Springboard **Graphs** Springboard Graphs Download Demo Code « Back to Homepage Goals • Learn what a graph is • Compare and contrast different types of graphs What is a Graph? • Code a graph implementation Terminology • Check if two nodes are connected Examples What is a Graph? Food Chain Facebook Friends (or LinkedIn) Processes Luke **Markov Chains** Airline Route Map Carpooling Leia Graphs Linked Lists, Trees, and Graphs Darth\_Vader Han Representing a Graph Representing a Graph - Adjacency Lists Palpatine Lando Representing a Graph - Adjacency Graphs are like trees, except they can contain loops ("cycles"). We're going to use Adjacency Lists! Friend Graph Also, the relationships can be directed or un-directed. Node and Graph Class **Terminology** Demo: **friends.js Graph Traversal Node (or Vertex)** Problem: basic unit Is Marge connected to Grampa? Edge (or Arc) Is Marge connected to Moe? connects two nodes How do we figure this out? **Adjacent** Not like your tree traversal two nodes are "adjacent" if they share an edge Graph Breadth First Search Weight (optional) Solution each edge can have a weight (ex: price, or distance) Graph Depth First Search Another Iterative Approach **Recursive Solution Examples Further Study Food Chain** Further Study Sperm Whales Penguins Baleen Whales This graph is **directed**, showing "what eats what" Penguins' adjacency list: [Squid, Krill] **Facebook Friends (or LinkedIn)** Krusty\_The\_Clown This graph is undirected Homer's adjacency list: [Bart, Lisa, Maggie, Marge] Lisa's adjacency list: [Maggie, Bart, Homer] **Processes** Making Cupcakes: add\_sugar cupcake\_mix take\_out\_of\_oven Don't want to do a step until the necessary prerequisites are done! Similar idea for manufacturing processes, supply chains, etc. **Markov Chains** could you like them, like green with a Other Markov chains: states of health and disease, finance **Airline Route Map** Each node is an airport. Each edge is a flight. The weight of each edge is the price. What is the cheapest way to go from New York to San Francisco? Carpooling Each node is a rider, and edges represent possible carpooling matches. Only two people can carpool together at a time. How can we match the maximum number of pairs of riders? There exists a solution where everyone gets a pair. Can you find it? **Graphs** • Graphs are often used to model relationships between things • Trees are directed, acyclic graphs • All trees are graphs, but not all graphs are trees • Trees have hierarchy, graphs do not **Linked Lists, Trees, and Graphs** Linked lists, trees, and graphs are all structures that have a relationship, much like squares, rectangles, and parallelograms do. A linked list is a special, more-restricted form of a tree, and a tree is a special, more-restricted form of a graph. **Linked List** Nodes have 0 or 1 child; acyclic and directed Tree Nodes have 0+ children; acyclic and directed; only one designated root node **Graphs** Nodes have 0+ connections; cyclic or acyclic; directed or undirected; disconnected or connected; optional weights There are other possibilities, including: • there are "circular linked lists," where the linked list can contain a cycle (A points to B points to C which points to B). These do not have tails, as there's no single end-point. • there are "forests," which are collections of directed, acyclic graphs but without a single root node. This essentially is a set of trees, hence a "forest." Code **Representing a Graph Adjacency List** for node, a list of every node it is directly connected to **Adjacency Matrix** a matrix of every pair of nodes, with a 1 if that pair is connected (otherwise 0) **Representing a Graph - Adjacency Lists** E: ["D", "F"], **Representing a Graph - Adjacency Matrix** We're going to use Adjacency Lists! They're more common. Adjacency matrices can be preferred for graphs that are highly connected. **Friend Graph Node and Graph Class** demo/friends.js class PersonNode { constructor(name, adjacent = new Set()) { // Create a person node with friends adjacent this.name = name; this.adjacent = adjacent; demo/friends.js class FriendGraph { // Graph holding people and their friendships. constructor() { this.nodes = new Set(); addPerson(person) { // Add a person to our graph this.nodes.add(person); setFriends(person1, person2) { // Set two people as friends person1.adjacent.add(person2); person2.adjacent.add(person1); addPeople(people\_list) { // Add a list of people to our graph for (let person of people\_list) { this.addPerson(person); Demo: friends.js demo/friends.js let homer = new PersonNode("Homer"); let marge = new PersonNode("Marge"); Marge let maggie = new PersonNode("Maggie"); let lisa = new PersonNode("Lisa"); let grampa = new PersonNode("Grampa"); Maggie let friends = new FriendGraph(); friends.addPeople([homer, marge, maggie, lisa, grampa]); friends.setFriends(homer, marge); friends.setFriends(homer, maggie); Grampa friends.setFriends(homer, lisa); friends.setFriends(marge, maggie); friends.setFriends(lisa, grampa); **Graph Traversal Problem:** Write a function that checks if two people are connected. **Is Marge connected to Grampa?** Marge Grampa Is Marge connected to Moe? Marge Barney Lenny Maggie Grampa How do we figure this out? • We need to traverse through the graph • We want to make sure we only visit each vertex once • But how do we search through it? • BFS - go to all closest neighbors and work your way outwards • DFS - continue on a path until it's exhausted Not like your tree traversal • This one is a bit different! • Since graphs can have cycles, we need to be sure not visit same node again! • How can we mark a node as visited? **Graph Breadth First Search Solution** demo/friends.js areConnectedBFS(person1, person2) { let toVisitQueue = [person1]; let seen = new Set(toVisitQueue); while (toVisitQueue.length > 0) { let currPerson = toVisitQueue.shift(); if (currPerson === person2) return true for (let neighbor of currPerson.adjacent) { if (!seen.has(neighbor)) { toVisitQueue.push(neighbor); seen.add(neighbor); return false; This is a breadth-first search (would be depth-first if we used a stack) **Graph Depth First Search Another Iterative Approach** demo/friends.js areConnectedDFS(person1, person2) { let toVisitStack = [person1]; let seen = new Set(toVisitStack); while (toVisitStack.length > 0) { let currPerson = toVisitStack.pop(); if (currPerson === person2) return true; for (let neighbor of currPerson.adjacent) { if (!seen.has(neighbor)) { toVisitStack.push(neighbor); seen.add(neighbor); return false; **Recursive Solution** demo/friends.js areConnectedRecursive(person1, person2, seen=new Set([person1])) { if (person1 === person2) return true; for (let neighbor of person1.adjacent) { if (!seen.has(neighbor)) { seen.add(neighbor); if (this.areConnectedRecursive(neighbor, person2, seen)) { return true; return false; This is a recursive depth-first search **Further Study Gentle Introduction to Graph Theory BFS Graph Traversal** From Theory to Practice: Representing Graphs • Visualizations: Visualgo.net • Problem Solving with Algorithms and Data Structures (awesome FREE book!) • Graph Database: Neo4j • Joe Celko, SQL for Smarties (graphs and trees in SQL)

Goals

Code

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