

GENERATORS AND STREAMS

CS 61A GROUP MENTORING

July 25, 2018

1 Iterators and Generators

1. What does the following code block output?

```
def foo():  
    a = 0  
    if a < 10:  
        print("Hello")  
        yield a  
        print("World")  
  
for i in foo():  
    print(i)
```

Solution:

```
Hello  
0  
World
```

2. How can we modify `foo` so that it satisfies the following doctests?

```
>>> a = list(foo())
>>> a
[1, 2, 3, 4, 5, 6, 7, 8, 9, 10]
```

Solution: Change the **if** to a `while` statement, and make sure to increment `a`. This looks like:

```
def foo():
    a = 0
    while a < 10:
        a += 1
        yield a
```

3. Define `filter_gen`, a generator that takes in iterable `s` and one-argument function `f` and yields every value from `s` for which `f` returns `True`

```
def filter_gen(s, f):  
    """  
    >>> list(filter_gen([1, 2, 3, 4, 5],  
                        lambda x: x % 2 == 0))  
  
    [2, 4]  
    >>> list(filter_gen([1, 2, 3, 4, 5], lambda x: x < 3))  
    [1, 2]  
    """
```

Solution:

```
    for x in s:  
        if f(x):  
            yield x
```

4. Define `tree_sequence`, a generator that iterates through a tree by first yielding the root value and then yielding the values from each branch. Use the object-oriented representation of trees in your solution.

```
def tree_sequence(t):
    """
    >>> t = Tree(1, [Tree(2, [Tree(5)]), Tree(3, [Tree(4)])])
    >>> print(list(tree_sequence(t)))
    [1, 2, 5, 3, 4]
    """
```

Solution:

```
    yield t.label
    for branch in t.branches:
        for value in tree_sequence(branch):
            yield value
```

Alternate solution:

```
    yield t.label
    for branch in t.branches:
        yield from tree_sequence(branch)
```

5. **(Optional)** Write a generator that takes in a tree and yields each possible path from root to leaf, represented as a list of the values in that path. Use the object-oriented representation of trees in your solution.

```
def all_paths(t):
    """
    >>> t = Tree(1, [Tree(2, [Tree(5)]), Tree(3, [Tree(4)])])
    >>> print(list(all_paths(t)))
    [[1, 2, 5], [1, 3, 4]]
    """
```

Solution:

```
    if t.is_leaf():
        yield [t.label]
    for b in t.branches:
        for subpath in all_paths(b):
            yield [t.label] + subpath
```

2 Streams

1. What's the advantage of using a stream over a scheme list?

Solution: Lazy evaluation. We only evaluate up to what we need.

2. What's the maximum size of a stream?

Solution: Infinity

3. What's stored in the car and cdr of a stream? What are their types?

Solution: First is a value, rest is another stream encapsulated in a promise. The promise in the cdr of a stream may be forced (evaluated) or unforced (yet to be evaluated)

4. When is the next element actually calculated?

Solution: Only when it's requested (and hasn't already been calculated)

5. What Would Scheme Display?

(a) scm> (**define** (foo x) (+ x 10))

Solution: foo

(b) scm> (**define** bar (cons-stream (foo 1) (cons-stream (foo 2) bar)))

Solution: bar

(c) scm> (car bar)

Solution: 11

(d) scm> (cdr bar)

Solution: #[promise (**not** forced)]

(e) scm> (**define** (foo x) (+ x 1))

Solution: foo

(f) scm> (cdr-stream bar)

Solution: (3 . #[promise (**not** forced)])

(g) scm> (**define** (foo x) (+ x 5))

Solution: foo

(h) scm> (car bar)

Solution: 11

(i) scm> (cdr-stream bar)

Solution: (3 . #[promise (**not** forced)])

(j) scm> (cdr bar)

Solution: `#[promise (forced)]`

3 Code Writing for Streams

1. Implement `double-naturals`, which returns a stream that evaluates to the sequence 1, 1, 2, 2, 3, 3, etc.

```
(define (double-naturals)
  (double-naturals-helper 1 #f)
)
```

Solution:

```
(define (double_naturals_helper first go-next)
  (if go-next
      (cons-stream first (double_naturals_helper (+ 1
                                                    first) #f))
      (cons-stream first (double_naturals_helper first
                                                    #t))))
```

2. Implement `interleave`, which returns a stream that alternates between the values in `stream1` and `stream2`. Assume that the streams are infinitely long.

Solution:

```
(define (interleave stream1 stream2)
  (cons-stream
    (car stream1)
    (interleave stream2 (cdr-stream stream1)))
)

(define (interleave stream1 stream2)
  (cons-stream (car stream1)
    (cons-stream (car stream2)
      (interleave (cdr-stream stream1) (cdr-stream
                                          stream2)))))
)
```

4 Tail Recursion

1. Consider the following function:

```
(define (count-instance lst x)
  (cond ((null? lst) 0)
        ((equal? (car lst) x) (+ 1 (count-instance
                                   (cdr lst) x)))
        (else (count-instance (cdr lst) x))))
```

What is the purpose of `count-instance`? Is it tail recursive? Why or why not?

Optional: draw out the environment diagram of this sum-list with `lst = (1 2 1)` and `x = 1`.

Solution: `count-instance` returns the number of times `x` appears in `lst`. It is not tail recursive. The call to `count-instance` appears as one of the arguments to a function call, so it will not be the final thing we do in every frame (we will have to apply `+` after evaluating it.)

2. Rewrite count-instance to be tail recursive.

```
(define (count-tail lst x)
```

```
)
```

Solution:

```
(define (count-tail lst x)
  (define (count-helper lst x instances)
    (cond ((null? lst) instances)
          ((equal? (car lst) x) (count-helper (cdr
        lst) x (+ instances 1)))
          (else (count-helper (cdr lst) x instances))))
  (count-helper lst x 0))
```

3. Implement `filter`, which takes in a one-argument function `f` and a list `lst`, and returns a new list containing only the elements in `lst` for which `f` returns true. Your function must be tail recursive.

You may wish to use the built-in `append` function, which takes in two lists and returns a new list containing the elements of the first list followed by the elements of the second.

```
;Doctests
```

```
scm> (filter (lambda (x) (> x 2)) '(1 2 3 4 5))  
(3 4 5)
```

```
(define (filter f lst)
```

```
)
```

Solution:

```
(define (filter f lst)  
  (define (filter-tail f lst so-far)  
    (cond ((null? lst) so-far)  
          ((f (car lst)) (filter-tail f (cdr lst)  
                                       (append so-far (list (car  
                                                             lst)))))  
          (else (filter-tail f (cdr lst) so-far))))  
  (filter-tail f lst nil))
```