$$\vec{p}_{E} = R_{B}^{E} \vec{V}_{B}^{E}$$

$$\vec{O} = T \vec{\omega}_{B}$$

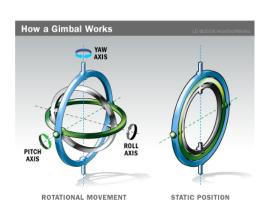
$$\vec{V}_{B}^{E} = \frac{\vec{f}_{B}}{m} - \vec{\omega}_{X} \vec{V}_{B}^{E}$$

$$\vec{\omega}_{B} = I_{B}^{-1} [\vec{G}_{B} - \vec{\omega}_{B} \times I_{B} \vec{\omega}_{B}]$$

$$Sin \Phi + \tan \Theta \qquad Cos \Phi + \tan \Theta$$

$$Cos \Phi \qquad -sin \Phi$$

$$T = \begin{bmatrix} 1 & \sin \phi & \tan \theta & \cos \phi & \tan \theta \\ 0 & \cos \phi & -\sin \phi \\ 0 & \sin \phi & \sec \theta & \cos \phi & \sec \theta \end{bmatrix}$$

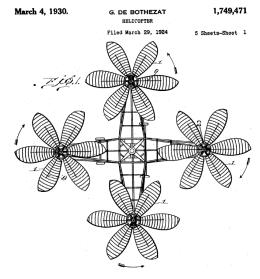


Multi copter

Quadrotor







$$\begin{array}{c}
\vec{f}_{B} = \begin{bmatrix} 0 \\ 0 \\ Z_{c} \end{bmatrix} \\
\vec{G} = \begin{bmatrix} L_{c} \\ M_{c} \\ N_{c} \end{bmatrix}
\end{array}$$

Since symmetric about 
$$\hat{l}^B - \hat{k}^B$$
 plane and  $\hat{l}^B \hat{f}^B$  plane
$$I_{xy} = I_{yz} = I_{xz} = 0$$

$$I_{y} = \begin{bmatrix} I_{x} & 0 & 0 \\ 0 & I_{y} & 0 \\ 0 & 0 & I_{z} \end{bmatrix}$$

$$\begin{pmatrix} \dot{x}_E \\ \dot{y}_E \\ \dot{z}_E \end{pmatrix} = \begin{pmatrix} c_{\theta}c_{\psi} & s_{\phi}s_{\theta}c_{\psi} - c_{\phi}s_{\psi} & c_{\phi}s_{\theta}c_{\psi} + s_{\phi}s_{\psi} \\ c_{\theta}s_{\psi} & s_{\phi}s_{\theta}s_{\psi} + c_{\phi}c_{\psi} & c_{\phi}s_{\theta}s_{\psi} - s_{\phi}c_{\psi} \\ -s_{\theta} & s_{\phi}c_{\theta} & c_{\phi}c_{\theta} \end{pmatrix} \begin{pmatrix} u^E \\ v^E \\ w^E \end{pmatrix}$$

$$\begin{pmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{pmatrix} = \begin{pmatrix} 1 & \sin \phi \tan \theta & \cos \phi \tan \theta \\ 0 & \cos \phi & -\sin \phi \\ 0 & \sin \phi \sec \theta & \cos \phi \sec \theta \end{pmatrix} \begin{pmatrix} p \\ q \\ r \end{pmatrix}$$

$$\begin{pmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{pmatrix} = \begin{pmatrix} 1 & \sin \phi \tan \theta & \cos \phi \tan \theta \\ 0 & \cos \phi & -\sin \phi \\ 0 & \sin \phi \sec \theta & \cos \phi \sec \theta \end{pmatrix} \begin{pmatrix} p \\ q \\ r \end{pmatrix}$$

$$\begin{pmatrix} \dot{u}^E \\ \dot{v}^E \\ \dot{v}^E \end{pmatrix} = \begin{pmatrix} rv^E - qw^E \\ pw^E - ru^E \\ qu^E - pv^E \end{pmatrix} + g \begin{pmatrix} -\sin \theta \\ \cos \theta \sin \phi \\ \cos \theta \cos \phi \end{pmatrix} + \frac{1}{m} \begin{pmatrix} X \\ Y \\ Z \end{pmatrix} + \frac{1}{m} \begin{pmatrix} 0 \\ 0 \\ Z_c \end{pmatrix}$$

$$\begin{pmatrix} \dot{I}_y - I_z \\ \dot{I}_z - I_x \\ I_y \\ \dot{I}_z - I_y \\ I_z \end{pmatrix} + \begin{pmatrix} \frac{1}{I_x} L \\ \frac{1}{I_y} M \\ \frac{1}{I_z} N \end{pmatrix} + \begin{pmatrix} \frac{1}{I_x} L_c \\ \frac{1}{I_y} M_c \\ \frac{1}{I_z} N_c \end{pmatrix}$$

Aerodynamic Forces and Moments

$$\vec{f} = -D \frac{\vec{v}}{|\vec{v}|}$$

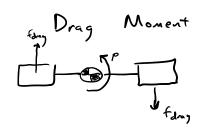


$$V_a = |\vec{V}|$$
 airspeed

 $D = \frac{1}{2} \rho C \rho A V_a^2 = \nu V_a^2$ 

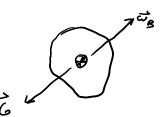
density (coefficient area of drag (shape)

$$a \overrightarrow{f}_{B} = \begin{bmatrix} \chi \\ \gamma \\ Z \end{bmatrix} = -\nu \sqrt{2} \frac{\overrightarrow{v}_{B}}{\sqrt{a}}$$
$$= -\nu \sqrt{2} \frac{\overrightarrow{v}_{B}}{\sqrt{a}}$$

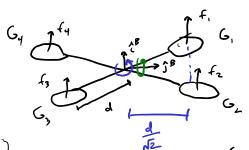


$${}^{\alpha}\vec{\mathsf{G}}_{g} = \begin{bmatrix} \mathsf{L} \\ \mathsf{M} \\ \mathsf{N} \end{bmatrix} = -\mathcal{M} \sqrt{p^{2} + q^{2} \cdot r^{2}} \begin{bmatrix} \mathsf{P} \\ \mathsf{q} \\ \mathsf{r} \end{bmatrix}$$

$$-p^2 sign(p) = -1pp$$



## + Monents



$$\vec{f}_{\beta} = \begin{bmatrix} 0 \\ 0 \\ -f_{1}-f_{2}-f_{3}-f_{4} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ Z_{c} \end{bmatrix}$$

$$\begin{array}{c}
G_{B} = \begin{bmatrix}
\frac{d}{dx} \left( -f_{1} - f_{2} + f_{3} + f_{4} \right) \\
\frac{d}{dx} \left( f_{1} - f_{2} - f_{3} + f_{4} \right) \\
G_{1} - G_{2} + G_{3} - G_{4}
\end{bmatrix} = \begin{bmatrix}
G_{1} \\
N_{1} \\
N_{2} \\
N_{3}
\end{bmatrix}$$

V5

$$\begin{bmatrix} f_1 \\ f_2 \\ f_3 \\ f_4 \end{bmatrix} = \begin{bmatrix} \vdots \\ f_N \\ N \end{bmatrix}$$

## Multirotor

Aerodymanic Efficient

Mechanical Control Complexity

Power System Complexity Turbine

Electric





Helicopter



