CS 61A Spring 2018

Structure and Interpretation of Computer Programs

FINAL SOLUTIONS

INSTRUCTIONS

- You have 3 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except three hand-written $8.5" \times 11"$ crib sheet of your own creation and the official CS 61A midterm 1, midterm 2, and final study guides.
- Mark your answers on the exam itself. We will not grade answers written on scratch paper.

Last name	
First name	
Student ID number	
CalCentral email (_@berkeley.edu)	
TA	
Name of the person to your left	
Name of the person to your right	
All the work on this exam is my own. (please sign)	

POLICIES & CLARIFICATIONS

- If you need to use the restroom, bring your phone and exam to the front of the room.
- You may use built-in Python functions that do not require import, such as min, max, pow, len, and abs.
- You may not use example functions defined on your study guides unless clearly specified by the question.
- For fill-in-the blank coding problems, we will only grade work written in the provided blanks. You may only write one Python statement per blank line, and it must be indented to the level that the blank is indented.
- Unless otherwise specified, you are allowed to reference functions defined in previous parts of the same question.
- You may use the Tree, Link, and BTree classes defined on Page 2 (left column) of the Midterm 2 Study Guide.

1. (12 points) The Floss

For each of the expressions in the table below, write the output displayed by the interactive Python interpreter when the expression is evaluated. The output may have multiple lines. The first row is completed for you.

- If an error occurs, write **Error**, but include all output displayed before the error.
- To display a function value, write **FUNCTION**.
- To display an iterator value, write **ITERATOR**.
- If an expression would take forever to evaluate, write **FOREVER**.

The interactive interpreter displays the contents of the repr string of the value of a successfully evaluated expression, unless it is None.

Assume that you have started python3 and executed the code shown on the left first, then you evaluate each expression on the right in the order shown. Expressions evaluated by the interpreter have a cumulative effect.

```
class Forth:
    next = 1
    def __init__(self, k):
        self.k = k
    def __repr__(self):
        return str(self.k) + '*'
    def go(self, k):
        if k == 1:
            print(self)
        if k:
            return self.next.go(k-1)
        print(self)
class Back(Forth):
    @property
    def next(self):
        return self
g = [Forth(n) for n in range(3, 8)]
for i in range(4):
    g[i].next = g[i+1]
g[3] = Back(2)
m = map(lambda o: o.k, g)
```

Expression	Output
g[0]	3*
[next(m), next(m)]	[3, 4]
next(next(iter([[0]])))	Error
<pre>len([map(print, g)])</pre>	1
g[0].go(2)	4* 5*
g[0].go(4)	6* 7*
[x.next for x in g[3:]]	[2*, 1]

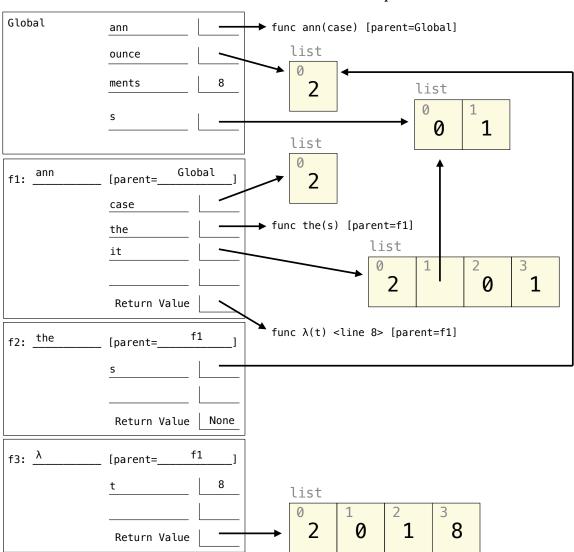
Name:

2. (8 points) Announcements

```
def ann(case):
    def the(s):
        nonlocal case
        case = s[:]
    it = list(ounce)
    it.extend(case.pop())
    if it is not the(case):
        return lambda t: [2]+s+[t]
    else:
        return lambda u: [2]+s+[u]
    ounce, ments = [2, [0, 1]], 8
    s = ounce[1]
    ann(ounce)(ments)
```

Fill in the environment diagram that results from executing the code on the left until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames. A complete answer will:

- Add all missing names and parent annotations to all local frames.
- Add all missing values created or referenced during execution.
- Show the return value for each local frame.
- Use box-and-pointer diagrams for lists and tuples.



3. (7 points) Binary Trees

Definition. A binary search tree is a BTree instance for which the label of each node is larger than all labels in its left branch and smaller than all labels in its right branch.

(a) (5 pt) Implement largest, which takes a binary search tree t and a number x. It returns the largest label in t that is smaller than x. If no such label exists, it returns 0. Assume that t contains only positive numbers as labels. The BTree class is on page 2 (bottom of left column) of the Midterm 2 Study Guide.

```
def largest(t, x):
     """Return the largest label in t that is less than x, or 0 if none exists.
    >>> a = BTree(5, BTree(3, BTree(1), BTree(3.5)), BTree(8, BTree(5.5), BTree(9)))
    >>> largest(a, 5)
    3.5
    >>> largest(a, 5.1)
    >>> largest(a, 6)
    >>> largest(a.right, 5)
    11 11 11
    if t is BTree.empty:
        return 0
    elif t.label >= x:
        return largest(t.left, x)
    y = largest(t.right, x)
    if y:
        return y
    return t.label
(b) (2 pt) Implement second, which takes a binary search tree t containing only positive numbers, and a
   number x. It returns the second largest label in t that is smaller than x.
def second(t, x):
     """Return the second largest label in t that is less than x, or 0 if none exists.
    >>> a = BTree(5, BTree(3, BTree(1), BTree(3.5)), BTree(8, BTree(5.5), BTree(9)))
    >>> second(a, 5)
    3
    >>> second(a, 5.1)
```

3.5 >>> second(a.left, 2) return largest(t, largest(t, x)) Name: 5

4. (10 points) Apply Yourself

(a) (6 pt) Implement times, which takes a one-argument function f and a starting value x. It returns a function g that takes a value y and returns the minimum number of times that f must be called on x to return y. Assume that calling f repeatedly on x eventually results in y.

```
def times(f, x):
    """Return a function g(y) that returns the number of f's in f(f(...(f(x)))) == y.
    >>> times(lambda a: a + 2, 0)(10)
                                        #5 times: 0 + 2 + 2 + 2 + 2 + 2 == 10
    >>> times(lambda a: a * a, 2)(256) # 3 times: square(square(square(2))) == 256
    3
    11 11 11
    def repeat(z):
        """Yield an infinite sequence of z, f(z), f(f(z)), f(f(f(z))), f(f(f(z))), ...."""
        yield z
        yield from repeat(f(z))
    def g(y):
        n = 0
        for w in repeat(x):
            if w == y:
                return n
            n += 1
```

return g

(b) (2 pt) Circle the Θ expression that describes how many steps are required to evaluate f(f(n)), assuming f(n) returns 2^n for all n, and $\Theta(n)$ steps are required to evaluate f(n).

- $\Theta(1)$ $\Theta(\log n)$ $\Theta(\sqrt{n})$ $\Theta(n)$ $\Theta(n^2)$ None of these
- (c) (2 pt) Circle the Θ expression that describes how many steps are required to evaluate g(g(n)), assuming g(n) returns \sqrt{n} for all n, and $\Theta(n)$ steps are required to evaluate g(n).
 - $\Theta(1)$ $\Theta(\log n)$ $\Theta(\sqrt{n})$ $\Theta(n)$ $\Theta(n^2)$ None of these

5. (12 points) Functions As Expected

Definition. For n > 1, an order n function takes one argument and returns an order n-1 function. An order 1 function is any function that takes one argument.

(a) (6 pt) Implement scurry, which takes a function f and a positive integer n. f must be a function that takes a list as its argument. scurry returns an order n function that, called successively n times on a sequence of values $x_1, x_2, \ldots x_n$, returns the result of calling f on a list containing $x_1, x_2, \ldots x_n$.

```
def scurry(f, n):
     """Return a function that calls f on a list of arguments after being called n times.
    >>> scurry(sum, 4)(1)(1)(3)(2) # equivalent to sum([1, 1, 3, 2])
    >>> scurry(len, 3)(7)([8])(-9) # equivalent to len([7, [8], -9])
    11 11 11
    def h(k, args_so_far):
         if k == 0:
             return f(args_so_far)
         return lambda x: h(k-1, args_so_far + [x])
    return h(n, [])
(b) (6 pt) Implement factorize, which takes two integers n and k, both larger than 1. It returns the number
   of ways that n can be expressed as a product of non-decreasing integers greater than or equal to k.
def factorize(n, k=2):
    """Return the number of ways to factorize positive integer {\tt n}.
    >>> factorize(7) # 7
    1
    >>> factorize(12) # 2*2*3, 2*6, 3*4, 12
    >>> factorize(36) # 2*2*3*3, 2*2*9, 2*3*6, 2*18, 3*3*4, 3*12, 4*9, 6*6, 36
     11 11 11
    if k == n:
         return 1
    elif k > n:
         return 0
    elif n % k > 0:
         return factorize(n, k + 1)
    return factorize(n // k, k) + factorize(n, k + 1)
```

Name:

6. (16 points) Scheme Forever

(a) (4 pt) Implement fibs, which takes a positive integer n and prints out the first n Fibonacci numbers in order, one on each line. For example, (fibs 7) prints 0 on one line, 1 on the next, then 1, 2, 3, 5, and 8; seven lines in total. Your implementation must run in constant space to receive full credit.

```
(define (fibs n)
  ; Print the first n Fibonacci numbers. Each one is the sum of the previous two.
  ; (fibs 7) prints the Fibonacci numbers 0 1 1 2 3 5 8 each on a different line.
  (define (taipei a b k)
     (if (= k n)
         (print b)
         (begin (print b) (taipei b (+ a b) (+ k 1))) ))
(taipei 1 0 1))
(b) (4 pt) Write the first 7 elements of each stream that results from the two calls to e below. Note: In Scheme,
   quotient performs floor division like // in Python, and remainder is like % in Python.
(define (e n d) (cons-stream (quotient n d) (e (* 10 (remainder n d)) d)))
(e 1 8)
           ; Starts with: 0 1 2 5 0 0 0
(e 2 3)
           ; Starts with: 0 6 6 6 6 6 6
(c) (4 pt) Implement lambda-macro, a macro that creates anonymous macros. A lambda-macro expression has
   a list of formal parameters and one body expression. It creates a macro with those formal parameters and
   that body. Assume that the symbol anon is not use anywhere else in a program that contains lambda-macro.
(define-macro (lambda-macro bindings body)
     ; A lambda-macro expression evaluates to a macro.
     ; For example: ((lambda-macro (expr) (car expr)) (+ 1 2)) evaluates to the symbol +
     `(begin (define-macro ,(cons 'anon bindings) ,body)
             anon))
(d) (4 pt) Implement dotted?, which takes a value s. It returns whether s is a dotted list or contains a dotted
   list anywhere within it.
(define (dotted? s)
  ; Return whether s contains a dotted list.
  ; Examples that are dotted:
                                  (1 2 . 3) , (1 (2 . 3)) , (((1 . 2)) 3)
  ; Examples that are not dotted: (1 2 3) , (1 2.3) , ((1) ((2)) 3)
  (cond ((not (pair? s)) #f)
         ((not-pair-or-nil? (cdr s)) #t)
         (else (or (dotted? (car s)) (dotted? (cdr s))))))
```

(define (not-pair-or-nil? s) (and (not (pair? s)) (not (null? s))))

7. (10 points) Gotta Select 'Em All

For the questions below, assume that the following two SQL statements have been executed. The pokedex table describes the names of some Pokémon and their heights in inches. The evolve table describes how those Pokémon can evolve into the other Pokémon in the pokedex.

```
CREATE TABLE pokedex AS
```

```
SELECT "Eevee" AS name, 12 as height UNION
                                                 CREATE TABLE evolve AS
SELECT "Jolteon"
                       , 31
                                       UNION
                                                   SELECT "Eevee" AS before,
                                                                              "Jolteon" AS after UNION
                       , 39
SELECT "Leafeon"
                                       UNION
                                                   SELECT "Eevee"
                                                                              "Leafeon"
                                                                                                   UNION
SELECT "Bulbasaur"
                       , 28
                                       UNION
                                                   SELECT "Bulbasaur"
                                                                               "Ivysaur"
                                                                                                   UNION
SELECT "Ivysaur"
                         39
                                       UNION
                                                   SELECT "Ivysaur"
                                                                               "Venasaur"
                                                                                                   UNION
SELECT "Venasaur"
                         79
                                       UNION
                                                   SELECT "Charmander"
                                                                               "Charmeleon"
                                                                                                   UNION
                       , 24
SELECT "Charmander"
                                       UNION
                                                   SELECT "Charmeleon"
                                                                              "Charizard";
SELECT "Charmeleon"
                       , 43
                                       UNION
SELECT "Charizard"
                       , 67;
```

(a) (4 pt) Write a SQL statement that adds a new row to the evolve table for each pair of Pokémon for which before evolves to after in two steps. For example, Charmander can evolve twice: first to Charmeleon and then to Charizard. Therefore, ("Charmander", "Charizard") should be added as a row. Likewise, ("Bulbasaur", "Venasaur") should also be added. Your statement should behave correctly even if the rows in evolve and pokedex were different. The rows can be added in any order.

```
INSERT INTO evolve

SELECT a.before, b.after

FROM evolve AS a, evolve AS b

WHERE a.after = b.before;

SELECT * FROM evolve;
```

(b) (6 pt) Write a SELECT statement that results in a table with one row for each Pokémon that can evolve. The table should have two columns: the first contains the name of the Pokémon that can evolve, and the second contains the maximum increase in height that it can attained by evolving. For example, Eevee can grow as much as 27 inches (when evolving to Leafeon), so the result should contain the row ("Eevee", 27). Your statement should behave correctly even if the rows in evolve and pokedex were different. The result should only consider ways of evolving that are described by a single row in the evolve table.

```
SELECT before, max(b.height - a.height)

FROM evolve, pokedex as a, pokedex as b

WHERE before=a.name AND after=b.name

GROUP BY before;
```