

Practical Exercises:
Classical cryptography and cryptanalysis

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Changelog

- v1.0 - Initial version.

1 Introduction

In classical cryptography, the information subject to cryptographic transformations was just the sequence of letters extracted from a text, excluding all non-alphabetical symbols (spaces, digits, punctuation, etc.). Also, characters with diacritics were used without them (thus, á was transformed to a, ç was transformed to c, etc.). Thus, the plaintext presented to the encryption algorithm was a sequence of letters, disregarding case, and the resulting ciphertext was of the same nature.

Those plaintext contents maintain the relative frequency of letters, as well as digrams, trigrams, etc., but can create some less evident n-grams, caused by space suppressions (e.g. “six xylophones” becomes “sixxylophones”, which contains an “xx” digram that does not exist in English).

2 Preparation

Select a set of texts from a given language (Portuguese, English) and create a tool to prepare them for encryption with classical cryptographic tools. Then, create tools to evaluate their letter frequency, as well as to evaluate the more frequent n-grams (digrams, trigrams, etc.). You will get different results for different languages. Choose large texts for getting more accurate statistics.

3 Classical monoalphabetic substitution encryption

In the classical monoalphabetic encryption using the substitution of symbols, the first step to take is to create a single substitution alphabet, or table, for a given key.

Use some strategy to create it, and use it to perform a successful encryption and decryption of the prepared texts.

Use the tools previously developed to analyse the statistics of the cryptograms, and verify that the frequency of letters and n-grams is kept, though for different letters and n-grams. This fact is the starting point for a successful cryptanalysis of a classical cryptogram performed with a monoalphabetical cipher.

4 Classical polyalphabetic substitution encryption

Polyalphabetic substitution encryption attempts to mitigate the weaknesses of monoalphabetic techniques, namely to hide the frequencies of letters and n-grams of the original plaintext that are observable in the ciphertext.

Use a Vigenère square to implement a polyalphabetic cipher and decipher. Note: you do not have to create the complete square, you can compute its transformations.

Encrypt texts with the Vigenère cipher, with a given key, and use the analysis tools previously developed to observe the statistics of the cryptograms produced for different key lengths. Compare these statistics with the ones observed with cryptograms created with monoalphabetic ciphers.

4.1 Determination of the key length

The cryptanalysis of polyalphabetic ciphers that use a short-term, cyclic behaviour can benefit from knowing the number of alphabets used to implement it (usually, in a round-robin fashion). This information allows a cryptanalyst to slice the cryptogram in N parts, where N is the number of alphabets used consecutively, and to process each part as the result of a monoalphabetic cipher. The cryptanalysis of a slice can also facilitate the cryptanalysis of other adjacent slices, because tentative substitutions may be used to find suitable n-grams on the recovered text.

Create a tool to find possible sizes of an encryption key for a Vigenère cipher. For that purpose, use the Kasiski and the index of coincidence (autocorrelation) methods. Verify the tool efficacy with the cryptograms previously generated.

References

- Substitution cipher, https://en.wikipedia.org/wiki/Substitution_cipher
- Vigenère cipher, https://en.wikipedia.org/wiki/Vigen%C3%A8re_cipher
- Kasiski examination, https://en.wikipedia.org/wiki/Kasiski_examination
- Index of coincidence, https://en.wikipedia.org/wiki/Index_of_coincidence