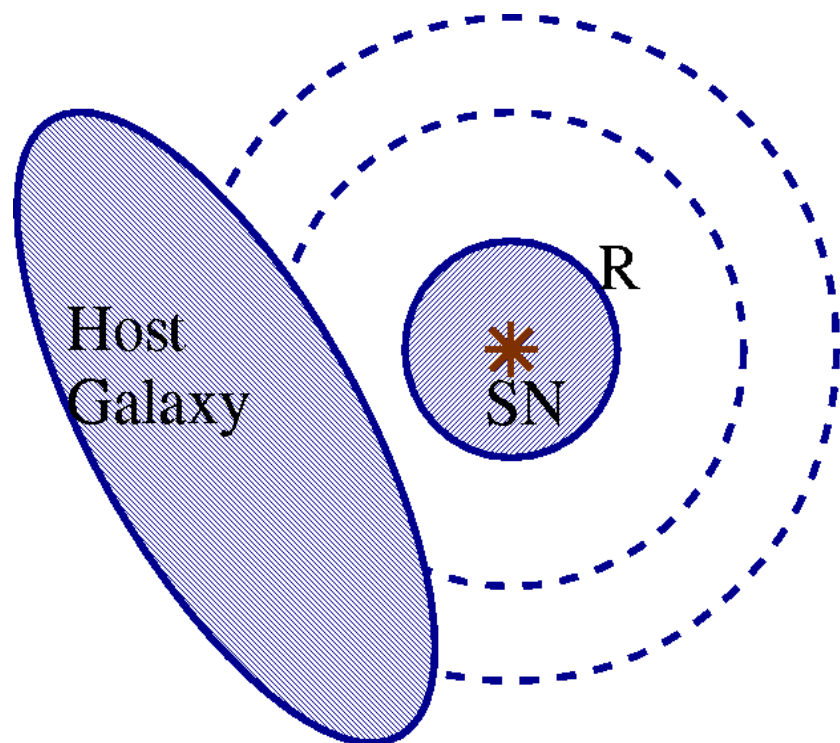


# Why do PSF-fitting



The simple aperture photometry has an assumption of *linearly-varying background* in the aperture's vicinity.

- Choice of (optimal) aperture size

$$S/N = C / \sqrt{\sigma_C^2 + \sigma_{noise}^2} = C / \sqrt{C + \pi * R^2 * RN^2}$$

Especially relevant for low S/N cases.

- If do not know PSF very well – may want to make larger-than optimal. More on this later.
- Varying background can represent a problem. Crowded fields!

Things to be cautious about:  
low S/N,  
varying background.

# Crowded field example



Even when nominally well separated, bright stars can shadow faint neighbours.

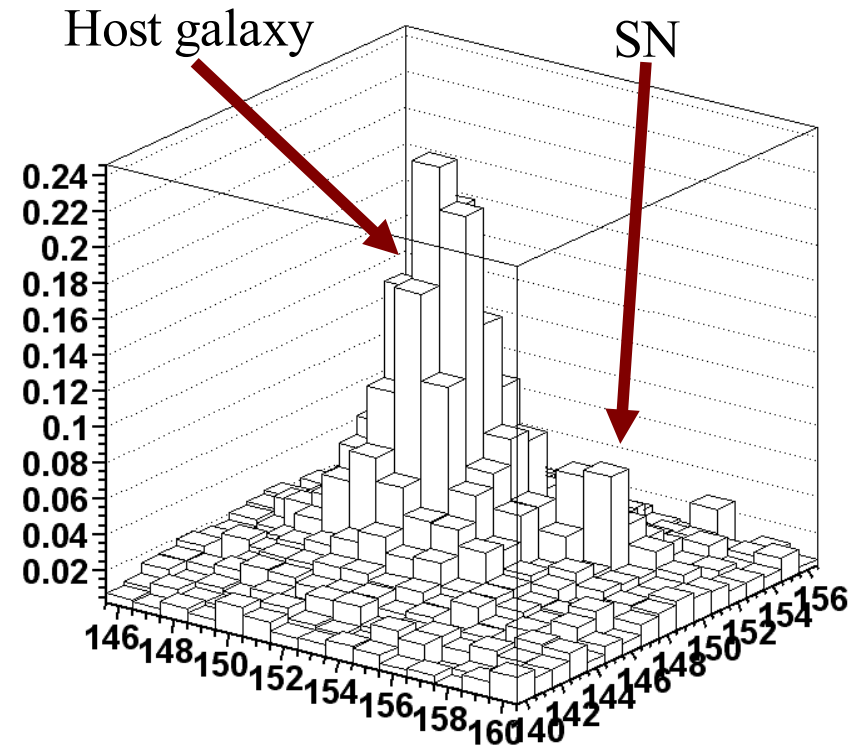
Starburst Region NGC 3603 (VLT ANTU + ISAAC)

ESO PR Photo 38a/99 (13 October 1999)

© European Southern Observatory



# PSF-fitting formalism



**What if know PSF well?**

**Then can use this information to do better in a number of aspects.**

**Can minimize**

$$\chi^2 = \sum (Bkg_i + C * PSF_i - Pix_i)^2 / \sigma_i^2$$

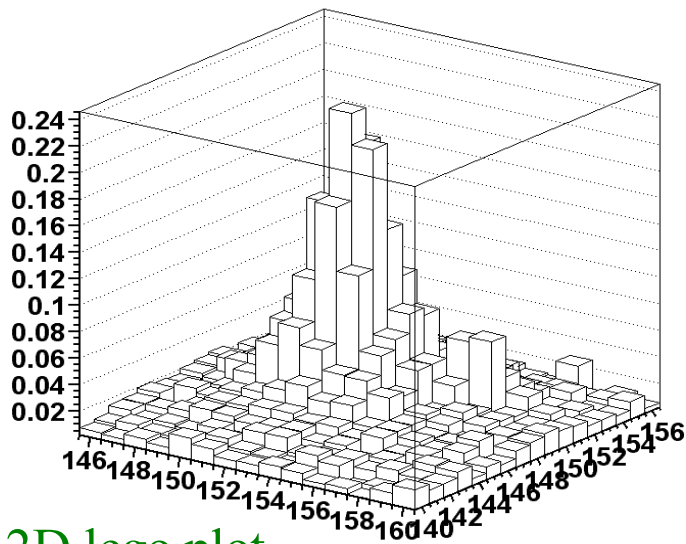
**in the star neighbourhood (image patch) to find the SN counts  $C$ , position and (maybe) the background parameters.**

**Pixelated image as 2D histogram.**

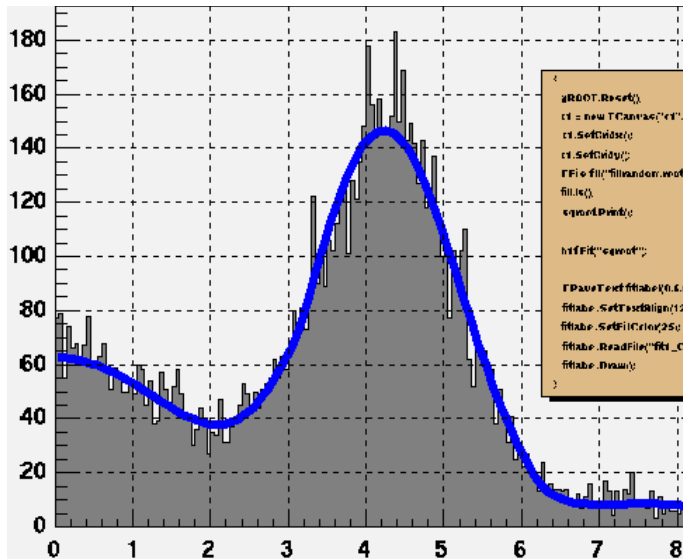
**“Just a 2D fit”.**

Things to be cautious about:  
inter-pixel correlations due to diffusion,  
intra-pixel efficiency variation (undersampled case).

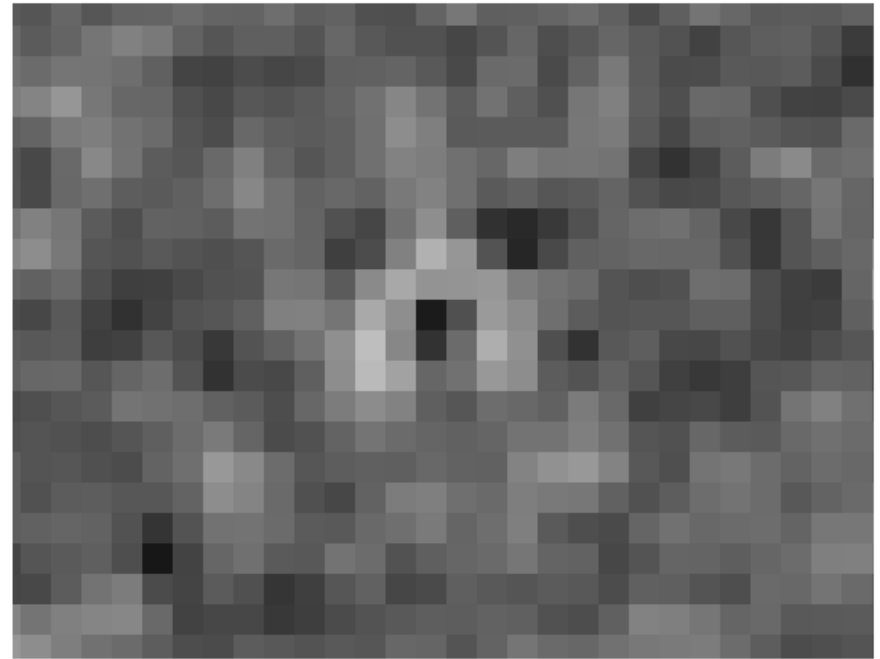
## Examining 2D fit results



2D lego plot



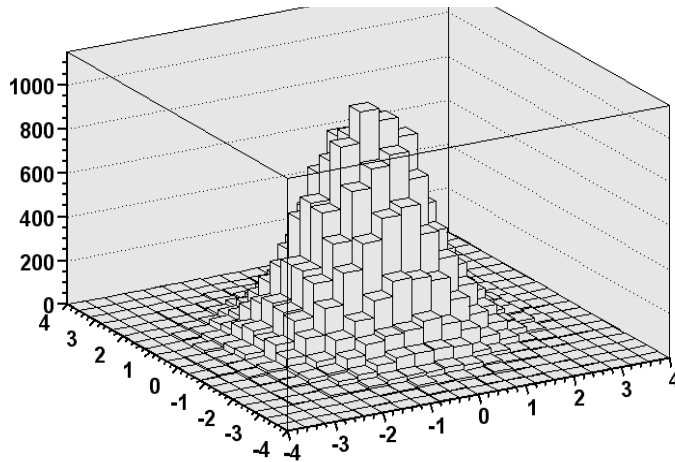
1D fit with function superimposed



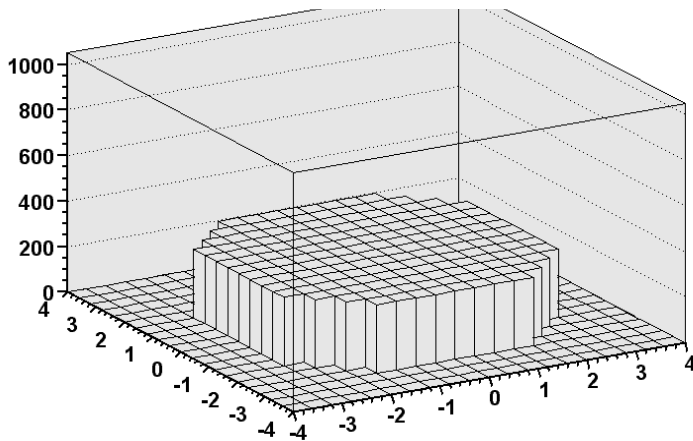
2D fit residuals (doughnut pattern)

**Detailed visualization of the 2D data and the fit function comparison is difficult. Resort to examining residuals, to see if the data subtract well.**

# PSF-fitting advantages



2D Gaussian weight function



Aperture photometry weight function

**Can be used in crowded fields – multiple PSF models for multiple overlapping stars.**

**Can be used in case of SN+galaxy if the galaxy model is known (no subtraction!).**

**Optimal weighting:  
suppose (for simplicity) that Bkg = 0, then**

$$C = \frac{\sum Pix_i * PSF_i / \sigma_i^2}{\sum PSF_i * PSF_i / \sigma_i^2}$$

**Compare this with the aperture photometry:**

$$C = \frac{\sum Pix_i}{\sum PSF_i}$$

**AP is psf-fitting with a simplistic shape!**



# S/N for PSF and aperture photometry

**What is the noise level in our procedures? I.e. if we are probing the pure sky, what is the rms of derived counts?**

**Assume that sky noise is constant  $\sigma_i = \text{const}$  then**

$$\sigma(\text{noise}) = \sigma_{\text{sky}} / \sqrt{\sum PSF_i^2}$$

**For the aperture photometry, get**

$$\sigma(\text{noise}) = \sigma_{\text{sky}} * \sqrt{N} / (\sum PSF_i)^2$$

**So, the noise ratio (or inverse of the S/N ratio) is**

$$\frac{\sigma(\text{aper})}{\sigma(\text{psf})} = \frac{\sqrt{\sum PSF_i^2} * \sqrt{N}}{(\sum PSF_i)^2}$$

**For wide aperture, this becomes**

$$\frac{\sigma(\text{aper})}{\sigma(\text{psf})} = \sqrt{\sum PSF_i^2} * \sqrt{N} \geq 1$$

# PSF shape dependence

**For the ground-based telescopes, the PSF shape mostly depends on seeing – variable atmospheric condition.**

**For a space-based mission, the seeing is non-existent => the following factors are more apparent:**

- 1) color**
- 2) pointing jitter (telemetry info)**
- 3) optical aberrations**
- 4) field dependence**

**Sampling is crucial for centering, width determination, algorithmic processing, etc.**

**Undersampled / critically sampled (FWHM 1-2 pix) / oversampled.**

Things to be cautious about:  
pointing errors (can be easily overlooked),  
large-angle scattering (atm. dust, ccd backscattering, etc).

# PSF modelling

Can use *analytical* shapes:

- 1) 2D Gaussian  $A * \exp(-r^2 / \sigma^2 / 2)$
- 2) Lorentz  $A / (r^2 / \sigma^2 + 1)$
- 3) Moffat  $A / (r^2 / \sigma^2 + 1)^\beta$

May need sub-pixel integration if not well sampled. Hard to model tails, non-circularity.

*Empirical* modelling off the bright field stars:

can templetize PSF(x,y) => “any shape”

But:

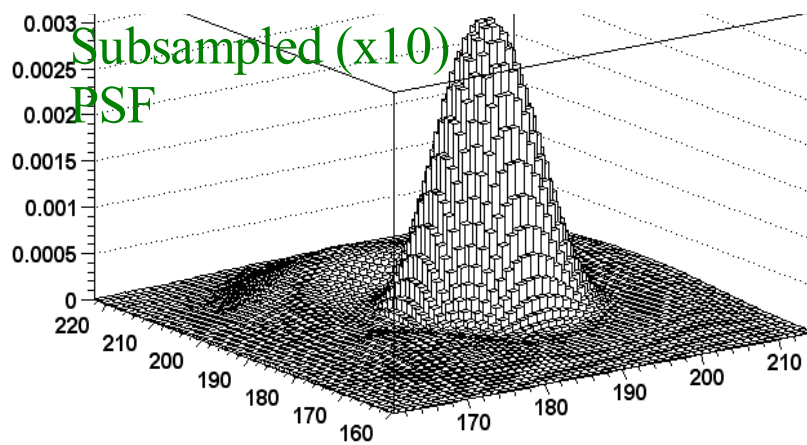
- noisy,
- centering,
- interpolation,
- may not have enough field stars.

*Hybrid* approach:

use analytical models for the fast-varying core, then model the (tail) residuals empirically.



## PSF modelling (cont.)

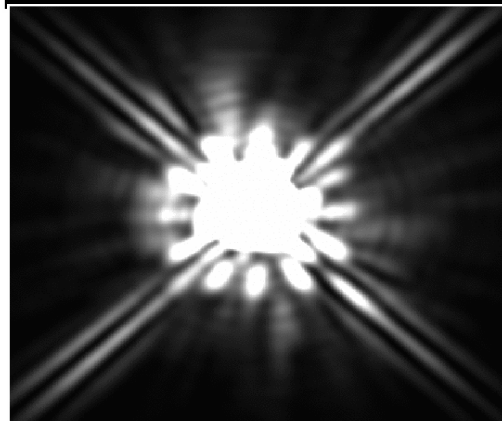


Another approach is to model the PSF from the known optical geometry.

TinyTim package for HST instruments gives a sub-sampled PSF template.



log scale 1

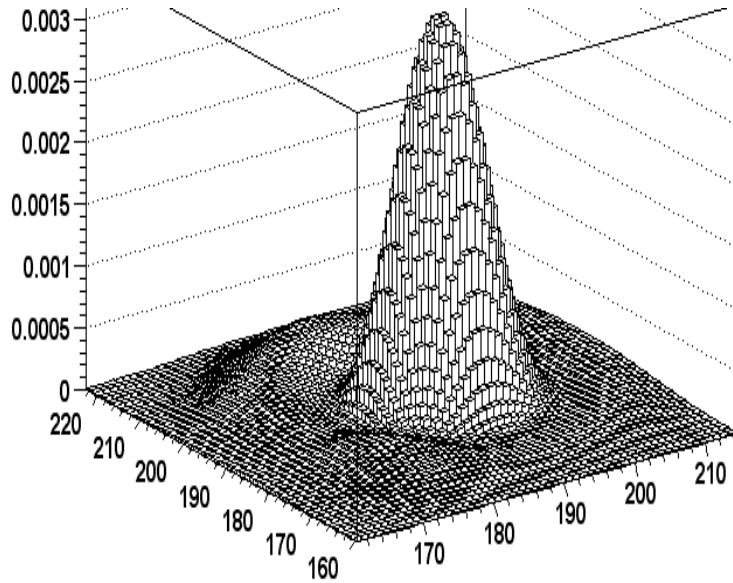


log scale 2

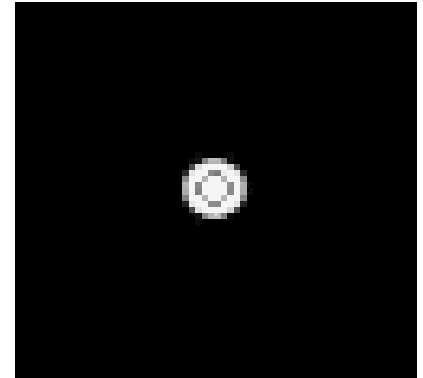
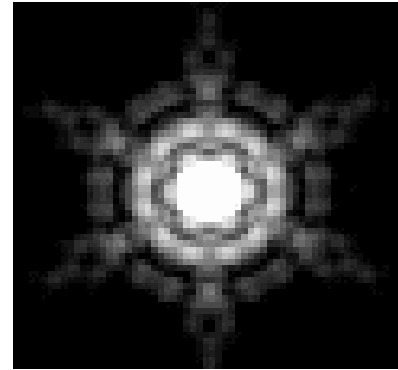
Full geometrical description as an input => can model the diffraction patterns with Airy ring, obscurations, and hard-to-trace features:

- 1) color dependence,
- 2) field dependence,
- 3) focal breathing.

## PSF width in Space

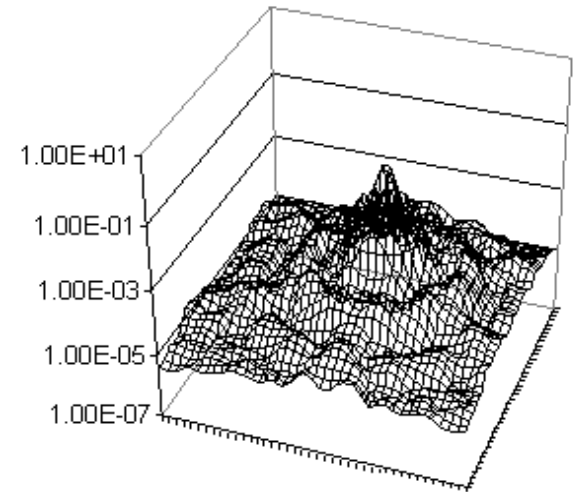


HST (subsampling!)



Spitzer

**1<sup>st</sup> diffraction minimum is at  $R = 1.22 \lambda / d \Rightarrow$   
PSF is wider at longer  $\lambda$  and smaller mirror  
diameter.**



# Aperture Correction

**Aperture photometry is not free of PSF-related knowledge.**

**If correct to infinity:**

- 1) do AP on a star  $\Rightarrow C_{raw}$**
- 2) do AP on the normalized PSF to account for the tails  $\Rightarrow \varepsilon$**
- 3) get the full flux  $C_{\infty} = C_{raw} / \varepsilon$**

**The uncertainty on the PSF correction is small if  $\varepsilon$  is close to 1.**

**Another way to do the large-angle correction is to forget about them.  
Calibrate the flux within fixed radius to standards. HST WFPC2 used  
 $R = 0.5''$ . Relevant if there may be a large-angle scatter.  
(This “fixed” radius may vary with seeing.)**

# “Standard” PSF-fitting packages

Things to be cautious about:

a standard package is a just piece of software, which somebody wrote, and somebody else uses. Domains of applicability vary!

Differences:

- PSF shape,
- background,
- bad pixels.

All for stars photometry.

None accounts for custom errors.

**ROMAFOT** (Buonanno 1983) – developed at Rome Observatory, originally for photographic plates. Gaussian or Moffat PSF.

**STARMAN** (Penny 1995) – a stand-alone program from UK. Hybrid Lorentz-Gaussian-empirical profile. Can deal with very crowded and very undersampled images, as well as field-variable PSF.

**DAOPHOT** (Stetson 1987) – probably the most famous package, included in IRAF. Uses a hybrid approach to PSF building (Gaussian/Moffat/Lorentz). Has bad pixel thresholds.

**DoPHOT** (Schechter 1993) – written with automated processing in mind. Analytical or empirical PSF. Capability to detect CRs and saturated pixels.

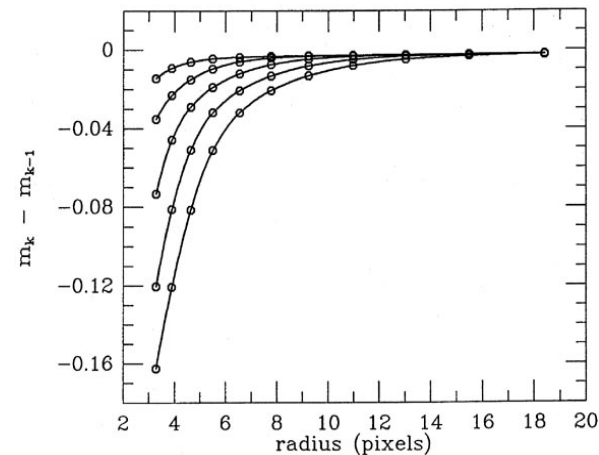
**HSTPHOT** (Dolphin 2000) – written for HST WFPC2. Features TinyTim PSF library with per-image adjustments, bad pixel masks, CTE corrections.

# Typical steps (with DAOPHOT)

Typical steps with PSF photometry in a crowded field include:

- 1) find all stars above a threshold
- 2) run aperture photometry on all stars
- 3) choose a set of bright “good” stars (*growth curves*)
- 4) build a hybrid psf from the sample in step (3)
- 5) PSF fit with position from the centroid and the background from the aperture photometry, i.e. just amplitude.

(There is a star grouping with simultaneous fit in the crowded field.)



A family of growth curves at different seeings.

# Supernova specifics and extensions

**Why invent something new? Because it is necessary...**

**Typically there is a host galaxy near SN => a fast-varying background in the vicinity of the signal.**

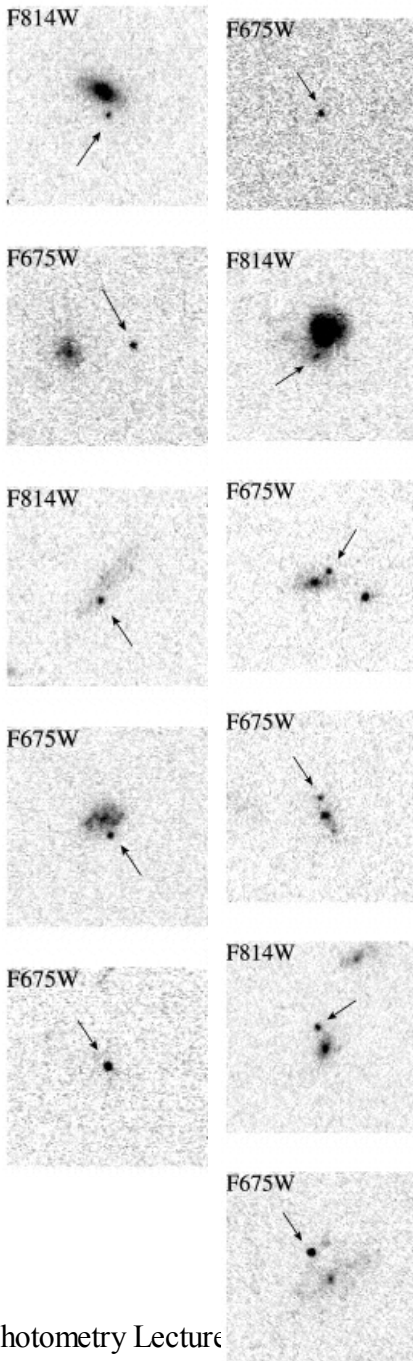
**Usually the packages assume slowly varying background. Can use them if align and subtract the final reference, with *statistical penalty for subtraction*.**

**Extensions:**

**a) PSF + polynomial bkg. behaviour (Rob's paper)**

**One step ahead of the usual assumptions. *Partially separated SN and galaxy*. Valid in particular redshift range and PSF width. *Do not need final references*.**

Thumbnail  
images from  
Rob's paper





# Supernova specifics and extensions (cont.)

## Extensions (cont):

### b) PSF + galaxy model (Nicolas Regnault's thesis)

Used when SN-galaxy distance is less and low-order polynomials do not model the background well. *Need final references.*

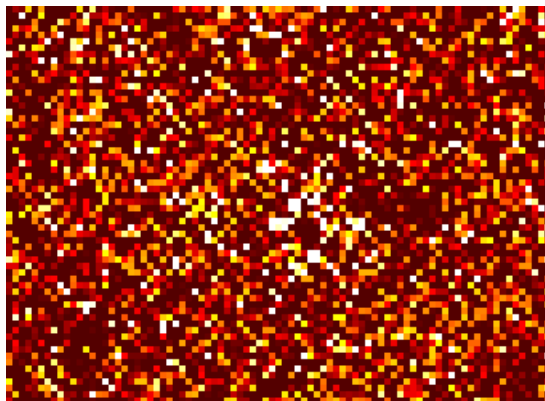
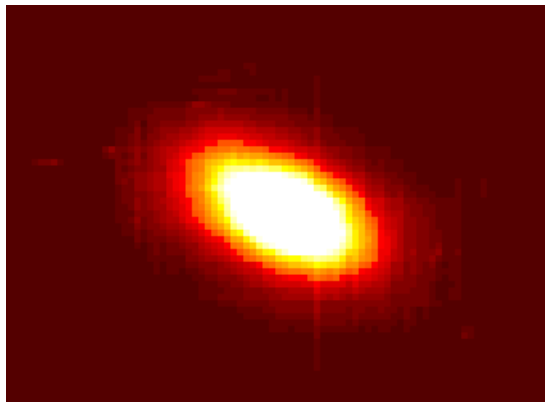
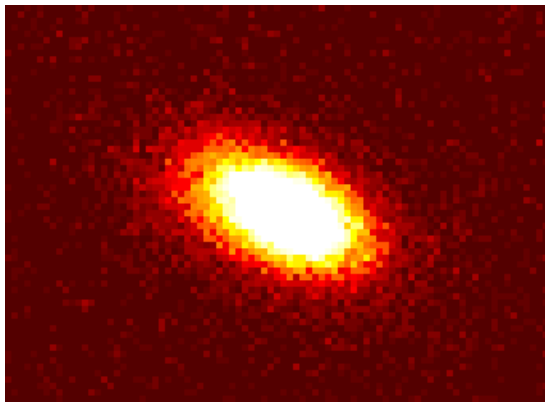
Fit image slices (rows) by the following function:

$$\phi(x) = \phi_0 / (1 + \alpha * |x - x_0|^\beta)$$

Then use spline interpolation for the function values in a column.

This is an intermediate solution between pure 2D spline (noisy) and low-pass filter (blurs galaxy profile).

An example with galaxy, its model and residuals.



## Supernova specifics and extensions (cont.)

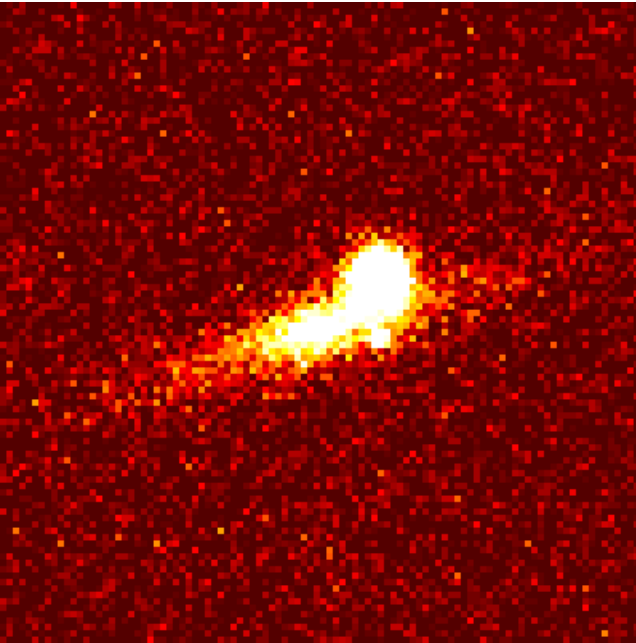
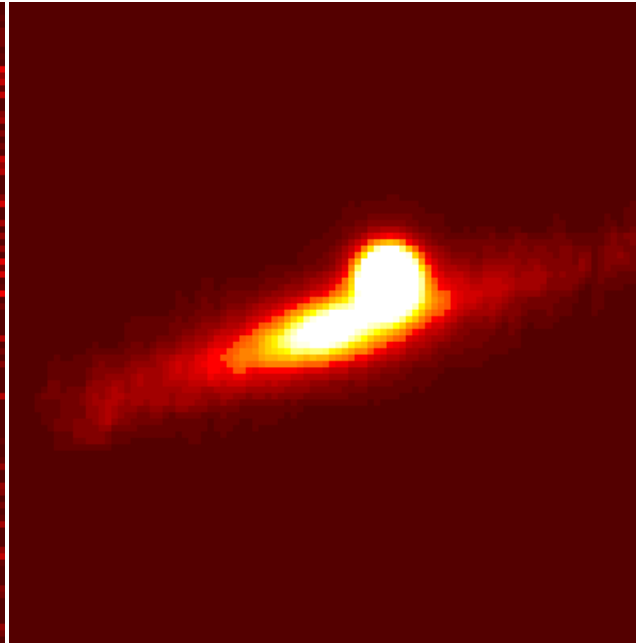
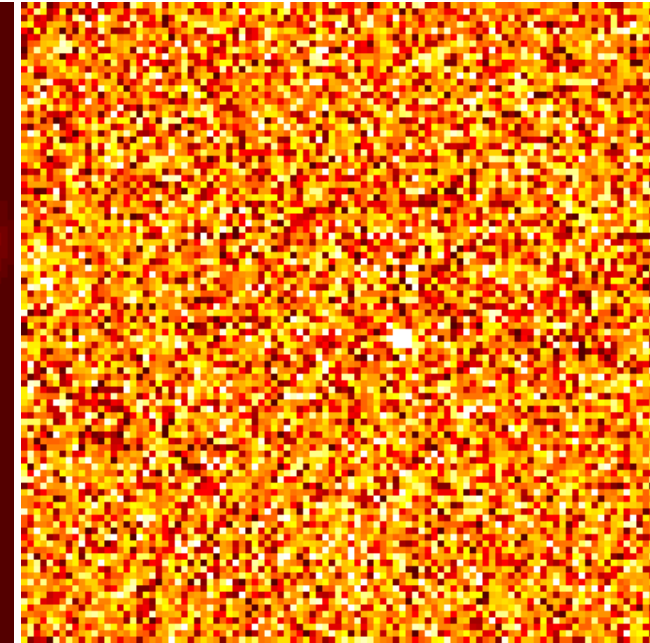


Image with SN and  
host galaxy



Fit function (galaxy  
model + PSF)



Residuals

**Then each SN image is fit with 2 templates: PSF function and galaxy function. There is a problem with matching different seeings. In this case it was solved by distorting the galaxy profile:**

$$Gal(x, y) = H * Gal_0(\alpha * x + \beta * y + \gamma * x * y)$$

# Supernova specifics and extensions (cont.)

## Extensions (cont):

### c) PSF fit to all lightcurve images with pixel-by-pixel background model (Sebastian Fabbro)

Fairly general background consideration. *Need final references.* Field-adaptive PSF and background.

Simultaneous fit for all lightcurve images. TOADS.

- Best seeing image is chosen as a grid/model reference =>  $D_{0ij}$ . All other images are aligned and resampled to its grid. Assumed noiseless. *The pixelized shape of the galaxy on this image is the galaxy model.*
- PSFs and convolution kernels  $K_l$  are determined off the field stars.
- Simultaneous fit for SN flux, position and galaxy model for images 0...n :

$$I_{0ij} = s_0 \quad P_0(x_i - x_s, y_j - y_s) + \quad G(x_i, y_j) + B_0$$

$$I_{1ij} = s_1 [K_1 \otimes P_1(x_i - x_s, y_j - y_s)] + [K_1 \otimes G(x_i, y_j)] + B_1$$

$$I_{nij} = s_n [K_n \otimes P_n(x_i - x_s, y_j - y_s)] + [K_n \otimes G(x_i, y_j)] + B_n$$

$$\text{Minimize} \quad \chi^2 = \sum_l \sum_{i,j} W_{l,i,j} [D_{l,i,j} - I_{l,i,j}]^2$$

Iterative weight adjustment to account for variances of image bkg, PSF, kernel, and model.

## Further reading

**P. Stetson “The Techniques of Least Squares and Stellar Photometry with CCDs”**

(insights of the DAOPHOT author)

**N. Regnault thesis**

(Good general introduction in SN+galaxy photometry; in French)

**S. Fabbro “simfit” writeup**

(Concise description of the method)