CSE320 Boolean Logic Practice Problems Solutions

1. Prove the following Boolean expression using algebra.

```
A. X'Y' + X'Y + XY = X' + Y
      = (X'Y+X'Y')+(X'Y+XY) replication of term X'Y
      = X'(Y + Y') + Y(X + X')
      = X' + Y
B. A'B + B'C' + AB + B'C = 1
      = (A'B+AB) + (B'C'+B'C)
      = B(A + A') + B'(C + C')
      = \mathbf{B} + \mathbf{B}'
      = 1
C. Y + X'Z + XY' = X + Y + Z
      = Y + X Y' + X' Z
      = \mathbf{Y}(1+\mathbf{X}) + \mathbf{X}\mathbf{Y'} + \mathbf{X'Z}
      = (\mathbf{Y} + \mathbf{X})(\mathbf{Y} + \mathbf{Y'}) + \mathbf{X'Z}
      = \mathbf{Y} + \mathbf{X} + \mathbf{X}'\mathbf{Z}
      = \mathbf{Y} + (\mathbf{X} + \mathbf{X}')(\mathbf{X} + \mathbf{Z})
      = X + Y + Z
D. X'Y' + Y'Z + XZ + XY + YZ' = X'Y' + XZ + YZ'
      = X'Y' + Y'Z(X + X') + XZ + XY + YZ'
      = X' Y' + X Y' Z + X' Y' Z + XZ + XY + Y Z'
      = X' Y' (1 + Z) + X Y' Z + XZ + XY + Y Z'
      = X'Y' + XZ(1 + Y') + XY + YZ'
      = X' Y' + XZ + XY (Z + Z') + Y Z'
      = X'Y' + XZ + XYZ + YZ'(1 + X)
      = X' Y' + XZ(1 + Y) + Y Z'
      = X'Y' + XZ + YZ'
E. AB' + A'C'D' + A'B'D + A'B'CD' = B' + A'C'D'
      = AB'(C+C')(D+D') + A'C'D'(B+B') + A'B'D(C+C') + A'B'CD'
      = AB'CD + AB'C'D + AB'CD' + AB'C'D' + A'BC'D' + A'B'C'D + A'B'CD + A'B'C'D + A'B'CD'
      = AB'CD + AB'C'D + AB'CD' + AB'C'D' + A'B'C'D + A'B'C'D + A'B'C'D' + A'B'C'D' + A'BC'D' +
        A'B'C'D'
      = B'(A+A')(C+C')(D+D') + A'C'D'(B+B')
      = B' + A'C'D'
      Alternate approach:
      AB' + A'C'D' + A'B'D + A'B'CD'
      = B' (A + A'C'D' + A'D + A'CD') + A'C'D'
      (replicate A'C'D') (A'C'D hides B')
      = B'(A + A'(C'D' + D + CD') + A'C'D'
      = B'(A + A'(D+D'(C'+C)) + A'C'D'
      = B'(A + A'(D+D'(1)) + A'C'D'
      = B'(A + A'(D+D')) + A'C'D'
      = B'(A + A'(1)) + A'C'D'
      = \mathbf{B'(A + A')} + \mathbf{A'C'D'}
      = B'(1) + A'C'D'
      = B' + A'C'D'
F. XZ + WY'Z'+W'YZ'+WX'Z' =
    XZ + WY'Z' + WXY' + W'XY + X'YZ'
      = XZ(W+W')(Y+Y') + WY'Z'(X+X') + W'YZ'(X+X') + WX'Z'(Y+Y')
      = XZ(W+W')(Y+Y'): WXYZ + W'XYZ + WXY'Z + W'XY'Z
         WY'Z'(X+X'): WXY'Z' + WX'Y'Z'
```

```
W'YZ'(X+X'): W'XYZ' + W'X'YZ'
                                   WX'Z'(Y+Y'): WX'YZ' + WX'Y'Z'
                          = WXYZ + W'XYZ + WXY'Z + W'XY'Z + WXY'Z' + W'XYZ' + WX'YZ' + WX'YZ
                          = *XZ(W+W')(Y+Y'): WXYZ + W'XYZ + WXY'Z + W'XY'Z
                                *WY'Z'(X+X'): WXY'Z' + WX'Y'Z'
                                  WXY'(Z+Z'): WXY'Z + WXY'Z'
                                   W'XY(Z+Z'): W'XYZ + W'XYZ'
                                  X'YZ'(W+W'): WX'YZ' + W'X'YZ'
                          = XZ(W+W')(Y+Y') + WY'Z'(X+X') + WXY'(Z+Z') + W'XY(Z+Z') + X'YZ'(W+W')
G. CD + AB' + AC + A'C' + A'B + C'D' =
                 (A' + B' + C + D')(A + B + C' + D)
                          = CD(A+A')(B+B') + C'D'(A+A')(B+B') + AB'(C+C')(D+D') + A'B(C+C')(D+D') + AC(B+B')(D+D') + AC(B+D')(D+D') + AC(B+D')(D+D')(D+D') + AC(B+D')(D+D')(D+D') + AC(B+D')(D+D')(D+D') + AC(B+D')(D+D')(D+D') + AC(B+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(D+D')(
                                  A'C'(B+B')(D+D')
                          = CD(A+A')(B+B'): ABCD + A'BCD + AB'CD + A'B'CD
                                  C'D'(A+A')(B+B'): ABC'D' + A'BC'D' + AB'C'D' + A'B'C'D'
                                  AB'(C+C')(D+D'): AB'CD + AB'C'D + AB'CD' + AB'C'D'
                                  A'B(C+C')(D+D'): A'BCD + A'BC'D + A'BCD' + A'BC'D'
                                  AC(B+B')(D+D'): ABCD + AB'CD + ABCD' + AB'CD'
                                  A'C'(B+B')(D+D'): A'BC'D + A'B'C'D + A'BC'D' + A'B'C'D'
                          = ABCD + A'BCD + AB'CD + ABC'D + ABCD' + A'B'CD + AB'C'D + ABC'D' + A'BCD' + AB'CD'
                                   + A'BCD' + A'BC'D + AB'C'D' + A'B'C'D + A'BC'D'
                          = *A'B(C+C')(D+D'): A'BCD + A'BC'D + A'BCD' + A'BC'D'
                                   *A'C'(B+B')(D+D'): A'BC'D + A'B'C'D + A'BC'D' + A'B'C'D'
                                  A'D(B+B')(C+C'): A'BCD + A'B'CD + A'BC'D + AB'C'D
                                  *AB'(C+C')(D+D'): AB'CD + AB'C'D + AB'CD' + AB'C'D'
                                  B'C'(A+A')(D+D'): AB'C'D + A'B'C'D + AB'C'D' + A'B'C'D'
                                  B'D(A+A')(C+C'): AB'CD + A'B'CD + AB'C'D + A'B'C'D
                                  *AC(B+B')(D+D'): ABCD + AB'CD + ABCD' + AB'CD'
                                  BC(A+A')(D+D'): ABCD + A'BCD + ABCD' + A'BCD'
                                   *CD(A+A')(B+B'): ABCD + A'BCD + AB'CD + A'B'CD
                                  AD'(B+B')(C+C'): ABCD' + AB'CD' + ABC'D' + AB'C'D'
                                  BD'(A+A')(C+C'): ABCD' + A'BCD' + ABC'D' + A'BC'D'
                                   *C'D'(A+A')(B+B'): ABC'D' + A'BC'D' AB'C'D' + A'B'C'D'
                          =A'B(C+C')(D+D')+A'C'(B+B')(D+D')+A'D(B+B')(C+C')+AB'(C+C')(D+D')+B'C'(A+A')(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D+D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')+A'D'(D')
                                  B'D(A+A')(C+C') + AC(B+B')(D+D') + BC(A+A')(D+D') + CD(A+A')(B+B') + AD'(B+B')(C+C') + AD'(B+B')(C+C') + AD'(B+B')(D+D') + BC'(A+A')(D+D') + CD(A+A')(B+B') + AD'(B+B')(D+D') + CD(A+A')(B+B') + CD(A')(B+B') + CD(A')(B') + CD(A') + CD(A')(B') + CD(A') + CD(A')(B') + CD(A') + CD(A')(B') + CD(A') + CD(A')(B') + CD(A')(B') + CD(A')(B') + CD(A')(B') + CD(A')(B') + CD(A')(B') + CD(A') + CD(A')(B') + CD(A') + CD(A') + CD(A') + CD(A') + CD(A') + 
                                  BD'(A+A')(C+C') + C'D'(A+A')(B+B')
                          = A'B + A'C' + A'D + AB' + B'C' + B'D + AC + BC + CD + AD' + BD' + C'D'
                          = AA' + A'B + A'C' + A'D + AB' + BB' + B'C' + B'D + AC + BC + CC' + CD + AD' + BD' + C'D' + DD'
                          = (A' + B' + C + D') (A + B + C' + D)
```

Note that the * denotes lines which are the same as in step 2. All other terms are repeats. Also, note that the only term missing is A'B'CD' this implies that the truth table has only 1 zero (0010). The function can be represented as $\prod M(2)$.

2. Simplify the following Boolean expressions to the minimum number of literals (total number of appearances of all variables, eg. AB+C' has 3 literals).

A.
$$ABC + ABC' + A'B$$
 = **B**
B. $(A + B)'(A' + B')$ = **A'B'**
C. $A'BC + AC$ = **AC** + **BC**

- D. BC + B(AD + AD') = B(C + A)
- E. (A + B' + AB')(AB + A'C + BC) = AB + A'B'C
- 3. Reduce the following expressions to the indicated number of literals (total number of appearances of all variables, eg. AB+C' has 3 literals).
 - A. X'Y' + XYZ + X'Y to 3 literals
 - = X' + XYZ = (X' + XY)(X' + Z)
 - = (X' + X)(X' + Y)(X' + Z) = (X' + Y)(X' + Z)
 - = X' + YZ
 - B. $X + Y(Z + (X + Z)^2)$ to 2 literals
 - = X + Y(Z + X'Z') = X + YZ + X'YZ' = X + (YZ + X')(YZ + YZ')
 - = X + Y(X' + YZ) = X + X'Y + YZ = (X + X')(X + Y) + YZ
 - = X + Y + YZ
 - = X + Y
 - C. W'X(Z' + Y'Z) + X(W + W'YZ) to 1 literals
 - = W'XZ' + W'XY'Z + WX + W'XYZ = WX + W'XZ' + W'XZ
 - $= \mathbf{W}\mathbf{X} + \mathbf{W'X} = \mathbf{X}$
 - D. ((A + B) + A'B')(C'D' + CD) + A'C' to 4 literals
 - = ABC'D' + ABCD + A'B'C'D' + A'B'CD + A' + C'
 - = A'(1 + B'C'D' + B'CD) + C'(1 + ABD') + ABCD
 - = A'(1 + BCD) + C' + ABCD = A' + A'BCD + C' + ABCD
 - = A' + C' + (A+A')BCD
 - = A' + C'(1 + BD) + BCD = A' + C' + BC'D + BCD
 - = A' + C' + (C' + C)(BD)
 - = A' + C' + BD
- 4. Find the complement of the following expressions
 - A. AB' + A'B = (A' + B)(A + B')
 - B. (V'W + X)Y + Z' = ((V+W')X'+Y')Z

- C. WX(Y'Z+YZ') + W'X'(Y'+Z)(Y+Z')= [W'+X'+(Y+Z')(Y'+Z)][W+X+YZ'+Y'Z]
- D. (A + B' + C)(A'B' + C)(A + B'C') = A'BC' + (A + B)C' + A'(B + C)
- 5. Obtain the truth tables for the following expressions
 - $A. \quad \mathbf{Z} = (XY + Z)(Y + XZ)$ Z X Y \mathbf{Z}

B. Z = (A' + B)(B' + C)Y Z \mathbf{Z} X

6. Convert the following truth table to switching expression (Boolean Algebra), and simplify the expression as much as possible

X	Y	Z	E
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

G = Y

 $\mathbf{E} = \mathbf{X} + \mathbf{Y'Z}$

7. Using DeMorgan's theorem, express the function

$$F = ABC + A'C' + A'B'$$

- a. with only OR and complement operators
- b. with only AND and complement operators

Solution:

a.
$$F = (A' + B' + C')' + (A+C)' + (A+B)' = (A'+B'+C')' + (A+(B'+C')')'$$

b.
$$F = (ABC)'(A'C')'(A'B')'$$
 or $[(ABC)'(A'(BC)')']'$

Minterms & Maxterms

8. Write the truth table for the following functions, and express the functions as sum-of-minterms and product-of-maxterms

c.
$$(XY + Z)(Y + XZ)$$

a.
$$(A' + B)(B' + C)$$

b.
$$WXY' + WXZ' + WXZ + YZ'$$

Solution:

X	Y	Z	a
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

sum-of-minterms: X'YZ + XY'Z + XYZ' + XYZproduct-of-maxterms: (X + Y + Z)(X + Y + Z')

$$(X + Y' + Z)(X' + Y + Z)$$

b.

Α	В	C	b
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

sum-of-minterms: A'B'C' + A'B'C + A'BC + ABCproduct-of-maxterms: (A + B' + C) (A' + B + C)

$$(A' + B + C')(A' + B' + C)$$

W	X	Y	Z	С
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

 $\begin{array}{l} \text{sum-of-minterms: } W'X'YZ' + W'XYZ' + WX'YZ' + \overline{WXY'Z' + WXY'Z' + WXY'Z' + WXYZ'} \\ \text{product-of-maxterms:} (W+X+Y+Z) \ (W+X+Y+Z') \ (W+X+Z') \ (W$

9. Convert the following expressions into sum-of-products (minterms) and product-of-sums (maxterms)

d.
$$(AB + C)(B + C^{2}D)$$

= $AB + ABC^{2}D + BC + CC^{2}D = AB + ABC^{2}D + BC = AB(1+C^{2}D) + BC$
= $AB + BC$ (SOP)
= $B(A+C) = (B+B)(A+C)$ (POS)

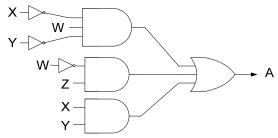
e.
$$X' + X(X + Y')(Y + Z')$$

= $(X'+X)(X' + (X + Y'))(Y+Z') = (X' + X + Y')(X' + Y + Z')$
= $X' + Y + Z'$ (SOP & POS)

f.
$$(A + BC' + CD)(B' + EF)$$

= $(A + BC' + CD)(B'+E)(B'+F)$
= $(A + B + C)(A + B + D)(A + C'+D)(B'+E)(B'+F)$ (POS)
= $A(B'+EF) + BC'(B'+EF) + CD(B'+EF)$
= $AB' + AEF + BC'EF + B'CD + CDEF$ (SOP)

10. Convert the following gate diagrams into (1) switching expression, (2) truth table, (3) sum-of-products, and (4) product-of-sums

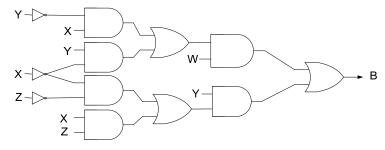


- (1) switching expression: WX'Y' + W'Z + XY
- (2)

W	X	Y	Z	Α
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1

0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

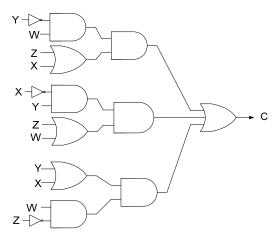
- (3) sum-of-products: W'X'YZ+W'XYZ+W'XYZ+W'XYZ'+ W'XYZ+WX'Y'Z'+ WXYZ'+ WXYZ'+ WXYZ
- (4) product-of-sums: (W+X+Y+Z)(W+X+Y'+Z)(W+X'+Y+Z)(W'+X+Y'+Z)(W'+X+Y'+Z')(W'+X'+Y+Z)(W'+X'+Y+Z')



- (1) switching expression: W(XY'+X'Y) + Y(XZ+X'Z')
- (2)

W	X	Y	Z	В
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

- (3) sum-of-products: W'X'YZ'+ W'XYZ+WX'YZ'+ WXY'Z'+WXY'Z'+WXYZ
- (4) product-of-sums: (W+X+Y+Z)(W+X+Y+Z')(W+X+Y'+Z')(W+X'+Y+Z)(W+X'+Y+Z')(W+X'+Y'+Z)(W'+X+Y+Z)(W'+X+Y+Z')(W'+X'+Y'+Z)



(1) switching expression: WY'(X+Z) + X'Y(W+Z) + WZ'(X+Y)

(2)

W	X	Y	Z	С
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

- (3) sum-of-products: W'X'YZ+ WX'YZ+WX'YZ'+ WXY'Z+ WXYZ'+WXYZ'+WXYZ
- (4) product-of-sums: (W+X+Y+Z)(W+X+Y+Z')(W+X+Y'+Z)(W+X'+Y+Z) (W+X'+Y+Z')(W+X'+Y'+Z)(W+X'+Y'+Z')(W'+X+Y+Z)(W'+X'+Y'+Z')

11. Simplify/write the following expressions in (1) sum-of-products and (2) product-of-sums forms

- g. AC' + B'D + A'CD + ABCD
- = AC' + B'D(1 + AC) + A'CD(B+B')A + ABCD
- = AC' + B'D + AB'CD + A'BCD + A'B'CD + ABCD
- = AC' + B'D + CD(AB' + A'B + A'B' + AB)
- = CD + AC' + B'D (SOP)
- = (C+D')(A'+D')(A'+B+C') (POS)
- h. (A' + B + D')(A + B' + C')(A' + B + D')(B + C' + D')
- = A'C'+B'D'+AD' (SOP)
- = (C'+D')(A'+D')(A+B'+C') (POS)
- i. (A' + B' + D)(A' + D')(A + B + D')(A + B' + C + D)
- $= A'BD+B'D'+A'BC \quad or \quad A'BD+B'D'+A'CD' \quad (SOP)$
- = (A'+B')(B+D')(B'+C+D) (POS)
- j. $F(A,B,C,D) = \sum m(2,3,5,7,8,10,12,13)$
- = A'B'CD'+ A'B'CD+ A'BC'D + A'BCD + AB'C'D'+ AB'CD'+ ABC'D'+ ABC'D
- = AB'D'+ABC'+A'BD+A'B'C+B'CD' (there are multiple answers) (SOP)
- = (A+B'+D)(B+C+D')(A+B+C)(A'+C'+D')(A'+B'+C') (there are multiple answers) (POS)

k.
$$F(W,X,Y,Z) = \prod M(2,10,13)$$

= Y'Z' + W'X + X'Z + XY (SOP)
= (W+X+Y'+Z)(X'+Y+Z') (POS)

12. For the Boolean functions given in the following truth table:

X	Y	Z	Е	F	G
0	0	0	1	0	1
0	0	1	1	0	1
0	1	0	1	1	1
0	1	1	0	1	0
1	0	0	0	0	1
1	0	1	1	0	0
1	1	0	0	1	1
1	1	1	0	1	0

1. List the minterms and maxterms of each function

m. List the maxterms of E', F', and G'

E' = $\prod M$ (0,1,2,5) E' = $\sum m$ (3,4,6,7) G' = $\prod M$ (0,1,2,4,6) F' = $\sum m$ (0,1,4,5) G' = $\sum m$ (3,5,7)

n. Write the truth tables for E + F and EF

X	Y	Z	Е	F	E+F	EF
0	0	0	1	0	1	0
0	0	1	1	0	1	0
0	1	0	1	1	1	1
0	1	1	0	1	1	0
1	0	0	0	0	0	0
1	0	1	1	0	1	0
1	1	0	0	1	1	0
1	1	1	0	1	1	0

o. List the minterms of E + F and EF

E+F =
$$\sum m(0,1,2,3,5,6,7)$$
 =X'Y'Z+X'Y'Z+X'YZ'+X'YZ+XY'Z+XYZ'+XYZ
EF = $\sum m(2)$ = X'YZ'

p. Express E, F and G in sum-of-products

$$E = X'Y'Z' + X'Y'Z + X'YZ' + XY'Z$$

$$F = X'YZ' + X'YZ + XYZ' + XYZ$$

$$G = X'Y'Z' + X'Y'Z + X'YZ' + XY'Z' + XYZ'$$

q. Express E, F and G in products-of-sums

$$E = (X+Y'+Z')(X'+Y+Z)(X'+Y'+Z)(X'+Y'+Z')$$

$$F = (X+Y+Z)(X+Y+Z')(X'+Y+Z)(X'+Y+Z')$$

$$G = (X+Y'+Z')(X'+Y+Z')(X'+Y'+Z')$$

r. Simplify E, F and G to expressions with a minimum number of literals (sum-of-products).

$$\mathbf{E} = \mathbf{X'Y'Z'} + \mathbf{X'Y'Z} + \mathbf{X'YZ'} + \mathbf{XY'Z}$$

$$= X'Z'(Y'+Y) + Y'Z(X+X')$$

$$= Y'Z + X'Z'$$

$$F = X'YZ' + X'YZ + XYZ' + XYZ$$

$$= \mathbf{YZ'(X+X')} + \mathbf{YZ(X'+X)}$$

$$= \mathbf{Y}(\mathbf{Z'} + \mathbf{Z}) = \mathbf{Y}$$

$$=X'Y'(Z+Z')+Z'(X'Y+XY'+XY+X'Y')$$
 duplicate $X'Y'Z'$

$$= X'Y' + Z'$$