

Code optimisations

course “Essentials of computing systems”

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writing efficient code

- Writing an efficient program in a given high-level programming language requires several types of skills.
- One must select the adequate algorithms and data structures.
- Source code must be in such a condition that the compiler can effectively produce code that runs fast or that occupies the minimum space.
- Speed and size are the traditional criteria of optimisation addressed by compilers.
- Energy consumption is gaining importance.
- It is relevant to comprehend how compilers try to apply some type of [code optimisation](#) to the programs.
- [Programmers must know how to make programs more amenable for compilers to generate \(more\) efficient code.](#)

readability vs. performance

- There are differences between a normal algorithm and a more efficient one.
- The former can be programmed in a matter of minutes, while the latter requires more effort to implement and refine.
- Many low-level optimisations tend to reduce the readability and the modularity of the program, making harder its modification.
- For code whose performance is relevant, applying optimisations is worthwhile.
- One should maintain some level of readability in the code.
- A compiler takes a valid program written in the source language code and generates a behaviourally-equivalent machine-level program.
- Compilers make use of sophisticated mechanisms to generate code that can be optimised according to different metrics.

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level of optimisations

- Most compilers employ advanced techniques to determine what values are computed in a program and how they are used.
- The compilers can exploit opportunities:
 - ① to simplify expressions,
 - ② to use a single computation in several different places,
 - ③ to reduce the number of times a given computation must be performed.
- Compilers allow programmers to control the level of optimisations.
- For example, gcc can be used with the option `-O` to specify which type of optimisations to apply.

compilers are conservative

- Compilers must only apply safe optimisations to a program.
- The resulting program must have the same external behaviour as an unoptimised version for all possible paths the program may take.
- A compiler is expected to be conservative in applying optimisations: whenever in doubt, it does not apply them.
- The compiler operates in a constrained context:
 - ① It must not modify the behaviour of the program under any possible condition.
 - ② The compiler has a limited and localised view of the program, so broader optimisations are not applied.
 - ③ The compilation process must be fast enough, so marginal gains are not appreciated if the compiler takes much longer.

optimisation blockers

- Compilers usually have problems in dealing with **optimisation blockers**.
- Optimisation blockers can greatly limit the opportunities for a compiler to generate optimised code.
- Often, the optimisation blockers are dependent on the execution environment.

```
int pr1(int *x, int *y) {  
    *x += *y;  
    *x += *y;  
}
```

6 memory accesses

```
int pr2(int *x, int *y) {  
    *x += 2* *y;  
}
```

3 memory accesses

-
- Both programs add twice the value stored at the location designated by pointer *y* to that designated by pointer *x*.

optimisation blockers

- It seems that a compiler when handling procedure pr1 could generate more efficient code based on the computations performed by the equivalent pr2.
- This approach cannot be applied when x and y are equal.

| | | |
|-----|------------------------|--------------------------------------|
| pr1 | <code>*x += *x;</code> | <code>/* double value at x */</code> |
| | <code>*x += *x;</code> | <code>/* double value at x */</code> |

| | | |
|-----|---------------------------|--------------------------------------|
| pr2 | <code>*x += 2* *x;</code> | <code>/* triple value at x */</code> |
|-----|---------------------------|--------------------------------------|

- The compiler cannot assume that arguments x and y are not equal.
- The situation where two pointers may designate the same memory location is called as [memory aliasing](#).

optimisation blockers

```
int a, *b;  
...  
a    = 5;  
*b   = 10;  
...  
a    = a+3;
```

optimisation blockers

- Another optimisation blocker may occur when a function has side effects.
- A function (or expression) has a **side effect**, if it alters the values of some variables outside its local context.
- The function has an observable effect besides returning a value to the calling procedure.

```
int func1(int x) {  
    return (f(x)+f(x));  
}
```

```
int func2(int x) {  
    return (2*f(x));  
}
```

-
- Both versions of the function appear to have the same behaviour.

optimisation blockers

```
int f(int p) {  
    return (p+counter++);  
}
```

- counter is a global integer variable.
- The expression `p+counter++`, calculates the value `p+counter` and afterwards increments the value of `counter` by one.
- If `counter` is equal to 0, calling:
 - `func1(5)` returns 11 ($5+6$)
 - `func2(5)` returns 10 (2×5)
- The value of `counter` is also different in both cases: 2 after calling `func1` and 1 after `func2`.

optimisation blockers

```
void lower2upper(char *s) {  
    int i;  
    for (i=0; i<strlen(s); i++)  
        if (s[i]>='a' && s[i]<='z')  
            s[i] -= ('a' - 'A');  
}
```

```
void lower2upper(char *s) {  
    int i, length=strlen(s);  
    for (i=0; i<length; i++)  
        if (s[i]>='a' && s[i]<='z')  
            s[i] -= ('a' - 'A');  
}
```

- Compilers tend to keep the call to `strlen` inside the loop, because it can have side effects.
- The loop body may change the string and its size.
- Compilers tend to treat procedures as black boxes that cannot be analysed.
- Compilers assume the worst case and the function call remains intact.

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types of optimisations

- Machine-independent optimisations improve the target code, but ignore any properties at the machine level.
- They include choosing the best (i.e., the fastest) algorithm for the problem at hand → **not addressed in this course**.
- Other optimisations that fit in this group are:
 - 1 code motion;
 - 2 elimination of unnecessary accesses to memory;
 - 3 loop unrolling;
 - 4 reduction of the number of procedure calls.

code motion

- Loops are good candidates for improvements.
 - The most typical cases of code motion consist of statements in a loop that can be moved outside its body, without affecting its semantics.
 - Moving statements from the inside to the outside of the loop obviously reduces the execution time of the program.
-

```
do {  
    x=y+z;  
    a[i]=i+x*x;  
    i++;  
} while (i<n);
```

```
x=y+z;  
int const j=x*x;  
do {  
    a[i]=i+j;  
    i++;  
} while (i<n);
```

code motion

```
above = val[(i-1)*n+j];  
below = val[(i+1)*n+j];  
left  = val[i*n+j-1];  
right = val[i*n+j+1];  
sum    = above + below + left + right;
```

code motion

| | |
|-------------------------------------|-------------------|
| above = val[(i-1)*n+j]; | $(i * n) - n + j$ |
| below = val[(i+1)*n+j]; | $(i * n) + n + j$ |
| left = val[i*n+j-1]; | $(i * n) + j - 1$ |
| right = val[i*n+j+1]; | $(i * n) + j + 1$ |
| sum = above + below + left + right; | |

code motion

```
long inj = i*n + j;  
above = val[inj-n];  
below = val[inj+n];  
left  = val[inj-1];  
right = val[inj+1];  
sum   = above + below + left + right;
```

$$(i * n) - n + j$$

$$(i * n) + n + j$$

$$(i * n) + j - 1$$

$$(i * n) + j + 1$$

code motion


- Similar transformations can be applied to WHILE-DO loops, but in some cases the result is more complex.
- WHILE-DO loops execute zero or more times, while DO-WHILE loops execute at least once.

```
while (i<n) {  
    x=y+z;  
    a[i]=i+x*x;  
    i++;  
}
```

```
if (i<n) {  
    x=y+z;  
    int const j=x*x;  
    do {  
        a[i]=i+j;  
        i++;  
    } while (i<n);  
}
```

code motion

- Compilers try to transform WHILE-DO and FOR loops in equivalent DO-WHILE loops, to avoid the IF-THEN statement.

| | |
|---|------------------|
| for (i=0; i<100; i++) { | |
| ... | |
| } | i=0; |
| | do { |
|  | ... |
| i=0; | i++; |
| while (i<100) { | } while (i<100); |
| ... | |
| i++; | |
| } | |

- It is guaranteed that the FOR loop executes at least once.
- The assembly code for DO-WHILE loops, in general, can be made faster than equivalent FOR and WHILE-DO loops.

elimination of unnecessary accesses to memory

- Accesses to main memory are also obvious candidates to optimise the performance of a program.

```
int addAll (int *a, int *v)
{  int i;
   *v=0;
   for (i=0; i<100; i++)
       *v += a[i];
}
```

3 memory accesses per iteration

```
int addAll (int *a, int *v)
{  int i;
   int acc=0;
   for (i=0; i<100; i++)
       acc += a[i];
   *v=acc;
}
```

1 memory access per iteration

loop unrolling

- **Loop unrolling** aims reducing the number of loop iterations, by increasing the number of elements computed on each iteration.
- Each loop iteration incurs in some non-effective computations, related to the control of the loop.

```
i=0;  
do {  
    arr[i]=0;  
    i++;  
} while (i<120);
```

```
i=0;  
do {  
    arr[i]=0;  
    arr[i+1]=0;  
    arr[i+2]=0;  
    arr[i+3]=0;  
    i+=4;  
} while (i<120);
```

```
arr[0]=0;  
arr[1]=0;  
arr[2]=0;  
arr[3]=0;  
...  
...  
arr[118]=0;  
arr[119]=0;
```

- Loop unrolling constitutes a space-time tradeoff.

loop unrolling

```
    movl $0, %eax  
.lbl:
```

```
    movl $0, arr(,%eax,4)
```

```
    incl %eax  
    cmpl $120, %eax  
    jle .lbl
```

481 (1 + 120×4) instructions

```
    movl $0, %eax  
.lbl:
```

```
    movl $0, arr (,%eax,4)  
    movl $0, arr+ 4(,%eax,4)  
    movl $0, arr+ 8(,%eax,4)  
    movl $0, arr+12(,%eax,4)
```

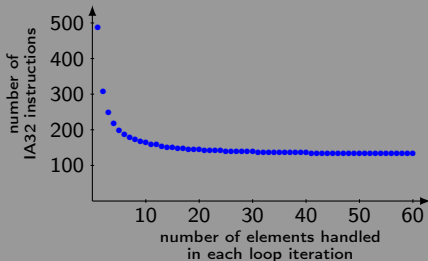
```
    addl $4, %eax  
    cmpl $120, %eax  
    jle .lbl
```

211 (1 + 30×7) instructions

- If all instructions take the same time to execute (not the case), the reduction in time is around 56%.

loop unrolling

- For an array with n positions and a block of $k \leq \frac{n}{2}$ positions manipulated in each iteration, the total number of instructions is $1 + (3+k) \times \lfloor \frac{n}{k} \rfloor + (n \bmod k)$.
- If n is not a multiple of k , additional instructions need to be put at the beginning or the end of the loop.
- If $n = 21$ and $k = 4$, there are five iterations with blocks of four elements, plus one instruction outside the loop.
- The performance improves whenever the block has more elements, but the code also occupies more space.



reduction of the number of procedure calls

- Procedure calls imply a great overhead and also tend to block many possible program optimisations.
- The idea of replacing a procedure call by the body of the called procedure is called **inline expansion**.
- It reduces time, at the cost of increasing the space usage.
- An inlined procedure runs faster than the normal procedure, as the calling overheads are avoided.
- However, code gets larger.
- Maintenance of the procedure gets harder, because when the body of the procedure needs to be changed, one must update it in several places.
- Inline expansion is adequate for small functions.

reduction of the number of procedure calls

```
int isEven (int num) {  
    return !(num & 1);  
}
```

```
if (isEven (number))
```

```
if (!(number & 1))
```

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different instructions

- Machine-dependent optimisations depend on the specific processor that is being considered.
- Optimisations that work in a given processor are not necessarily effective in a different one.
- These optimisations are related to the use of instructions that are faster or occupy less space in memory.
- When a given high-level statement is supported by different machine-level alternatives, one can use the best one, according to the preferred criterion.
- In IA32, assigning the value 0 to a register can be done with the following alternatives:

more space

```
movl $0, %eax
```

less space

```
xorl %eax, %eax
```

multiplication by a constant

- Another example occurs with multiplications, which in some processors take longer to execute than additions and shifts.
- **Compilers transform a multiplication involving a variable and a constant in a series of additions and shifts.**

| | |
|------------------|------------------------------|
| $y = 8 \cdot a;$ | <code>movl %eax, %ebx</code> |
| | <code>sall \$3, %ebx</code> |

- Things are not that simple when the constant is not a power of two.

| | |
|-------------------|-------------------------------------|
| $y = 37 \cdot a;$ | <code>imull \$37, %eax, %ebx</code> |
|-------------------|-------------------------------------|

- Since $37 = 32 + 4 + 1$, calculating $37 \cdot a = 32 \cdot a + 4 \cdot a + a$.

| | |
|------------------------------|---|
| <code>movl %eax, %ecx</code> | $ecx = a$ |
| <code>movl %ecx, %ebx</code> | $ebx = a$ |
| <code>sall \$2, %ecx</code> | $ecx = 4 \cdot a$ |
| <code>addl %ecx, %ebx</code> | $ebx = a + 4 \cdot a = 5 \cdot a$ |
| <code>sall \$3, %ecx</code> | $ecx = 8 \cdot 4 \cdot a = 32 \cdot a$ |
| <code>addl %ecx, %ebx</code> | $ebx = 5 \cdot a + 32 \cdot a = 37 \cdot a$ |

addresses

- The efficient computation of memory addresses is another machine-dependent optimisation.

```
arr[i]=0;
```

- If `i` is in `ecx` and the address array `arr` is in `ebx`, we have two alternatives for the assembly code:

slower

```
movl %ecx, %edx  
sall $2, %edx  
addl %edx, %ebx  
movl $0, (%ebx)
```

faster

```
movl $0, (%ebx,%ecx,4)
```


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good locality

- A program that exhibits good locality is very likely to execute faster than one that does not.
- Good locality is possible if a program refers data items that are near other recently referenced data items or that were recently referenced themselves.
- This situation may have a great impact on the performance of the program, because the hit rate of the cache gets higher.
- **Programmers must understand the principle of locality to positively exploit it.**
- This principle is present in all levels of modern computer systems.
- For example, web browsers explore temporal locality by locally caching recently referenced documents.

good locality

```
int addAll (int *arr) {  
    int i, acc=0;  
    for (i=0; i<100; i++)  
        acc += arr[i];  
    return (acc);  
}
```

- This procedure has a good temporal locality with respect to local variables `i` and `acc`.
- The elements of array `arr` are accessed one after the other.
- The procedure has good spatial locality with respect to array `arr`.
- Overall, [the `addAll` procedure exhibits good locality](#).
- It has a stride-1 reference pattern, as it accesses each element of the array sequentially.

stride

- The stride of an array is the number of locations in memory between successive array elements.
- It is measured in bytes or in units of the size of the array's elements.
- As the stride increases, the spatial locality decreases, since two element arrays consecutively accessed are more distant.

stride

stride 1 unit

```
for (i=0; i<100; i++)
    for (j=0; j<100; j++)
        acc += arr[i][j];
```

stride 100 units

```
for (i=0; i<100; i++)
    for (j=0; j<100; j++)
        acc += arr[j][i];
```

| | | |
|--------|----------|--------|
| 1 | [0][0] | 1 |
| 2 | [0][1] | 101 |
| 3 | [0][2] | 201 |
| ... | | ... |
| 99 | [0][98] | 9801 |
| 100 | [0][99] | 9901 |
| 101 | [1][0] | 2 |
| 102 | [1][1] | 102 |
| ... | | ... |
| 200 | [1][99] | 9902 |
| 201 | [2][0] | 3 |
| ... | | ... |
| 10 000 | [99][99] | 10 000 |