

Data Structures and Algorithms

Shikha Mehrotra

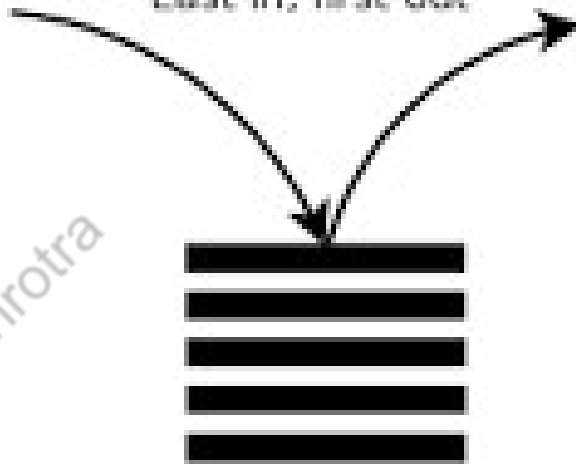
The Queue



Shikha Mehrotra

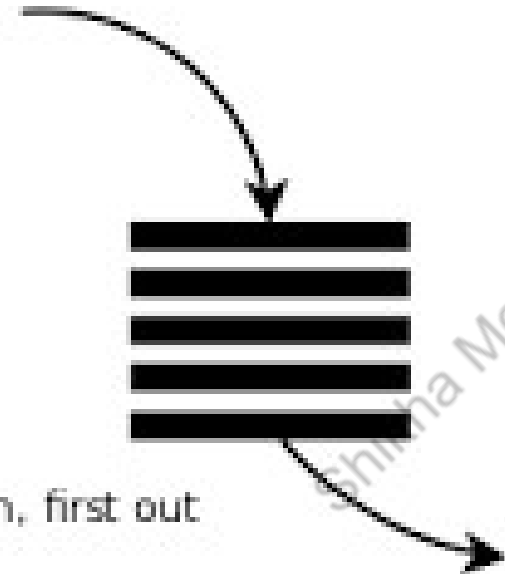
Stack:

Last in, first out



Queue:

First in, first out

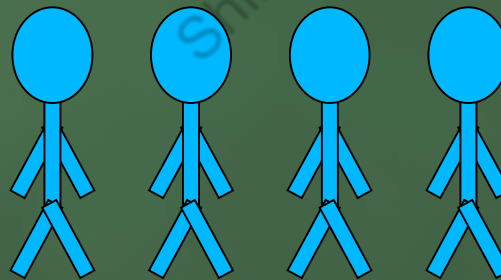


The Queue ADT

A list of collection with the restriction that insertion can be performed at one end (rear) and deletion can be performed at other end.

• The Queue Operations

- A queue is like a line of people waiting for a bank teller. The queue has a front and a rear.



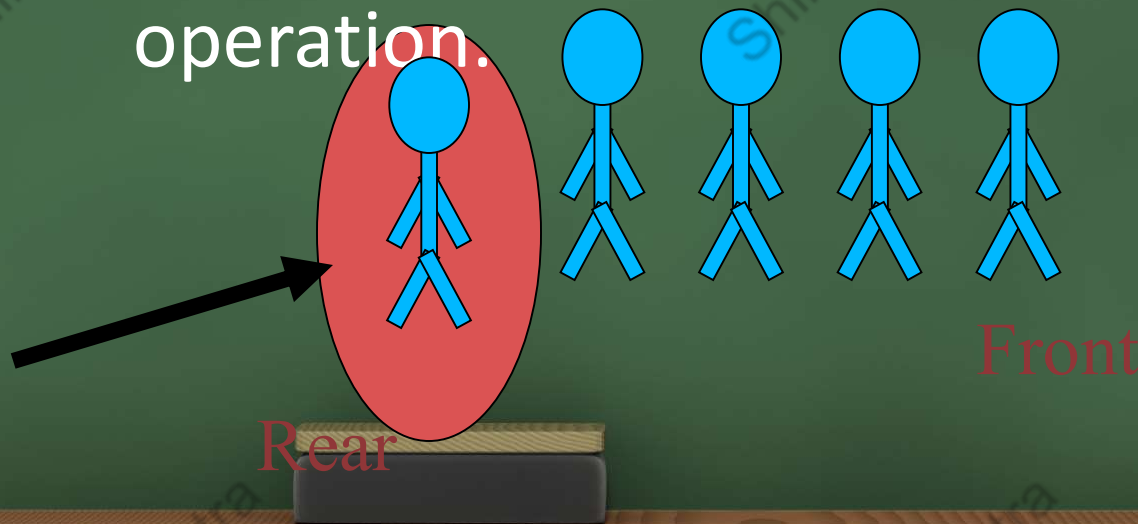
Front

Rear



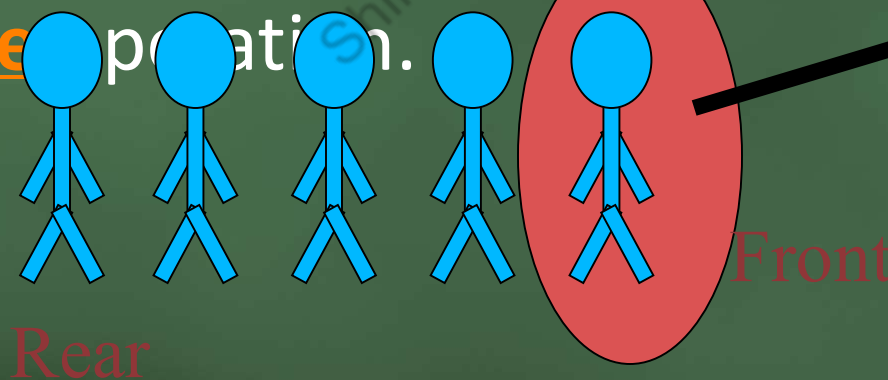
• The Queue Operations

- New people must enter the queue at the rear. The C++ queue class calls this a **push**, although it is usually called an **enqueue** operation.



• The Queue Operations

- When an item is taken from the queue, it always comes from the front. The C++ queue calls this a pop, although it is usually called a dequeue operation.



• Queue ADT

AbstractDataType queue {
 instances

 ordered list of elements; one end is the front; the other is the rear;

operations

 IsEmpty(): Return true if queue is empty, return false otherwise

 size(): Return the number of elements in the queue

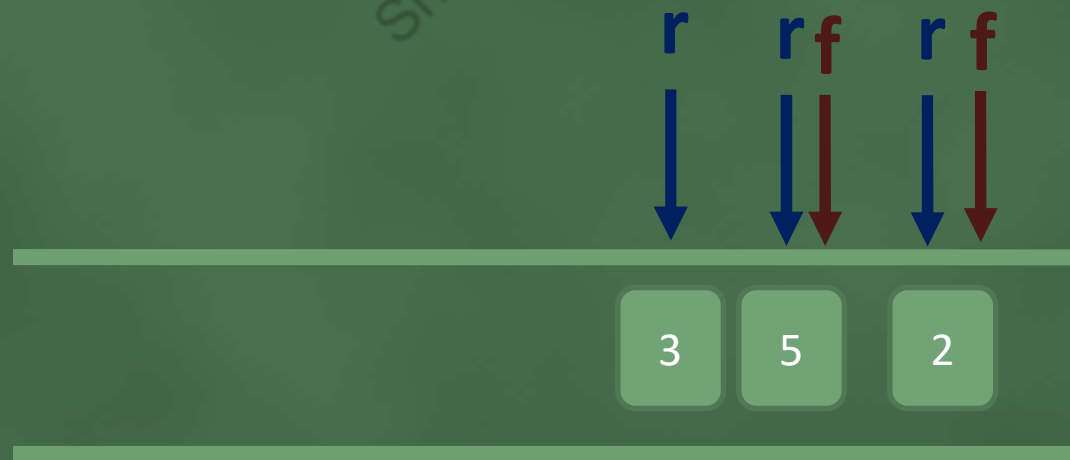
 front(): Return the front element of queue

dequeue(): Remove an element from the queue

enqueue(x): Add element x to the queue

•Queue





Enqueue(2)
Enqueue(5)
Enqueue(3)
Dequeue()
Front()
IsEmpty()

• Array Implementation

- A queue can be implemented with an array, as shown here. For example, this queue contains the integers 4 (at the front), 8 and 6 (at the rear).

[0]	[1]	[2]	[3]	[4]	[5]	...
4	8	6				

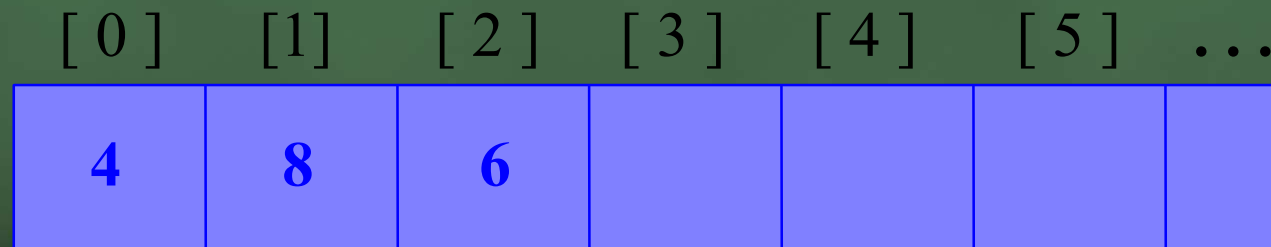
An array of integers
to implement a
queue of integers

We don't care what's in
this part of the array.

• Array Implementation

- The easiest implementation also keeps track of the number of items in the queue and the index of the first element (at the front of the queue), the last element (at the rear).

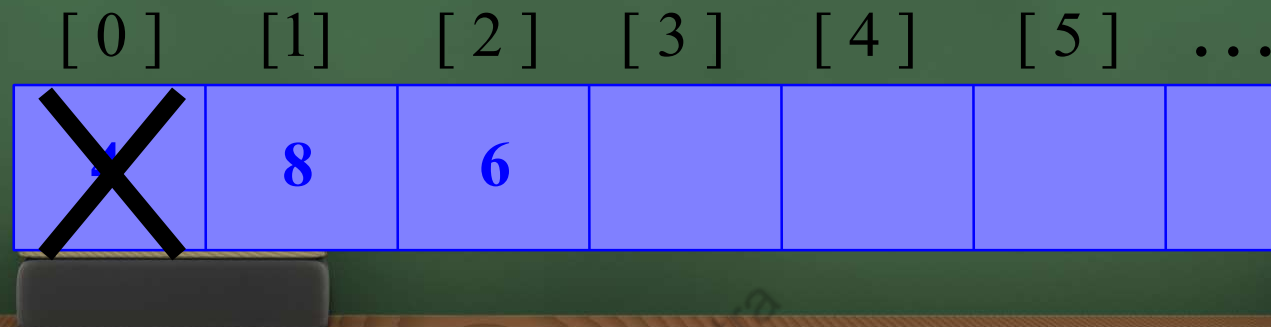
3 size
0 first
2 last



• A Dequeue Operation

- When an element leaves the queue, size is decremented, and first changes, too.

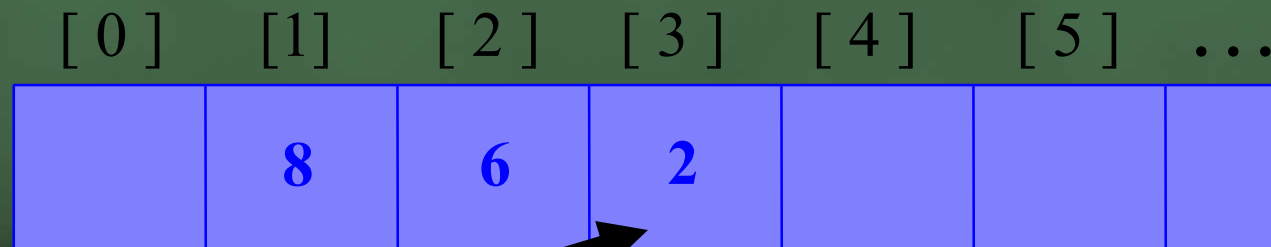
2 size
1 first
2 last



• An Enqueue Operation

- When an element enters the queue, size is incremented, and last changes, too.

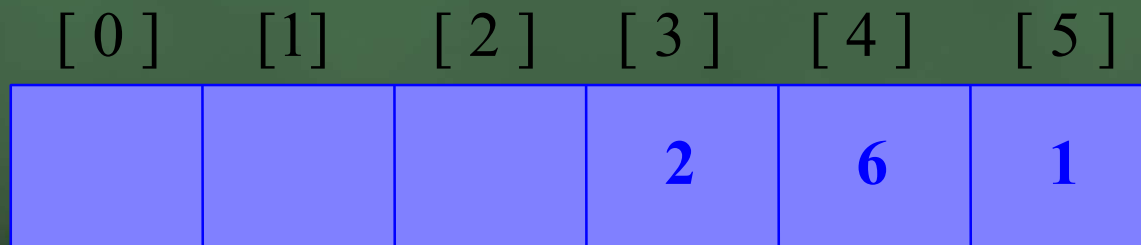
3 size
1 first
3 last



- **At the End of the Array**

- There is special behavior at the end of the array. For example, suppose we want to add a new element to this queue, where the last index is [5]:

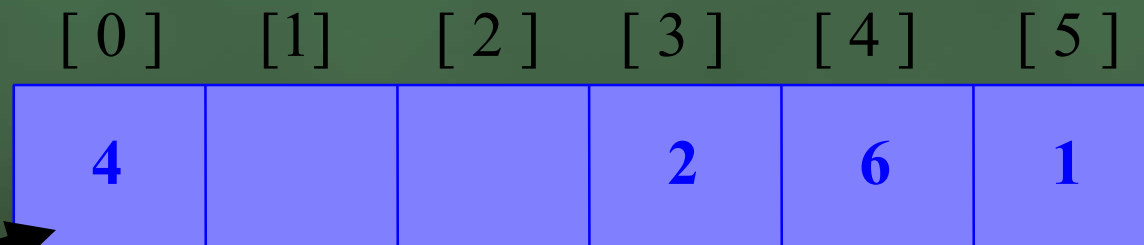
3 size
3 first
5 last



- **At the End of the Array**

- The new element goes at the front of the array (if that spot isn't already used):

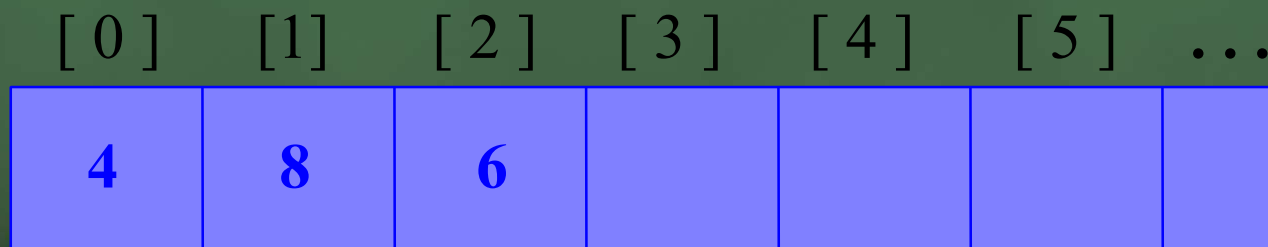
4 size
3 first
0 last



• Array Implementation

- Easy to implement
- But it has a limited capacity with a fixed array
- Or you must use a dynamic array for an unbounded capacity
- Special behavior is needed when the rear reaches the end of the array.

3 size
0 first
2 last



Applications of Queue



Applications of Queue



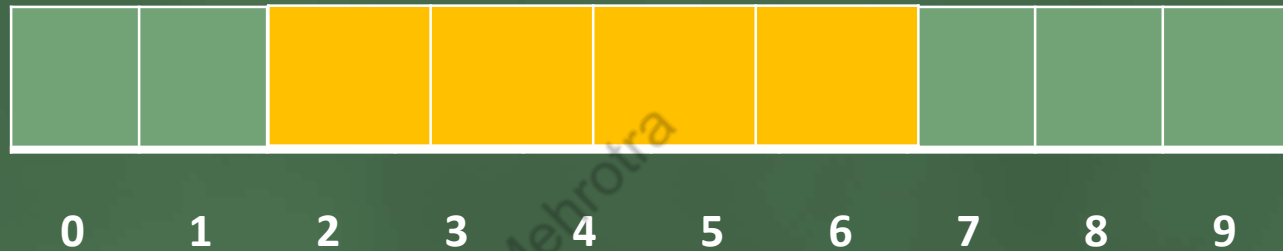
Applications of Queue



- Serving requests of a single shared resource (printer, disk, CPU),



Implementation of Queue



```
int A[10]
front=-1,
rear=-1
```

```
IsEmpty()
{
    if front == -1 && rear == -1
        return true
    else
        return false
}
```


Implementation of Queue

```
Enqueue(x)
```

```
{
```

```
  if IsFull()
```

```
    return
```

```
  else if IsEmpty()
```

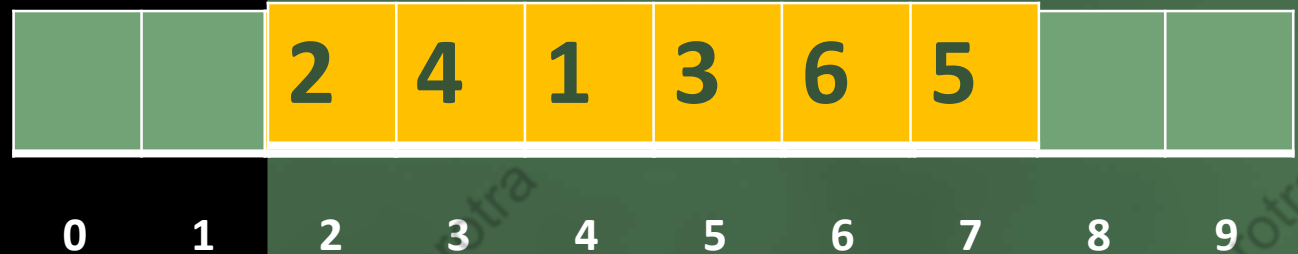
```
    front=rear=0
```

```
  else
```

```
    rear=rear+1
```

```
  a[rear]=x
```

```
}
```



Enqueue(5)

Implementation of Queue



Implementation of Queue

Dequeue(x)

{

if IsEmpty()

return

else if front==rear

front=rear=-1

else

front = front + 1

}



Implementation of Queue

```
Enqueue(x)
{
    if IsFull()
        return

    else if IsEmpty()
        front=rear=0

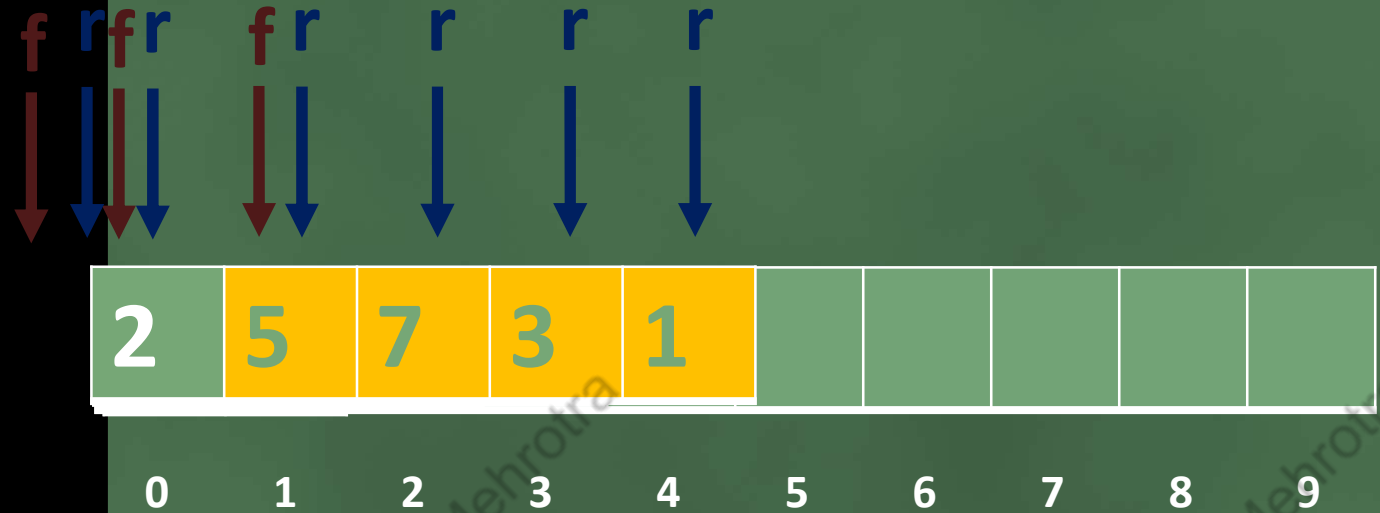
    else
        rear=rear+1

    a[rear]=x
}
```

```
Dequeue(x)
{
    if IsEmpty()
        return

    else if front==rear
        front=rear=-1

    else
        front = front + 1
}
```



Enqueue(2)
Enqueue(5)
Enqueue(7)
Dequeue()
Enqueue(3)
Enqueue(1)

• Implementation of Queue

```
Enqueue(x)
{
    if IsFull()
        return

    else if IsEmpty()
        front=rear=0

    else
        rear=rear+1

    a[rear]=x
}
```

```
Dequeue(x)
{
    if IsEmpty()
        return

    else if front==rear
        front=rear=-1

    else
        front = front + 1
}
```



Enqueue(2)

Enqueue(5)

Enqueue(7)

Dequeue()

Enqueue(3)

Enqueue(1)

Enqueue(9)

Enqueue(10)

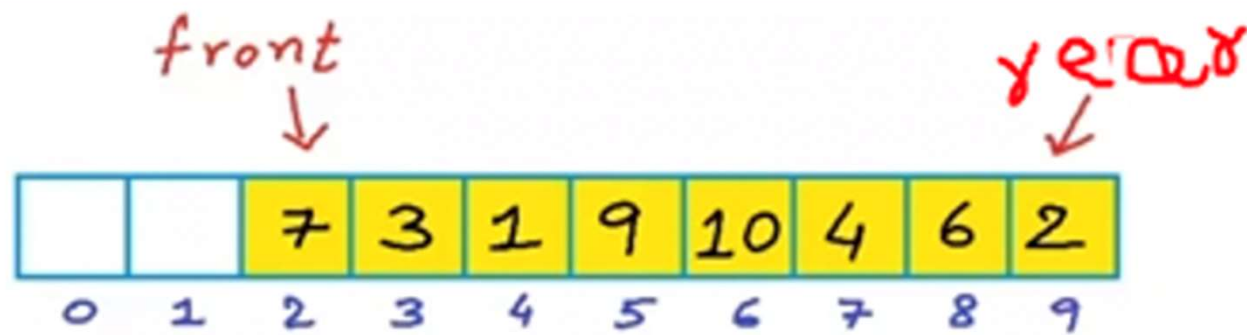
Enqueue(4)

Enqueue(6)

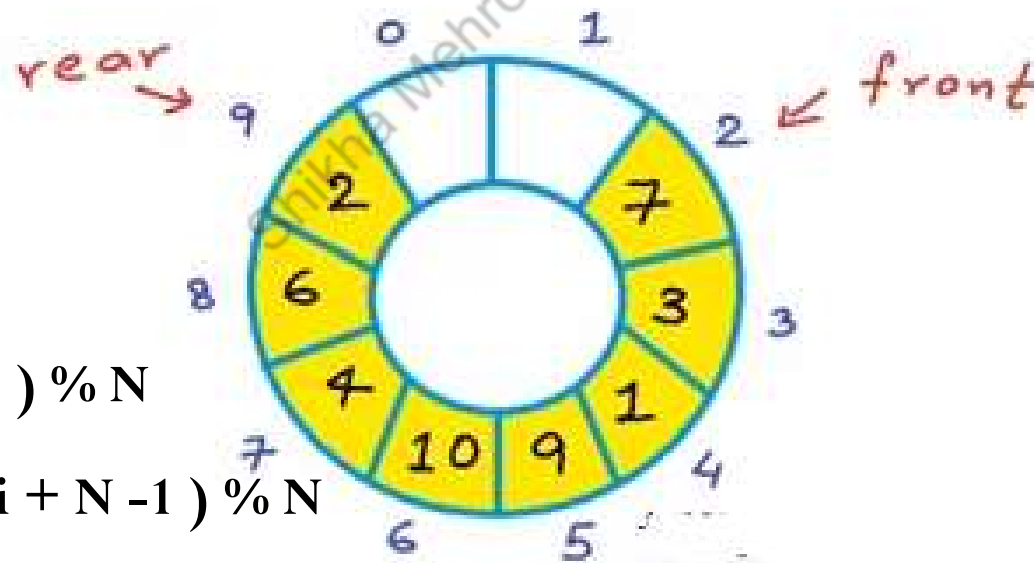
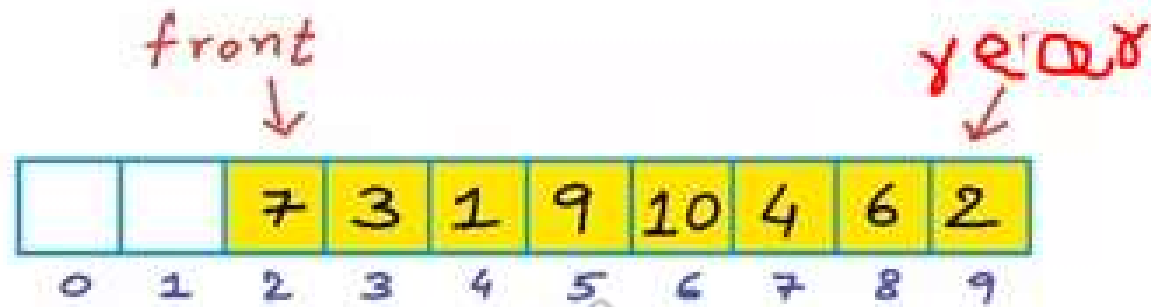
Dequeue()

Enqueue(2)

• CIRCULAR QUEUE



• CIRCULAR QUEUE



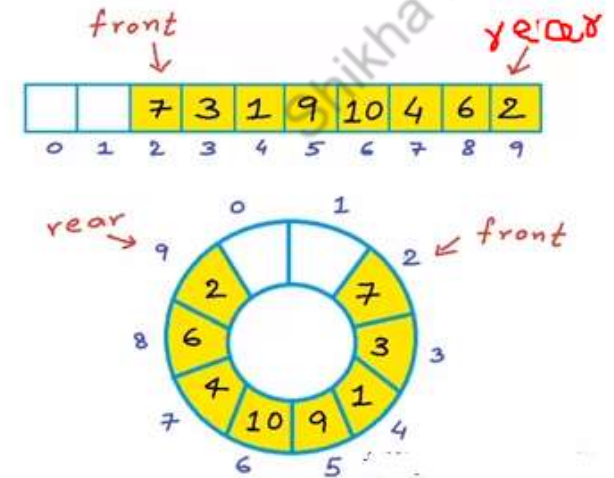
Current Position = i

Next Position = $(i + 1) \% N$

Previous position = $(i + N - 1) \% N$

IsEmpty()

```
{  
    if front == -1 && rear == -1  
        return true  
    else  
        return false  
}
```



```

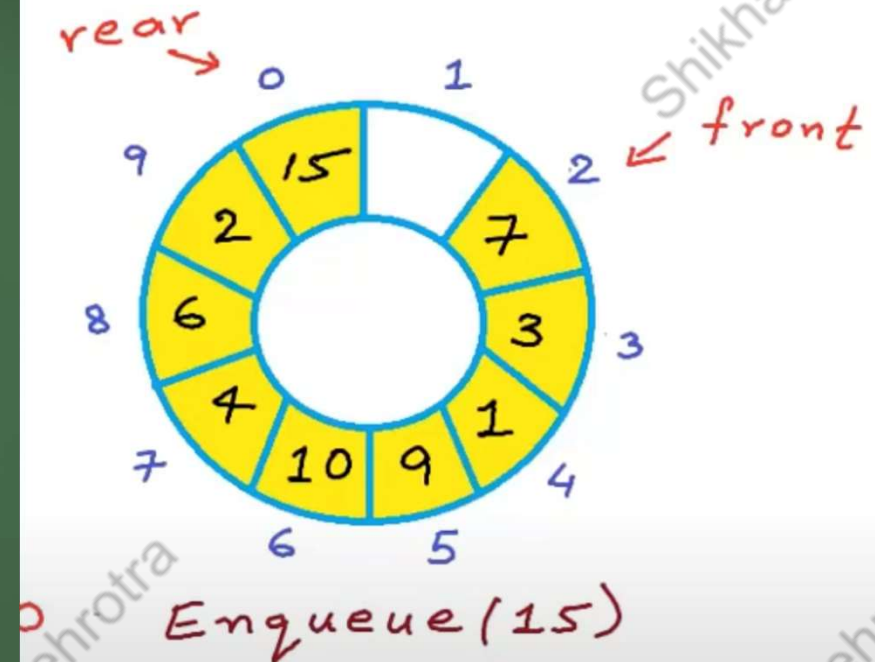
Enqueue(x)
{
    if ( rear + 1 ) % N == front

    else if IsEmpty()
        front=rear=0

    else
        rear= ( rear + 1 ) % N

    a[rear]=x
}

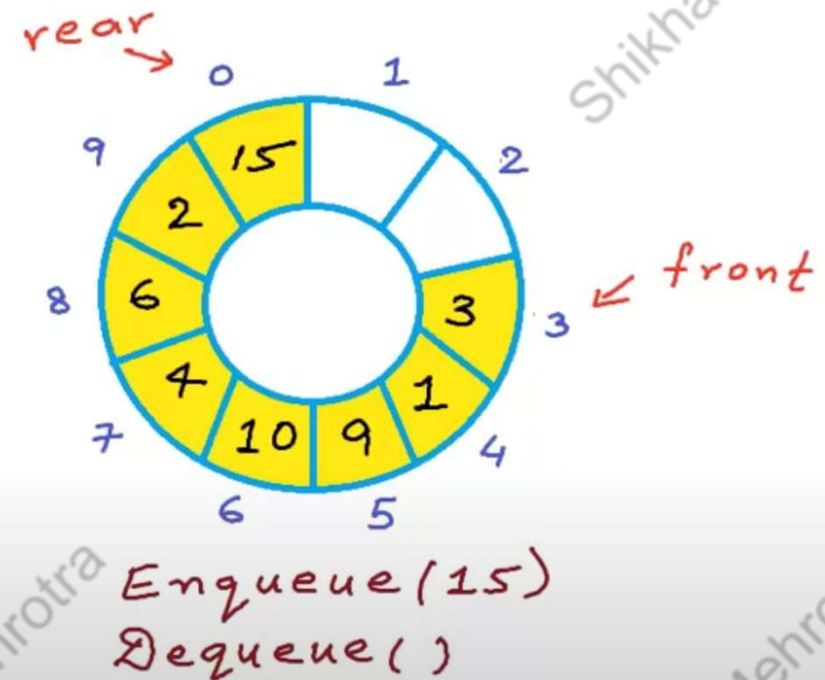
```



```
Dequeue(x)
{
    if IsEmpty()
        return

    else if front==rear
        front=rear=-1

    else
        front =( front + 1 ) % N
}
```



```

#include<stdio.h>
#define n 5
int main()
{
    int queue[n],ch=1,front=0,rear=0,i,j=1,x=n;
    printf("Queue using Array");
    printf("\n1.Insertion \n2.Deletion \n3.Display
\n4.Exit");
    while(ch)
    {
        printf("\nEnter the Choice:");
        scanf("%d",&ch);
        switch(ch)
        {
            case 1:
                if(rear==x)
                    printf("\n Queue is Full");
                else
                {
                    printf("\n Enter no %d:",j++);
                    scanf("%d",&queue[rear++]);
                }
                break;

```

```

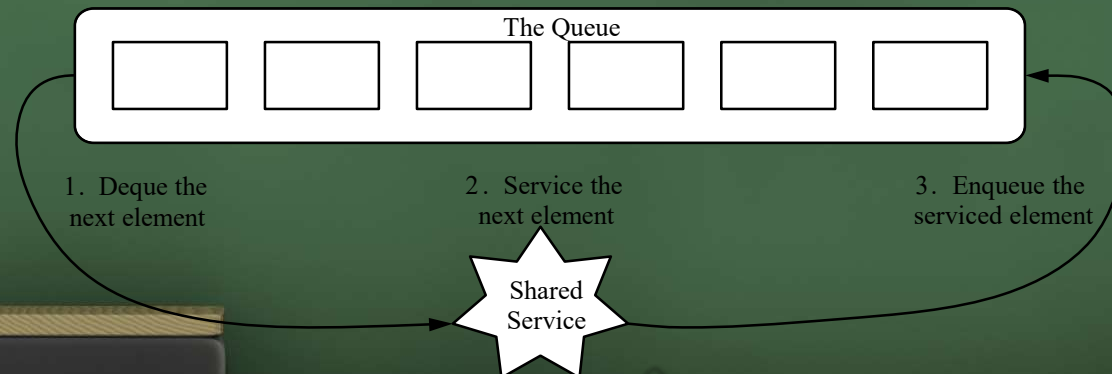
            case 2:
                if(front==rear)
                {
                    printf("\n Queue is empty");
                }
                else
                {
                    printf("\n Deleted Element is %d",queue[front++]);
                    x++;
                }
                break;

            case 3:
                printf("\nQueue Elements are:\n ");
                if(front==rear)
                    printf("\n Queue is Empty");
                else
                {
                    for(i=front; i<rear; i++)
                    {
                        printf("%d",queue[i]);
                        printf("\n");
                    }
                    break;
                }
            case 4:
                exit(0);
            default:
                printf("Wrong Choice: please see the options");
            }
        }
    }
    return 0;
}

```

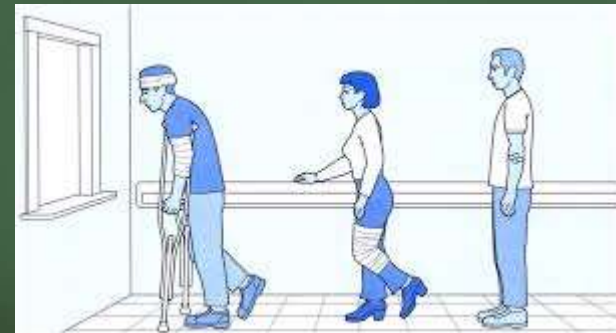
• Application: Round Robin Schedulers

- We can implement a round robin scheduler using a queue, Q , by repeatedly performing the following steps:
 1. $e = Q.dequeue()$
 2. Service element e
 3. $Q.enqueue(e)$



• Priority Queue

- In Priority queue items are ordered by key value so that item with the lowest value of key is at front and item with the highest value of key is at rear or vice versa.
- So we're assigned priority to item based on its key value.
- Lower the value, higher the priority.



• Priority Queue Abstract Data Type

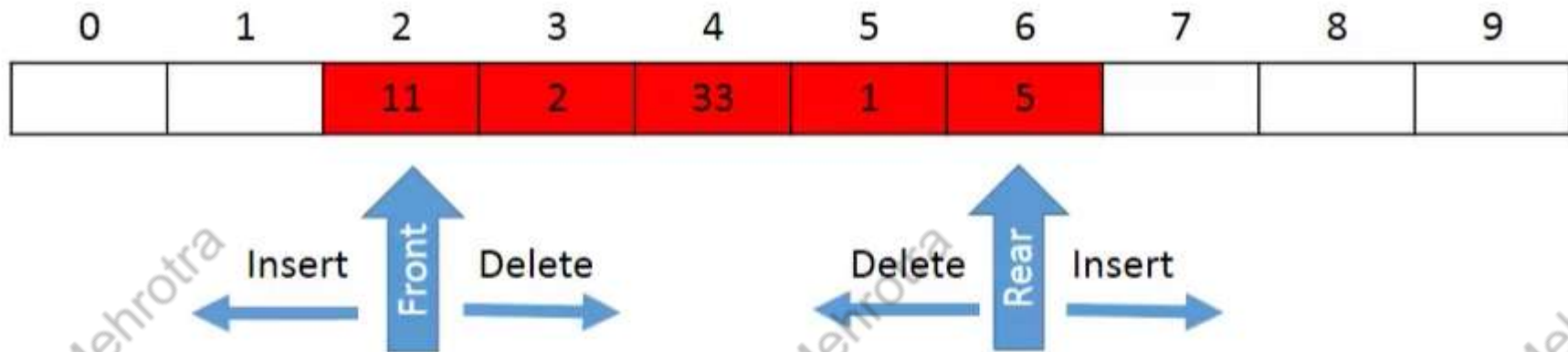
- Two fundamental methods:
 - enqueue
 - dequeue
- Supporting methods
 - PeekMin
 - removeMin
 - isFull – check if queue is full.
 - isEmpty – check if queue is empty.

• Double Ended Queue (Deque)

Double Ended Queue is also a Queue data structure in which the insertion and deletion operations are performed at both the ends (front and rear).



• Functions of Double Ended Queue (Deque)



Four functions possible:

- Insertion at front
- Deletion at front
- Insertion at Rear
- Deletion at Rear

• Deque Abstract Data Type

- Deque: it creates a new deque that is empty. It needs no parameters and returns an empty deque.
- Fundamental Methods:
 - `addFront(item)` adds a new item to the front of the deque. It needs the item and returns nothing.
 - `addRear(item)` adds a new item to the rear of the deque. It needs the item and returns nothing.
 - `removeFront()` removes the front item from the deque. It needs no parameters and returns the item. The deque is modified.
 - `removeRear()` removes the rear item from the deque. It needs no parameters and returns the item. The deque is modified.
- Supporting Methods
 - `isEmpty()` tests to see whether the deque is empty. It needs no parameters and returns a boolean value.
 - `size()` returns the number of items in the deque. It needs no parameters and returns an integer.

• Dequeue Operations

Queue Operation	Queue Contents	Return Value
q.isEmpty()	[]	true
q.enqueue(4)	[4]	
q.enqueue(10)	[10][4]	
q.enqueue(5)	[5][10][4]	
q.size()	[5][10][4]	3
q.isEmpty()	[5][10][4]	false
q.enqueue(9)	[9][5][10][4]	
q.dequeue()	[9][5][10]	
q.dequeue()	[9][5]	
q.size()	[9][5]	2