

Matrix Modulo

Time limit: 1 sec

Given a 2×2 non negative integer matrix A , we would like to calculate of $A^n \bmod k$, where n and k are given positive integers.

In a modular arithmetic, $a \bmod k$ is the remainder of a / k . For example $14 \bmod 5$ equals to 4. In c++, we can calculate $a \bmod k$ by this expression $a \% k$. A matrix $M \bmod k$ where $M = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ is defined as $M = \begin{bmatrix} a \bmod k & b \bmod k \\ c \bmod k & d \bmod k \end{bmatrix}$ and we also know that, for a positive integers p and q

- $(p + q) \bmod k = ((p \bmod k) + (q \bmod k)) \bmod k$
- $(p * q) \bmod k = ((p \bmod k) * (q \bmod k)) \bmod k$
- This property is also valid for matrices M and N
- $(MN) \bmod k = ((M \bmod k)(N \bmod k)) \bmod k$

Input

- The first line of input contains two integer n and k where $1 \leq N \leq 2^{30}$ and $1 \leq K \leq 10,000$.
- The second line contains four integers a, b, c, d which describe the matrix $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ where $1 \leq a, b, c, d \leq 9,999$

Output

There must be exactly 1 line that contains four integers that describe the matrix $A^n \bmod k$

Suggestion

- For 50% of the testcases, the value of n and k is very small such that a direct approach in $O(N)$ would pass
- **It will help to write a function that calculate $(MN) \bmod k$.** Be sure that that function must return a matrix. For example, the function could be written as `vector<int> matrix_multiply(const vector<int> &M,const vector<int> &N,int k);`

Example

Input	Output
2 1000 1 2 3 4	7 10 15 22
2 10 1 2 3 4	7 0 5 2

5 10000 1 2 3 4	1069 1558 2337 3406
5 10 1 2 3 4	9 8 7 6
999888777 4726 3 8 7 2	337 2916 3733 1154