

Assignment 2

Find global minimum point and value for function

$$f(x,y) = x^2 + y^2 + 10$$

DO manual calculations for 2 iterations.

Step 1 :- $x = -1, y = 1, \eta = 0.1, \text{ epochs} = 2$

Step 2 :- $\text{iter} = 1$

$$\text{step 3 b} - \frac{\partial f}{\partial x} = 2x = -2$$

$$\frac{\partial f}{\partial y} = 2y = 2$$

$$\text{step 4 :- } \Delta x = -\eta \frac{\partial f}{\partial x} = -0.1(-2) = 0.2$$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(2) = -0.2$$

$$\text{Step 5 :- } x = x + \Delta x = -1 + 0.2 = -0.8$$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

Step 6 :- $\text{iter} = \text{iter} + 1 = 1 + 1 = 2$

Step 7 :- If ($2 > 2$)

go to step 8

else

go to step 3

$$\text{Step 8 :- } \frac{df}{dx} = 2x = 2(-0.8) = -1.6$$

$$\frac{df}{dy} = 2y = 2(0.8) = 1.6$$

$$\text{Step 9 :- } \Delta x = -\eta \frac{\partial f}{\partial x} = -0.1(-1.6) = 0.16$$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(1.6) = -0.16$$

$$\text{Step 5: } x = x + \Delta x = -0.8 + 0.16 = -0.64$$

$$y = y + \Delta y = 0.8 - 0.16 = 0.64$$

$$\text{Step 6: } i_t = i_t + 1 = 2 + 1 = 3$$

Step 7 & 8 - If ($i_t > \text{epoches}$)

$$3 > 2$$

go to step 8

else

go to step 3

$$\text{Step 8: } x = -0.64$$

$$y = 0.64$$

$$f(x, y) = x^2 + y^2 + 10$$

$$= (-0.64)^2 + (0.64)^2 + 10$$

$$= 0.4 + 0.4 + 10 = 10.8$$

Assignment - 3

let us consider sample dataset have 1 input x_i^a
 and one off (y_i^a) and no. of samples. develop a
 sample regression model using stochastic
 gradient descent optimiser.

sample	x_i^a	y_i^a
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

1) $x, y, m=1, c=-1, \eta=0.1, \text{epoches } \neq 2, n_s=2$

2) $i_t = 1$

3) sample = 1

4) $\frac{\partial E}{\partial m} = -(8.4 - (1)) (0.2 + (-1)) 0.2$
 $= -0.84$

$\frac{\partial E}{\partial c} = -(8.4(1)) (0.2 + 1)$
 $= -4.2$

5) $\Delta m = -(0.1)(0.84) = 0.084 \quad \Delta c = -(0.1)(-4.2)$

6) $m = m + \Delta m$
 $= 1 + 0.84 = 1.084$

$c = c + \Delta c$
 $= -1 + 0.42 = -0.58$

7) sample + = 1 = 2

8) if ($2 > 2$)

 go to step 9

else

 step 4

$$4) \frac{\partial f}{\partial m} = -(3.8 - (1.084)(0.4) + 0.58) 0.4 \\ = -1.5785$$

$$\frac{\partial f}{\partial c} = -(3.8 - (1.084)(0.4) + 0.58) \\ = -3.9464$$

$$5) \Delta m = -(0.1)(-1.5785) = 0.1578$$

$$\Delta c = -(0.1)(-3.9464) = 0.3946$$

$$6) m = m + \Delta m = 1.84 + 0.1578 = 1.2418$$

$$c = c + \Delta c = -0.58 + 0.3946 = -0.1854$$

7) Sample = 1

8) if ($z > 2$)

go to step 9

else

step 4

9) fit + = 1

10) if ($z > 2$)

go to step 11

else

step 3

3) Sample = 1

$$4) \frac{\partial E}{\partial m} = -(3.4 - (1.2)(0.2) + 0.18) 0.2 \\ = -0.668$$

$$\frac{\partial E}{\partial c} = -(3.4 - (1.2)(0.2) + 0.18) \\ = -3.34$$

$$5) \Delta m = -(0.1)(-0.668) = 0.0668$$

$$6) m = \Delta m + m = 1.24 + 0.066 = 1.3$$
$$c = \Delta c + c = 0.18 + 0.33 = 0.51$$

7) Sample = 1

8) if ($\delta > 2$)

· go to step 9

else

step 4

$$4) \frac{\partial E}{\partial m} = -(2.8 - (1.3)(0.4) - 0.15) / 0.4$$
$$= -1.25$$

$$5) \frac{\partial E}{\partial c} = -(2.8 - (1.3)(0.4) - 0.15)$$
$$= -3.13$$

$$5) \Delta m = -(0.1)(-1.25) = 0.12$$

$$\Delta c = -(0.1)(-3.13) = 0.31$$

$$6) m = m + \Delta m = 1.3 + 0.12 = 1.42$$

$$c = c + \Delta c = 0.15 + 0.31 = 0.46$$

7) Sample + = 1

8) if ($\delta > 2$)

· go to step 9.

9) $i_t = i_t + 1$

10) if ($i_t > e_p$)

$\delta > 2$

Step 11

11) print m & c

$$m = 1.42$$

$$c = 0.46$$

Assignment - 5

Let us consider a sample dataset have x_i , y_i
 and i o/p (y_i) and no. of samples develop a SLR model
 using MBGD

Sample (i)	x_{i1}	y_{i1}	
1	0.2	3.4	\rightarrow batch = 1
2	0.4	3.8	
3	0.6	4.2	
4	0.8	4.6	\rightarrow batch = 2

1) $[x, y]; m=1, c=-1, \eta=0.1, \text{epochs}=2, \text{bs}=2$

2) $n_b = \frac{n_s}{\text{bs}} = \frac{4}{2} = 2$

3) $t=1$

4) Batch = 1

5) $\frac{\partial E}{\partial m} = -\frac{1}{\text{bs}} \cdot \sum_{i=1}^{\text{bs}} (y_i - mx_i - c)x_i$

$$= -\frac{1}{2} [(3.4 - (1)(0.2) + 1)0.2] + [3.8 - 0.4 + 1]0.4$$

$$= -1.34$$

$$\frac{\partial E}{\partial c} = -\frac{1}{2} [(3.4 - 0.241) + (3.8 - 0.4 + 1)]$$

$$= -4.3$$

6) $\Delta m = -(0.1)(-1.34) = 0.134$

$$= -(0.1)(-4.3) = 0.43$$

7) $m = m + \Delta m = 1 + 0.134 = 1.134$

$$c = c + \Delta c = -1 + 0.43 = -0.57$$

8) Batch + = 1

9) If ($z > 2$)

go to step 10 else step 5.

$$5) \frac{\partial E}{\partial m} = -\frac{1}{2} \left[4.2 - (1.1(0.6)) + 0.57 \right] 0.6 + \\ (4.6 - (1.134)(0.8) + 0.57) 0.8 \\ = 2.932$$

$$\frac{\partial E}{\partial c} = -\frac{1}{2} \left[4.2 - (1.134)(0.6) + 0.57 \right] + \\ (4.6 - (1.134)(0.8) + 0.57) \\ = -4.17$$

$$6) \Delta m = 0.2932$$

$$\Delta c = 0.417$$

$$7) m = 1.13 + 0.293 = 1.42$$

$$c = -0.57 + 0.4 = -0.15$$

8) Batch += 1

9) if (batch > nb)

$$3 > 2$$

go to step 10

10) if $t = 1$

11) if ($z > 2$) go to step 12 else step 4

4) Batch = 1

$$\frac{\partial E}{\partial m} = -\frac{1}{2} \left[3.4 - (1.4)(0.2) + 0.5 \right] 0.2 + \\ (3.8 - (1.4)(0.4) + 0.15) 0.4 \\ = -1.0029$$

$$\frac{\partial E}{\partial c} = -\frac{1}{2} \left[3.4 - (1.42)(0.2) + 0.1523 \right] + \\ (3.8 - (1.4)(0.4) + 0.15) \\ = -3.3241$$

$$8) \Delta m = -0.1(-1.0029) = 0.1002$$

$$\Delta c = -0.1(-3.3241) = 0.332$$

$$7) m+ = \Delta m = 1.42 + 0.1002 = 1.5$$

$$c+ = \Delta c = -0.15 + 0.3 = 0.15$$

8) Batch_{t+1} = 1

9) If ($t > 2$) go to step 10 else step 7

$$10) \frac{\partial E}{\partial m} = \frac{-1}{2} [4.2 - (1.5(0.6) - 0.15)(0.6) + (4.6 - (1.5(0.8) - 0.15)(0.8))] \\ = -2.21$$

$$\frac{\partial E}{\partial c} = -3.151$$

$$8) \Delta m = -0.1 \times -2.21 = 0.221$$

$$\Delta c = -0.1 \times -3.15 = 0.315$$

$$7) m+ = \Delta m = 1.5 + 0.22 = 1.7$$

$$c+ = \Delta c = 0.15 + 0.3 = 0.45$$

8) Batch_{t+1} = 1

9) If (Batch > nb) go to step 10 else step 5

10) $9t \neq 1$

11) If ($3 > 2$) go to step 12

12) print m, c

$$m = 1.748$$

$$c = 0.494$$

Assignment-7

Let consider a sample dataset have one input (x_i^o) and (y_i^o) and no. of samples a develop a sample linear regression model by BGD

sample	x_i^o	y_i^o
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

1) $[x, y]; m=1, c=-1, \eta=0.1, \text{ epochs}=2, n_s=2$

2) $\theta_t = 1$

$$3) \frac{\partial E}{\partial m} = -\frac{1}{n_s} \sum_{i=1}^{n_s} (y_i^o - m x_i^o - c) x_i^o$$

$$= -\frac{1}{2} [3.4 - (1)(0.2) + 1] 0.2 + (3.8 - (0.2) + 1) 0.4$$

$$= -1.34$$

$$4) \frac{\partial E}{\partial c} = -\frac{1}{2} [3.4 - 0.2 + 1] + (3.8 - 0.4 + 1)$$

$$= -4.3$$

$$5) \Delta m = -\eta \frac{\partial E}{\partial m}$$

$$= -0.1 \times -1.34 = 0.134$$

$$\Delta c = -\eta \frac{\partial E}{\partial c}$$

$$= -0.1 \times (-4.3) = 0.43$$

$$5) m+ = m + \Delta m$$

$$= 1 + 0.134 = 1.13$$

$$c+ = c + \Delta c$$

$$= -0.4 + 0.43 = 0.03$$

8) $9t+ = 1$

7) if ($t > 2$)

go to step 8;

3) $\frac{\partial E}{\partial m} = \frac{1}{2} [3.4 - (1.134)(0.2) + 0.54)(0.2) + 3.8 - (1.134)(0.4) + 0.57)(0.4)]$
 $= -1.157$

4) $\frac{\partial E}{\partial c} = -\frac{1}{2} [3.4 - (1.134)(0.2) + 0.57) + 3.8 - (1.134)(0.4) + 0.57)]$
 $= -3.829$

4) $\Delta m = -0.1 \times 1.157 = 0.1157$

$\Delta c = -0.1 \times -3.829 = 0.3829$

5) $m+ = \Delta m \Rightarrow 1.134 + 0.1157 = 1.2497$

$c+ = \Delta c \Rightarrow -0.57 + 0.3829 \Rightarrow -0.187$

6) $9t+ = 1$

7) if ($t > \epsilon_0$) go to step 8

$t > 2$

8) $m = 1.24$

$c = -0.187$

Assignment - 9

let us consider a sample dataset have 1 input (x_i) and one output (y_i) and no. of samples develop a simple linear regression model using momentum optimiser

sample	$\eta^{(i)}$	y_i
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

do manual calculations for 2 iterations with 1st 2 samples

Step 1: $[x, y] \cdot m=1, c=1, \eta=0.1, \text{epoch}=2, \beta=0.9,$

$$v_m = v_c = 0$$

2) $M = 1$

3) sample = 1

$$\begin{aligned} 4) \quad g_m &= \frac{\partial E}{\partial m} = -(y_i - m x_i - c) x_i \\ &= -(3.4 - (1)(0.2) + 1)(0.2) \\ &= -0.84 \end{aligned}$$

$$g_c = \frac{\partial E}{\partial c} = -(y_i - m x_i - c) = -(3.4 - 0.2 + 1) = -4.2$$

$$\begin{aligned} 5) \quad v_m &= \beta v_m - \eta g_m \\ &= (0.9)(0) - (0.1)(-0.84) \\ &= 0 - 0.084 = -0.084 \end{aligned}$$

$$\begin{aligned} v_c &= \beta v_c - \eta g_c \\ &= 0.9 \times 0 - (-0.1)(-4.2) = -0.42 \end{aligned}$$

$$6) \quad m = m + v_m = 1 + (-0.084) = -0.916$$

$$c = c + v_c = -1 - 0.42 = -1.42$$

7) sample + = 1

$$1+1=2$$

8) If (sample > ns) go to step 9
else : goto step 4

9) iter + = 1

$$1+1=2$$

10) If (ft > epoch) go to step 4
else Step 3

3) sample = 1

$$4) q_m = \frac{\partial e}{\partial m} = - (3.4 - (0.6463)(0.2) + 2.283)(0.2) \\ = -1.110$$

$$q_c = \frac{\partial e}{\partial c} = -3.4 - (0.6)(0.2) + 2.28 \\ = -5.5$$

$$5) v_m = \lambda v_m - \eta q_m = (0.9)(-0.289) - (0.1)(-1.110) \\ = -0.3453$$

$$v_c = \lambda v_c - \eta q_c \\ = (0.9)(-0.863) - (-0.1)(-5.5) \\ = -1.332$$

$$6) m = m + v_m \Rightarrow 0.6463 + (-0.3453) = 0.293$$

$$c = c + v_c \Rightarrow -3.283 - 1.332 = -4.615$$

7) sample + = 1

$$1+1=2$$

8) If (sample > ns) go to step 9
else goto step 4

$$9) q_m = -(3.8 - (0.293)(0.0 + 3.615))(0.4) = -2.919$$

$$q_c = -(3.8 - (0.293)(0.4) + \cancel{8.615}) \\ = -7.297$$

$$5) v_m = (0.9)(-0.353) - (-0.1 \times -2.919) = 0.6098$$

$$v_c = 0.9(-1.332) - (-0.1)(-7.297) = -1.9285$$

$$6) M_t = v_m \Rightarrow 0.293 - 0.609 = -0.316$$

$$C_t = v_c \Rightarrow -3.615 - 1.928 = -5.543$$

$$7) \text{sample } t=1 \Rightarrow 2+1=3$$

8) If (example > ns) : go to step 9
else go to step 4

$$9) e_{tert+1}$$

$$2+1=3$$

10) If ($e_{tert} > \text{epochs}$) go to step 11

$$3 > 2$$

else go to step 3

11) print m, c

$$m = -0.316, c = -5.543$$

Assignment - 11

Let us consider a sample dataset have 1 PPN_{AG}
 one O/P y_i and no. of sample 4. develop a SLR
 model using nested accelerated gradient (NAG)
 optimiser

Sample	x_{i9}	y_{i9}	→ do manual calculation for 2 iteration with 1st 2 samples
1	0.2	3.4	
2	0.4	3.8	
3	0.6	4.2	
4	0.8	4.6	

→ Step 1 : $x, y; m=1, c=-1, \eta=0.1, \text{epoch}=2, \beta=0.4$
 $v_m = v_c = 0, n_s = 2$

Step 2 : $\theta_{Hes} = 1$

Step 3 : Sample 2

$$\begin{aligned}
 g_m &= \frac{\partial E}{\partial m} = -(y_i - m + \beta m) x_i - (c + \beta c) x_i \\
 &= -(3.4 - (1+0.9)0)0.2 - (-1+(0.9)0)0.2 \\
 &= 0.84
 \end{aligned}$$

$$g_c = \frac{\partial E}{\partial c} = -4.2$$

$$\begin{aligned}
 \text{Step 5 : } v_m &= \eta v_m - \eta g_m \\
 &= 0.084
 \end{aligned}$$

$$\begin{aligned}
 v_c &= \eta v_c - \eta g_c \\
 &= -0.42
 \end{aligned}$$

$$\begin{aligned}
 \text{Step 6 : } m+ &= v_m = 1 - 0.084 = 0.916 \\
 c+ &= v_c = -1 - 0.42 = -1.42
 \end{aligned}$$

7: sample + = 1 $\Rightarrow 1+1=2$

8: if (sample > ns) goto step 9
else go to step 4

$$9: q_m = \frac{\partial E}{\partial m} = -(3.8 - (0.916 + (0.9(-0.8)))0.4) \\ - (-1.42 + (0.6 - 0.034)(0.4)) \\ = -1.983$$

$$q_c = \frac{\partial E}{\partial c} = -4.954$$

$$10: v_m = \theta v_m - \eta q_m \\ = 0.9(-0.84) - (-0.1(-1.983)) \\ = -0.2739$$

$$11: m+ = v_m = 0.916 - 0.2739 = 0.6421$$

$$v_c = -1.42 - 0.8739 = -2.293$$

12: sample + = 1

13: if (sample > ns) goto step 9
else step 4

14: $q_t + = 1$

15: if ($q_t >$ epochs) goto step 11
else goto step 3

16: sample = 1

$$17: \frac{\partial E}{\partial m} \Rightarrow -(3.8 - (0.64 + (0.9)(0.27))0.2) \\ - (-2.293 + 0.027)(0.2)$$

$$q_m = -1.0171$$

$$q_c = -5.85$$

$$18: v_m = \theta v_m - \eta q_m = (0.9)(-0.2739)] (-0.1(-1.1)) \\ = -0.86$$

$$-0.3627$$

$$v_c = v_c^2 - \eta q_c$$

$$= -1.37$$

$$6) m+ = v_m \Rightarrow 0.6421 + (-0.3627) = 0.2794$$

$$c+ = v_c \Rightarrow -2.2989 - 1.3707 = -3.6646$$

\Rightarrow sample $+ = 1$

8) $\text{if } (\text{sample} > n_s) : \text{go to step 9} \text{ else } (4)$

$$4) q_m = -2.985$$

$$q_c = -7.4645$$

$$5) v_m = 0.9 (-0.3627) - (-0.1) (-2.985)$$

$$= -0.6249$$

$$v_c = 0.9 (-1.37) - (-0.1 - 7.4645)$$

$$= -1.9800$$

$$6) m+ = v_m = 0.29 - (0.62) = -0.3$$

$$c+ = v_c = -3.6646 - 1.9800 = -5.6446$$

\Rightarrow Sample $+ = 1 \Rightarrow 2+1=3$

8) $\text{if } (\text{sample} > n_s) : \text{go to step 9} \text{ else } (4)$

9) $i_{tt}=1 \Rightarrow 2+1=3$

10) $\text{if } (i_{tt} > \text{epoch}) : \text{go to step 4}$

- else \Rightarrow go to step 3

11) print m, c

$$m = 0.3275$$

$$c = -4.6446$$

Assignment - 13

Let us consider a sample dataset have 19 p
 $(x_{i,c})$ and 1 o/p ($y_{i,a}$) and no. of sample 4
 develop a simple linear regression model using
 ADAGRAD optimiser.

Sample (i)	$x_{i,a}$	$y_{i,a}$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

1) $[x, y]$, epochs = 2, m = 1, c = -1, $g_m \neq g_c \geq 0$, $\eta = 0.1$,
 $\epsilon = 10^{-8}$

2) $i_{ter} = 1$

3) sample = 1

4) $g_m = -0.84$

$g_c = -0.2$

5) $g_m = 0.705$

$g_c = 17.64$

6)

$$\Delta m = \frac{-\eta}{\sqrt{g_m + \epsilon}} g_m = \frac{-0.1}{\sqrt{0.705 + 10^{-8}}} (0.8) = 0.09$$

$$\Delta c = \frac{-(0.1)}{\sqrt{17.64 + 10^{-8}}} \times 4.2 = 0.09$$

$$7) m = m + \Delta m = 1 + 0.09 = 1.09$$
$$c = c + \Delta c = -1 + 0.09 = -0.91$$

$$8) s = s + 1 \Rightarrow 1 + 1 = 2$$

9) if ($s > n_s$) go to step 10 else step 4

$$10) q_m = -(8.5 - (1.09)(0.4) + 0.91)(0.4) = -1.7$$

$$q_c = -4.27$$

$$11) G_m = 3.5$$

$$G_C = 35.37$$

$$12) \Delta m = 0.08$$

$$\Delta c = 0.07$$

$$13) m = m + c = 1.17$$

$$c = -0.84$$

$$14) s = s + 1 \Rightarrow 3$$

15) if ($s > n_s$) go to 10 else ④

$$16) \text{if } t = 1 \Rightarrow 1 + 1 \Rightarrow 2$$

17) if ($t > \text{epoch}$) go to ⑫ else ③

$$s > 2$$

$$18) s = 1$$

$$19) q_m = -0.80$$

$$q_c = -4.0$$

$$20) \Delta m = \frac{-0.1}{\sqrt{4.23 + 10^8}} (t(0.8)) = 0.088$$

$$\Delta c = \frac{-0.1}{\sqrt{5.18 + 10^8}} (t(4.0)) = 0.05$$

$$7) m = m + \Delta m = 0.038 + 1.17 = 1.208$$

$$c = c + \Delta c = -0.84 + 0.05 = -0.79$$

8) If (sample > ns) go to step 10 else go ④

$$4) q_m = -(3.8 - (1.20)(0.4) + 0.70)(0.4)$$
$$= -1.69$$

$$q_c = -(3.8 - (-1.20)(0.4) + 0.7) = -4.11$$

$$5) g_m = 4.28 + (-1.64)^2 = 6.09$$

$$g_c = 51.8 + (-4.11)^2 = 68.7$$

$$6) \Delta m = \frac{-0.1}{\sqrt{6.0 + 10^{-8}}} (1.64) = 0.06$$

$$\Delta c = \frac{-0.1}{\sqrt{68.7 + 10^{-8}}} (4.11) = 0.04$$

$$7) m = m + \Delta m = 1.2 + 0.06 = 1.26$$

$$c = c + \Delta m = -0.7 + 0.04 = -0.75$$

8) Sample + = 1 \Rightarrow 3

9) If (sample > ns) go to step 10 else go ④
3 > 2

10) Iter + = 1 \Rightarrow 2 + 1 = 3

11) If (Iter > epochs) go to ⑫ else go to ⑬

$$12) m = 1.26$$

$$c = -0.75$$

Assignment - 15

Let us consider a sample dataset have 1
 P(X_{i,j}) and P(Y_{i,j}) and no. of sample 2.
 develop a simple linear regression model
 using RMSPROP optimiser

sample	x _{i,j}	y _{i,j}
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

1) $\{x, y\} \cdot \eta = 0.1, \text{ epoch} = 2, m = 1, c = -1, b = 0.9, \epsilon_m = \epsilon_c$

$$\epsilon = 10^{-8}$$

2) Iter = 1

3) Sample = 1

4) $\epsilon_m = -(3.4 - (1)(0.2)) + 1)(0.2) = -0.84$

$$\epsilon_c = -(3.4 - (1)(0.2)) + 1)(-4.2) = -4.2$$

5) $\epsilon_m = (0.9)(0) + (1 - 0.9)(-0.84)^2 = 0.07$

$$\epsilon_c = (0.9)(0) + (1 - 0.9)(-4.2)^2 = 1.764$$

6) $\Delta m = \frac{-0.1}{\sqrt{0.07 + 10^{-8}}} (-0.84) = 0.31$

$$\Delta c = \frac{-0.1}{\sqrt{1.76 + 10^{-8}}} (-4.2) = 0.31$$

7) $m = m + \Delta m = 1 + 0.31 = 1.31$

$c = -0.69$

8) sample $t = 1$

$$t+1 = 2$$

9) if ($s > n_s$) go ⑩ else ④

4) $g_m = -(3.8 - (1.31)(0.4) + (0.69)(0.4)) = -1.5$

$$g_c = -(3.8 - (1.31)(0.4) + (0.69)) = -3.9$$

5) $E_m = 0.28$

$$E_c = 3.1$$

6) $\Delta m = \frac{-0.1}{\sqrt{0.28 + 10^{-8}}} (1.5) = 0.28$

$$\Delta c = \frac{-0.1}{\sqrt{3.1 + 10^{-8}}} (-3.9) = 0.22$$

7) $m = m + \Delta m \Rightarrow 1.31 + 0.28 = 1.5$

$$c = c + \Delta c \Rightarrow -0.69 + 0.22 = -0.47$$

8) sample $t = 1$

$$t+1 = 2$$

9) if (sample $> n_s$) go to step 10 else ④

$$3 > 2$$

10) $\hat{g}_t = \hat{g}_{t+1}$

11) if ($\hat{g}_t > \text{epoch}$) go ⑫ else step ⑧

8) $s = 1$

4) $g_m = -(3.4 - 1.5(0.2) + 0.47)(0.2) = -0.4$

$$g_c = -(3.4 - (1.59)(0.2) + 0.47) = 3.5$$

5) $E_m = 0.9(0.28) + (0.1)(-0.7)^2 = 0.3$

$$E_c = 0.9(3.1) + (0.1)(-3.5)^2 = 4.0$$

6)

$$\Delta m = 0.12$$

$$\Delta c = 0.17$$

$$7) m_t = \Delta m = 1.7$$

$$c_t = \Delta c = 0.3$$

8) if $s > n_s$ go to 10

$t > t$

else goto ④

$$9) g_m = - (3.8 - (1.7)(0.4) + 0.3)(0.4) = -1.4$$

$$g_c = -(3.8 - (1.7)(0.4) + 0.3) = -3.6$$

$$10) F_m = (0.4)(0.3) + (0.1)(1.4)^2 = 0.46$$

$$F_c = (0.9)(4.0) + (0.1)(-3.6)^2 = 4.89$$

$$11) \Delta m = 0.2$$

$$\Delta c = 0.16$$

$$12) m_t = \Delta m = 1.91$$

$$c_t = \Delta c = 0.14$$

8) sample $t = 1 \Rightarrow s+1 = 3$

9). if (sample $> n_s$) go to 10 else ④

10) if $t = 1 \Rightarrow s+1 = 3$

11) if ($t > epoch$) go to step 12 else go ③

$$12) m = 1.91$$

$$c = -0.14$$