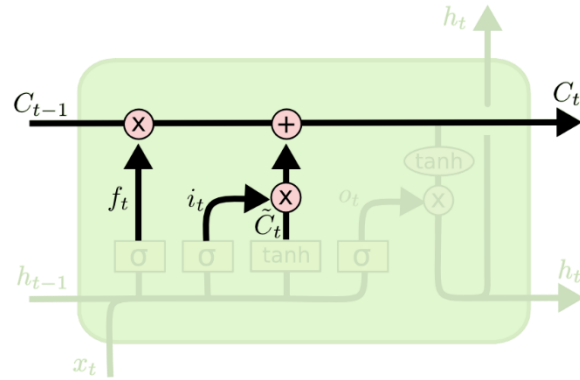


$$i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i)$$

$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

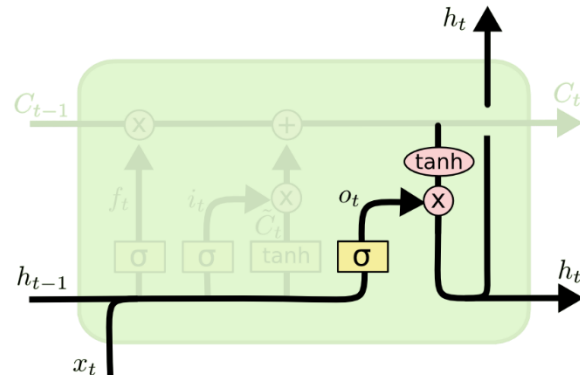
# LSTM Networks' Mechanism

Now it's time to update the old state cell,  $C_{t-1}$ , to the new state cell,  $C_t$ .



$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

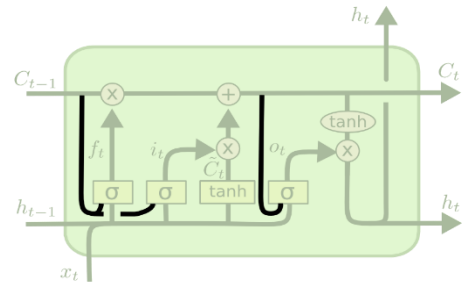
Finally, we have to decide what information we are going to output. This output will be in respect to the state cell's value but will pass through a certain filter.



$$o_t = \sigma(W_o [h_{t-1}, x_t] + b_o)$$

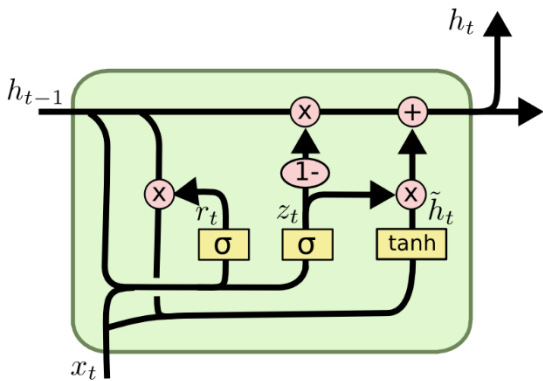
$$h_t = o_t * \tanh(C_t)$$

# Other LSTMs



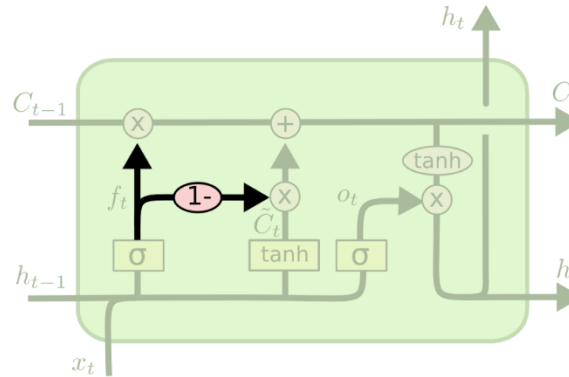
$$\begin{aligned} f_t &= \sigma(W_f \cdot [C_{t-1}, h_{t-1}, x_t] + b_f) \\ i_t &= \sigma(W_i \cdot [C_{t-1}, h_{t-1}, x_t] + b_i) \\ o_t &= \sigma(W_o \cdot [C_t, h_{t-1}, x_t] + b_o) \end{aligned}$$

Peephole



$$\begin{aligned} z_t &= \sigma(W_z \cdot [h_{t-1}, x_t]) \\ r_t &= \sigma(W_r \cdot [h_{t-1}, x_t]) \\ \tilde{h}_t &= \tanh(W \cdot [r_t * h_{t-1}, x_t]) \\ h_t &= (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t \end{aligned}$$

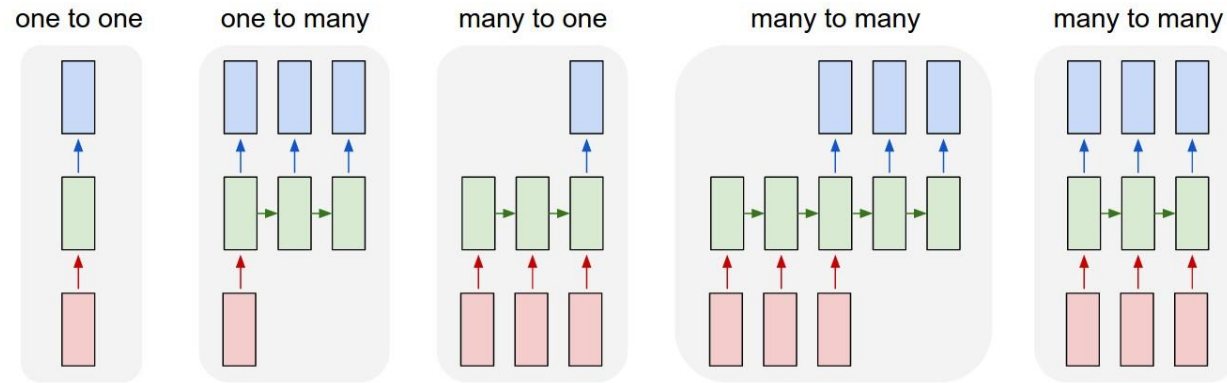
GRU-(Cho et al., 2014)



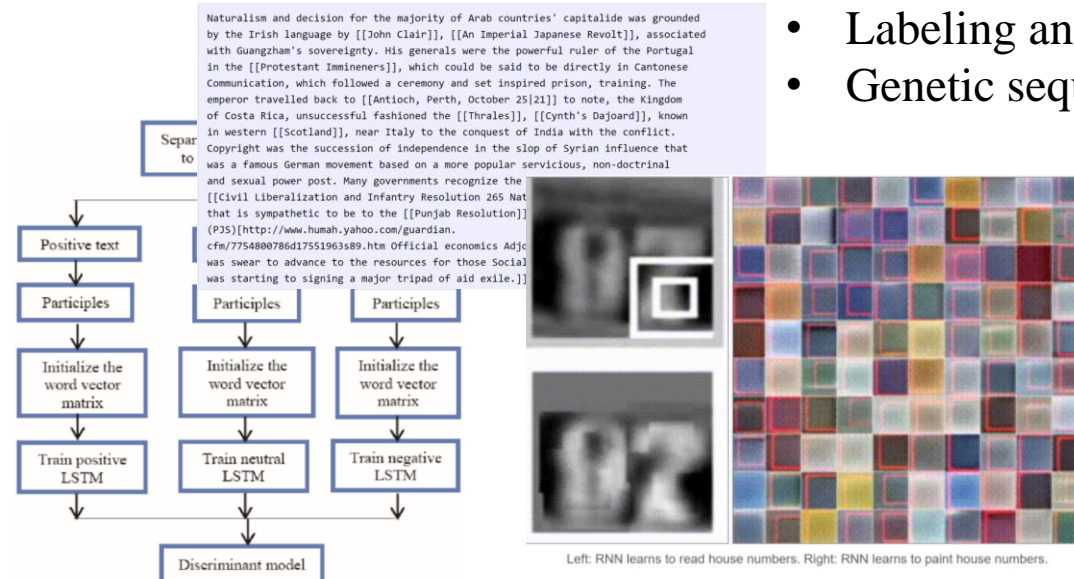
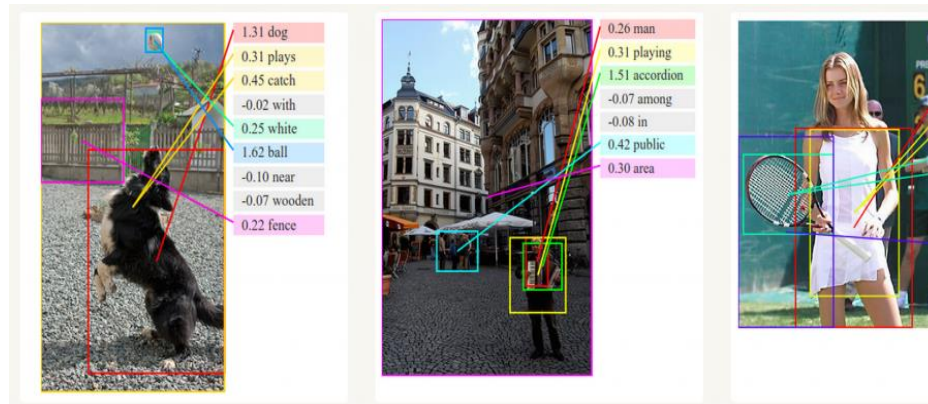
$$C_t = f_t * C_{t-1} + (1 - f_t) * \tilde{C}_t$$



# Architectures and Applications of Standard Recurrent Neural Network and LSTM



- Sequence generation like text or music
- Predict the trend of stock indices
- image captioning
- Translation machines
- Photo and video classification
- Convert speech to text
- Labeling and classification
- Genetic sequencing



(karpathy,2015.)

# Some Points About LSTM

- Compared to standard recurrent neural networks, these networks were highly capable of handling long sequences.
- One of the drawbacks of LSTM networks is the need for a lot of data and the high amount of computation that makes the learning process difficult. To solve these problems, scientists have made improvements to LSTM networks over time;
- There is no definite indication of the modified LSTM networks' superiority over the classical LSTM described above. Although LSTM networks have a slower learning process than modified LSTM networks, this is a drawback. The predictive power of LSTM networks will be higher if they have the right amount of data and provide the right time to the network.
- It is the most widely used network in people's daily lives. Virtual keyboards on smartphones that predict words and sentences for us, voice assistants Alexa, Cortana, Bixby, Siri, etc., classification of movies and content on social networks, etc., all of which are powered by recurrent neural networks, especially LSTMs.

# More Intuition

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Happy :)