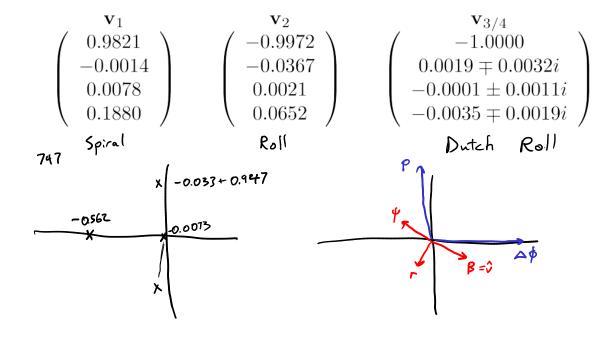
## Lateral Mode Approximations and Control Surfaces

$$\dot{\mathbf{x}}_{lat} = \mathbf{A}_{lat}\mathbf{x}_{lat} + \mathbf{c}_{lat}$$



$$A_{lat} = \begin{bmatrix} y_{v} & y_{r} & y_{r} & g_{\omega s} \theta_{o} \\ L_{v} & L_{r} & L_{r} & 0 \\ N_{v} & N_{r} & N_{r} & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$

ZXZ Spiral Approx.

$$\widetilde{V}_{1} = \begin{bmatrix} -0.00 & 12 \\ 0.00 & 13 \\ -0.00 & 13 \\ -0.1769 \\ 1.0 \end{bmatrix}$$

$$\widetilde{V}_{1} = \begin{bmatrix} -0.0012 \\ 0.0013 \\ -0.0073 \\ -0.1769 \\ 1.0 \end{bmatrix}$$

$$\begin{array}{c} p = 0 \\ p = 0 \\ \hline p$$

$$V = -\frac{1}{2} V$$

$$\dot{x} = -N_v \frac{1}{2}r + N_r r = \frac{N_r L_v - N_v L_r}{L_v}$$

$$\dot{x} = A_x e$$

$$|A - \lambda I| = 0 \qquad \lambda = A \quad \text{if } A \text{ is a scalar}$$

$$\frac{\lambda_{s,approx} = \left(\frac{N_{r}L_{v} - N_{v}L_{r}}{L_{v}}\right)}{L_{v}} = -0.0296 \quad for B747$$

$$T = \frac{1}{h} = 33.8s$$

$$= -0.0296$$
 for B  
 $T = \frac{1}{33.86}$ 

$$-0.0073$$
 Not a great  $T = 1375$  approximation

Characteristic Egn-Baced Spiral

$$|A_{lat} - \lambda I| = A \frac{\lambda}{1} + B \frac{3}{3} + C \frac{\lambda}{2} + D \lambda + E = 0$$
Since  $\lambda_s < < 1$ 

$$DJ + E = 0$$

$$\overline{J_{S,approx}} = -\overline{E}$$

$$\overline{J_{S,approx}} = -\overline{E}$$

$$DJ + E = 0$$

$$\overline{J_{S,approx}} = -\overline{D}$$

$$DJ + E = 0$$

$$DJ$$

for 18747 
$$\lambda_{5,approx} = -0.00725$$

One necessary condition for stability is E70 (Lloca, - Clocabo + (Clocabo - Clocabo Sin Bo >0 Roll Approximation p = Lp λ,= -0.56Z 1, approx = 1p = - Q434 23% difference Roll + Spiral Approximation Assume side force due to gravity produces same you rate that would exist with \$=0 0 = ~uor + g \$ & Also assume Yp=Y,=0  $\begin{bmatrix} 0 \\ \rho \\ r \end{bmatrix} = \begin{bmatrix} 0 & 0 & -u_0 & 9 \\ 1 & 1_p & 1_r & 0 \\ N_r & N_p & N_r & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} V \\ \rho \\ r \\ \phi \end{bmatrix}$  $\begin{vmatrix} \tilde{A} - \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & \lambda & 0 & 0 \\ 0 & 0 & \lambda & 0 \\ 0 & 0 & 0 & \lambda \end{vmatrix} = C \lambda^2 + D \lambda + E = 0$ D= u0 (2, Np - I, Nv) - g I E=g(L, N, -L, N) λ, approx = -0.00734 λ<sub>γαμριοχ</sub> = -0.597 "true" -0.0073 Dutch Roll Approx = 0=0 Y, =0 Assume  $\phi = p = 0$  $\begin{bmatrix} \dot{v} \\ \dot{r} \end{bmatrix} = \begin{bmatrix} \dot{y}_{v} & -u_{o} \\ \dot{v}_{v} & \mathcal{N}_{r} \end{bmatrix} \begin{bmatrix} v \\ r \end{bmatrix}$  $\lambda^{2} - (\gamma_{r} + N_{r}) \lambda - (\gamma_{r} N_{r} + u_{o} N_{r}) = 0$  $\lambda_{dr, approx} = -0.1008 \pm 0.9157c$   $\lambda_{dr} = -0.033 \pm 0.947c$ 

B 747

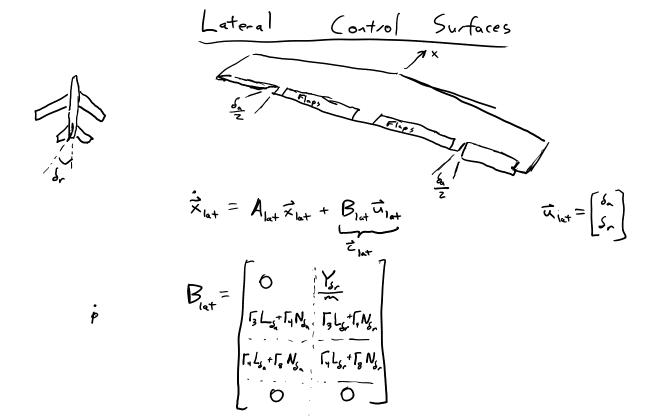


Table 7.1 Dimensional Control Derivatives

	X	Z	М
$\delta_e$	$C_{x_{\delta_e}^{-\frac{1}{2}}}\rho u_0^2 S$	$C_{z_{\delta_e}^{-1}}\rho u_0^2 S$	$C_{m_{\delta_c}^{-\frac{1}{2}}}\rho u_0^2 S\bar{c}$
$\delta_p$	$C_{x_{\delta_p}^{\frac{1}{2}}}\rho u_0^2 S$	$C_{z_{\delta_p}^{-1}}\rho u_0^2 S$	$C_{m_{\delta_{\rho}}} \frac{1}{2} \rho u_0^2 S \bar{c}$

	Y	L	N
$\delta_a$	$C_{y\delta_a}^{\frac{1}{2}}\rho u_0^2 S$	$C_{l_{\delta_a}}^{\frac{1}{2}}\rho u_0^2 Sb$	$C_{n_{\delta_a}}^{\frac{1}{2}}\rho u_0^2 Sb$
$\delta_r$	$C_{y\delta_r^{\frac{1}{2}}}\rho u_0^2 S$	$C_{l_{\delta_r}^2} \rho u_0^2 Sb$	$C_{n_{\delta_i}^{-1}}\rho u_0^2 Sb$

$$N_{F} = -l_{F}L_{F} = -l_{F}\frac{1}{2}\rho V_{F}^{2}S_{F}C_{LF}(\alpha_{F}, \delta_{r})$$

$$C_{n_{F}} = \frac{N_{F}}{\frac{1}{2}\rho V_{F}^{2}S_{b}} = -\frac{l_{F}S_{F}}{\frac{5}{6}}\left(\frac{V_{F}^{2}}{V^{2}}\right)C_{LF} = -V_{V}C_{LF}\left(\frac{V_{F}^{2}}{V^{2}}\right)$$

$$C_{n_{S}} = \frac{\lambda C_{n_{F}}}{\lambda \delta_{r}}\Big|_{0} = -V_{V}\left(\frac{V_{F}^{2}}{V^{2}}\right)\frac{\lambda C_{LF}}{\lambda \delta_{r}}\Big|_{0} = -\lambda V_{V}\left(\frac{V_{F}^{2}}{V^{2}}\right)$$

$$V_{S} = -\lambda V_{V}\left(\frac{V_{F}^{2}}{V^{2}}\right)\frac{\lambda C_{LF}}{\lambda \delta_{r}}\Big|_{0} = -\lambda V_{V}\left(\frac{V_{F}^{2}}{V^{2}}\right)$$

$$V_{S} = -\lambda V_{V}\left(\frac{V_{F}^{2}}{V^{2}}\right)\frac{\lambda C_{LF}}{\lambda \delta_{r}}\Big|_{0} = -\lambda V_{V}\left(\frac{V_{F}^{2}}{V^{2}}\right)$$

Ailerons

Lsa-Negative & Aileron reversal can occur due to

Non-Can be either if Non 70 this is called adverse your

Ys - usually small