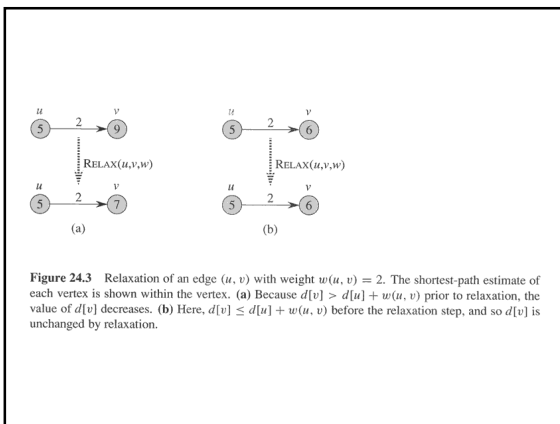
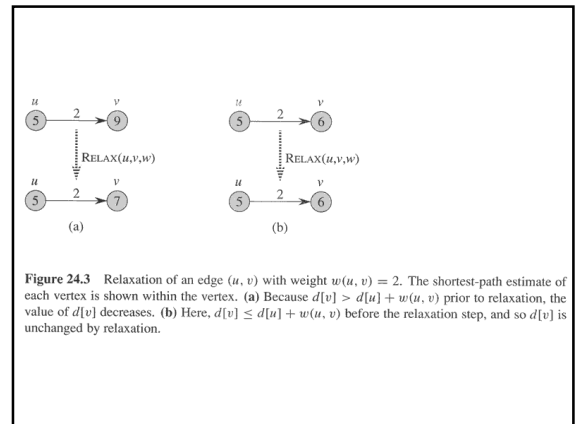


```

INITIALIZE-SINGLE-SOURCE( $G, s$ )
1  for each vertex  $v \in V[G]$ 
2      do  $d[v] \leftarrow \infty$ 
3       $\pi[v] \leftarrow \text{NIL}$ 
4   $d[s] \leftarrow 0$ 

```



```

RELAX( $u, v, w$ )
1  if  $d[v] > d[u] + w(u, v)$ 
2      then  $d[v] \leftarrow d[u] + w(u, v)$ 
3       $\pi[v] \leftarrow u$ 

```

BELLMAN-FORD(G, w, s)

```

1 INITIALIZE-SINGLE-SOURCE( $G, s$ )
2 for  $i \leftarrow 1$  to  $|V[G]| - 1$ 
3   do for each edge  $(u, v) \in E[G]$ 
4     do RELAX( $u, v, w$ )
5 for each edge  $(u, v) \in E[G]$ 
6   do if  $d[v] > d[u] + w(u, v)$ 
7     then return FALSE
8 return TRUE

```

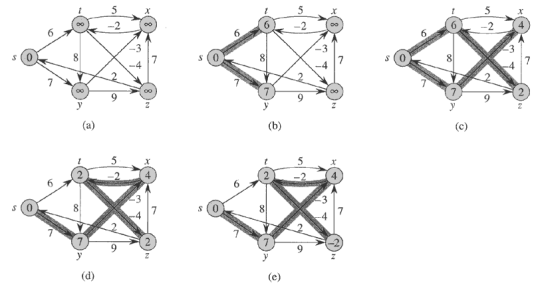


Figure 24.4 The execution of the Bellman-Ford algorithm. The source is vertex s . The d values are shown within the vertices, and shaded edges indicate predecessor values: if edge (u, v) is shaded, then $\pi[v] = u$. In this particular example, each pass relaxes the edges in the order $(t, x), (t, y), (t, z), (x, t), (y, x), (y, z), (z, x), (z, s), (s, t), (s, y)$. (a) The situation just before the first pass over the edges. (b)–(e) The situation after each successive pass over the edges. The d and π values in part (e) are the final values. The Bellman-Ford algorithm returns TRUE in this example.

DIJKSTRA(G, w, s)

```

1 INITIALIZE-SINGLE-SOURCE( $G, s$ )
2  $S \leftarrow \emptyset$ 
3  $Q \leftarrow V[G]$ 
4 while  $Q \neq \emptyset$ 
5   do  $u \leftarrow \text{EXTRACT-MIN}(Q)$ 
6      $S \leftarrow S \cup \{u\}$ 
7   for each vertex  $v \in \text{Adj}[u]$ 
8     do RELAX( $u, v, w$ )

```

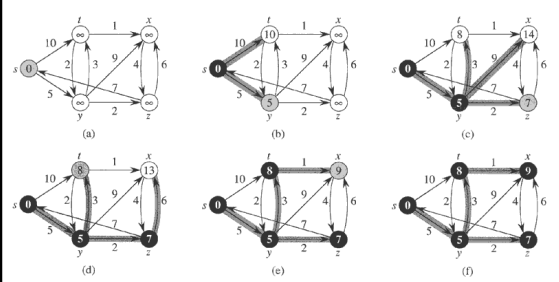


Figure 24.6 The execution of Dijkstra's algorithm. The source s is the leftmost vertex. The shortest-path estimates are shown within the vertices, and shaded edges indicate predecessor values. Black vertices are in the set S , and white vertices are in the min-priority queue $Q = V - S$. (a) The situation just before the first iteration of the while loop of lines 4–8. The shaded vertex has the minimum d value and is chosen as vertex u in line 5. (b)–(f) The situation after each successive iteration of the while loop. The shaded vertex in each part is chosen as vertex u in line 5 of the next iteration. The d and π values shown in part (f) are the final values.

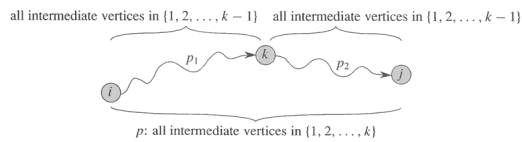


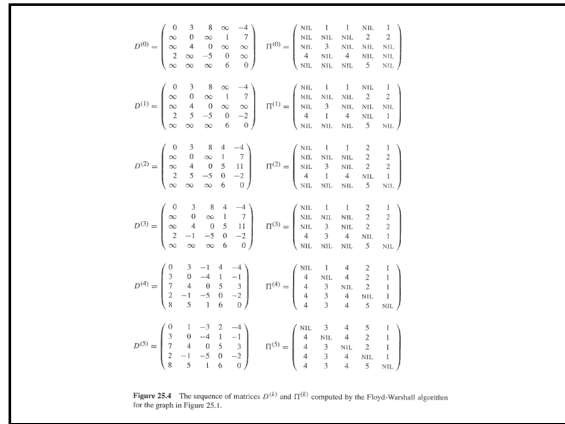
Figure 25.3 Path p is a shortest path from vertex i to vertex j , and k is the highest-numbered intermediate vertex of p . Path p_1 , the portion of path p from vertex i to vertex k , has all intermediate vertices in the set $\{1, 2, \dots, k-1\}$. The same holds for path p_2 from vertex k to vertex j .

FLOYD-WARSHALL(W)

```

1  $n \leftarrow \text{rows}[W]$ 
2  $D^{(0)} \leftarrow W$ 
3 for  $k \leftarrow 1$  to  $n$ 
4   do for  $i \leftarrow 1$  to  $n$ 
5     do for  $j \leftarrow 1$  to  $n$ 
6       do  $d_{ij}^{(k)} \leftarrow \min(d_{ij}^{(k-1)}, d_{ik}^{(k-1)} + d_{kj}^{(k-1)})$ 
7 return  $D^{(n)}$ 

```

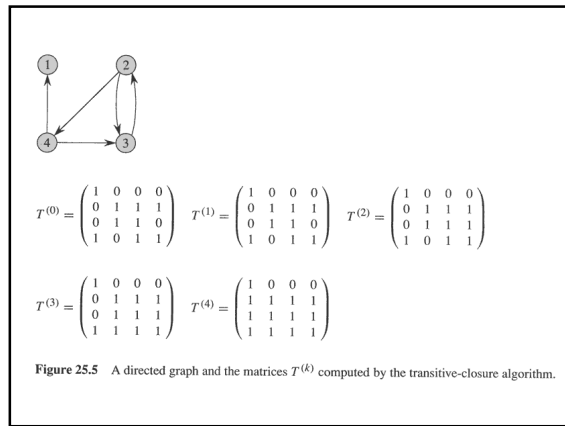


TRANSITIVE-CLOSURE(G)

```

1   $n \leftarrow |V[G]|$ 
2  for  $i \leftarrow 1$  to  $n$ 
3      do for  $j \leftarrow 1$  to  $n$ 
4          do if  $i = j$  or  $(i, j) \in E[G]$ 
5              then  $t_{ij}^{(0)} \leftarrow 1$ 
6              else  $t_{ij}^{(0)} \leftarrow 0$ 
7  for  $k \leftarrow 1$  to  $n$ 
8      do for  $i \leftarrow 1$  to  $n$ 
9          do for  $j \leftarrow 1$  to  $n$ 
10             do  $t_{ij}^{(k)} \leftarrow t_{ij}^{(k-1)} \vee (t_{ik}^{(k-1)} \wedge t_{kj}^{(k-1)})$ 
11  return  $T^{(n)}$ 

```

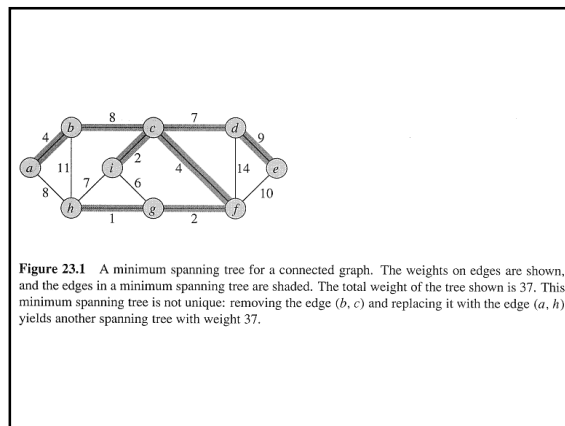


FLOYD-WARSHALL'(W)

```

1   $n \leftarrow \text{rows}[W]$ 
2   $D \leftarrow W$ 
3  for  $k \leftarrow 1$  to  $n$ 
4      do for  $i \leftarrow 1$  to  $n$ 
5          do for  $j \leftarrow 1$  to  $n$ 
6              do  $d_{ij} \leftarrow \min(d_{ij}, d_{ik} + d_{kj})$ 
7  return  $D$ 

```

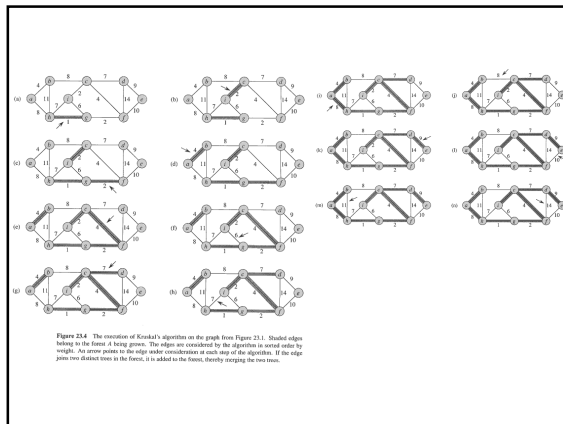
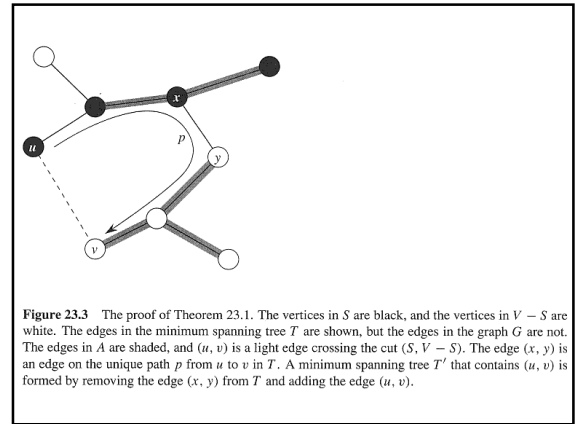
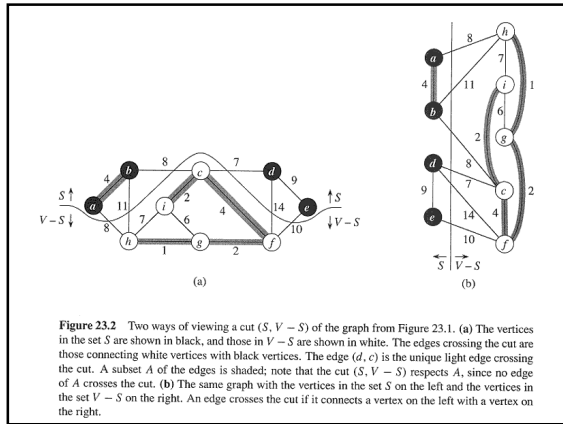


GENERIC-MST(G, w)

```

1   $A \leftarrow \emptyset$ 
2  while  $A$  does not form a spanning tree
3      do find an edge  $(u, v)$  that is safe for  $A$ 
4           $A \leftarrow A \cup \{(u, v)\}$ 
5  return  $A$ 

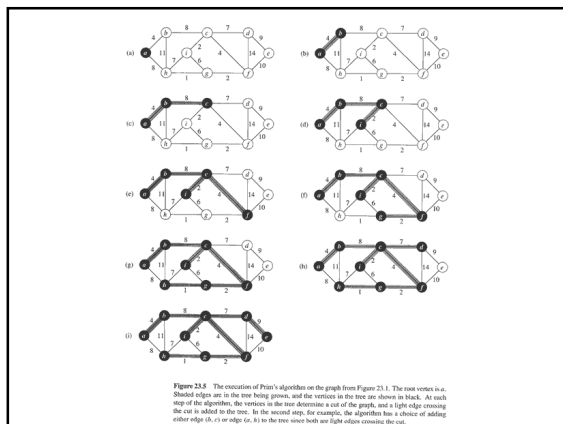
```



```

MST-KRUSKAL( $G, w$ )
1   $A \leftarrow \emptyset$ 
2  for each vertex  $v \in V[G]$ 
3      do MAKE-SET( $v$ )
4  sort the edges of  $E$  into nondecreasing order by weight  $w$ 
5  for each edge  $(u, v) \in E$ , taken in nondecreasing order by weight
6      do if FIND-SET( $u$ )  $\neq$  FIND-SET( $v$ )
7          then  $A \leftarrow A \cup \{(u, v)\}$ 
8              UNION( $u, v$ )
9  return  $A$ 

```



```

MST-PRIM( $G, w, r$ )
1  for each  $u \in V[G]$ 
2      do  $key[u] \leftarrow \infty$ 
3           $\pi[u] \leftarrow \text{NIL}$ 
4   $key[r] \leftarrow 0$ 
5   $Q \leftarrow V[G]$ 
6  while  $Q \neq \emptyset$ 
7      do  $u \leftarrow \text{EXTRACT-MIN}(Q)$ 
8          for each  $v \in \text{Adj}[u]$ 
9              do if  $v \in Q$  and  $w(u, v) < key[v]$ 
10                  then  $\pi[v] \leftarrow u$ 
11                       $key[v] \leftarrow w(u, v)$ 

```

```

MST-REDUCE( $G, orig, c, T$ )
1  for each  $v \in V[G]$ 
2    do  $mark[v] \leftarrow \text{FALSE}$ 
3    MAKE-SET( $v$ )
4  for each  $u \in V[G]$ 
5    do if  $mark[u] = \text{FALSE}$ 
6      then choose  $v \in Adj[u]$  such that  $c[u, v]$  is minimized
7      UNION( $u, v$ )
8       $T \leftarrow T \cup \{orig[u, v]\}$ 
9       $mark[u] \leftarrow mark[v] \leftarrow \text{TRUE}$ 
10  $V[G'] \leftarrow \{\text{FIND-SET}(v) : v \in V[G]\}$ 
11  $E[G'] \leftarrow \emptyset$ 
12 for each  $(x, y) \in E[G]$ 
13   do  $u \leftarrow \text{FIND-SET}(x)$ 
14    $v \leftarrow \text{FIND-SET}(y)$ 
15   if  $(u, v) \notin E[G']$ 
16     then  $E[G'] \leftarrow E[G'] \cup \{(u, v)\}$ 
17      $orig'[u, v] \leftarrow orig[x, y]$ 
18      $c'[u, v] \leftarrow c[x, y]$ 
19   else if  $c[x, y] < c'[u, v]$ 
20     then  $orig'[u, v] \leftarrow orig[x, y]$ 
21      $c'[u, v] \leftarrow c[x, y]$ 
22 construct adjacency lists  $Adj$  for  $G'$ 
23 return  $G', orig', c',$  and  $T$ 

```