

Practice Problem #2

Newton's Laws of Motion

Question: *An advertisement claims that a particular automobile can "stop on a dime". What net force would actually be necessary to stop a 850 kg automobile traveling initially at 45.0 km/hour in a distance equal to the diameter of a dime, which is 1.8 cm?*

Solution: First convert the speed of the automobile and the diameter of the dime to SI units:

$$45.0 \frac{\cancel{km}}{\cancel{h}} \cdot \frac{1,000 \cancel{m}}{1 \cancel{km}} \cdot \frac{1 \cancel{h}}{3,600 \cancel{s}} = 12.5 \frac{m}{s}$$

$$1.8 \cancel{cm} \cdot \frac{1 \cancel{m}}{100 \cancel{cm}} = 0.018 \cancel{m}$$

To solve for the net force, the net acceleration is needed first. This can be found using the following kinematic equation:

$$v_f^2 = v_i^2 + 2a\Delta x$$

Note that when the automobile comes to a stop, $v_f = 0$. Solving for a :

$$0 = v_i^2 + 2a\Delta x$$

$$-2a\Delta x = v_i^2$$

$$a = -\frac{v_i^2}{2\Delta x}$$

Applying Newton's 2nd Law:

$$\sum F = ma_{net}$$

$$= m\left(-\frac{v_i^2}{2\Delta x}\right)$$

$$= (850 \cancel{kg})\left(-\frac{(12.5 \frac{\cancel{m}}{\cancel{s}})^2}{2(0.018 \cancel{m})}\right)$$

$$\approx \boxed{-3.7 \cdot 10^6 \cancel{N}}$$

The magnitude of this force is $\approx 1/3$ the thrust of a Space Shuttle rocket booster at liftoff. It is *incredibly* unlikely that an automobile would have this capability.