State Space Et Laplace
$i_x = A_x + Bu$ $y = C_x + Du$ $G_{yu}(s)$
Review Properties of Laplace Transforms
$\mathcal{L}[x(t)](s) = \int_{0}^{\infty} e^{-st} x(t) dt$
× (+) ( × (5) Appendix A )
$\dot{x}(t) \iff \underline{s} \times (\underline{s}) - \times (\underline{\circ})$
$\int_{0}^{\tau} x(z) dz \iff \frac{1}{5} x(s)$
$\alpha \times (t) + \beta \gamma(t) \iff \alpha \times (s) + \beta \gamma (s)$
Transfer Function
$\dot{x} + 2 \int \omega_n \dot{x} + \omega_n^2 x = \omega_n^2 u$
$\ddot{x} = -2 \Im \omega_n \dot{x} - \omega_n^2 x + \omega_n^2 u$
52 x1)= -2 Jwn 5 x1+ wn2 x(s)+ wn2 u(s)
$(5^2 + 7 \int \omega_n + \omega_n^2) \times (6) = \omega_n^2 \omega (6)$
$G_{xy}(s) = \frac{X(s)}{u(s)} = \frac{\omega_n^2}{s^2 + 2 s \omega_n s + \omega_n^2}$
step $u(t) \longrightarrow u(s)$ step $u(s) = \frac{1}{5}$
impulse u(s) = 1 S(o)
$\int_{-\infty}^{\infty} \delta(t) dt = 1 \qquad \qquad \times (5) = G_{xu}(5) u(5)$
$\times (5) \longrightarrow \times (+)$ table, method of partial fractions
$\frac{5+b}{5^{3}+a_{2}s^{2}+a_{2}s^{2}+a_{3}} \xrightarrow{C_{1}} \frac{c_{1}}{5^{2}+d_{1}} + \frac{c_{2}}{5^{2}+d_{2}}$
$5^{5} + a_{1}5^{2} + a_{2}5^{4} + a_{3}$ $5^{2} + d_{1}$ $5^{2} + d_{2}$
Final Value Theorem
$\lim_{t\to\infty} x(t) = \lim_{s\to 0} s x(s)$
Only if sx(s) is stable

Two representations of a Linear System

11x-A

$$5 \times (5) \stackrel{?}{=} A \times (6) + B u(5)$$
  
 $(5I - A) \times (5) = B u(5)$   
 $X(5) = (5I - A)^{-1} B u(5)$   
 $Y(5) = ((5I - A)^{-1} B + D) u(5)$   
(from here on assume D=0)

$$M^{-1} = \frac{adj(M)}{|M|}$$

$$(SI-A)^{-1} = \frac{adj(sI-A)}{|sI-A|}$$

Adjugate: transpose of cofactor matrix F

$$F_{ij} = \frac{(-1)^{i+j}}{M_{-i-j}} M_{-i-j}$$

$$C_{-i,z} \text{ all rows except } i$$

$$ad_{j}(M) = F^{T}$$

$$G_{yu}(s) = \frac{y(s)}{u(s)} = C(sI-A)^tB = \frac{Cad_1^s(sI-A)B}{|sI-A|} = \frac{N(s)}{D(s)}$$

$$(sI-A)=0$$

Roots of D(s) are the eigenvalues of A

Stability (all roots of D(s) in LHP all eigenvalues of A in LHP

$$G(s) = \frac{N(s)}{D(s)} = \frac{b_0 s^n + b_0 s^{n-1} \dots b_n s^n + b_n}{a_0 s^n + \dots a_n s^n + a_n}$$

$$e.g. \frac{Y(s)}{U(s)} = G(s) = \frac{b_0 s^n + b_0}{s^2 + a_0 + a_0}$$

$$= \frac{b_0 s^n + b_0}{x(s)}$$

$$= \frac{b_0 s^n + b_0 s^n}{x(s)}$$

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$$= \frac{b_0 s^n + b_0 s^n + b_0 s^n}{x(s)}$$

$$= \frac{b_0 s^n + b_0 s^n + b$$

(1+GC) y = Gyr