

Stat 6021: HW Set 4

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1. You will use the dataset `copier.txt` for this question. This is the same data set that you used in the last homework. The Tri-City Office Equipment Corporation sells an imported copier on a franchise basis and performs preventive maintenance and repair service on this copier. The data have been collected from 45 recent calls by users to perform routine preventive maintenance service; for each call, **Serviced** is the number of copiers serviced and **Minutes** is the total number of minutes spent by the service person.

It is hypothesized that the total time spent by the service person can be predicted using the number of copiers serviced. Fit an appropriate linear regression and answer the following questions.

```
times_spent_servicing_and_numbers_of_copiers_serviced <- read.table(
  "../Module_3--Simple_Linear_Regression/Homework/copier.txt", header = TRUE
)
head(times_spent_servicing_and_numbers_of_copiers_serviced, n = 3)
```

```
##   Minutes Serviced
## 1      20         2
## 2      60         4
## 3      46         3
```

```
library(TomLeversRPackage)
data_set <- times_spent_servicing_and_numbers_of_copiers_serviced
linear_model <- lm(Minutes ~ Serviced, data = data_set)
summarize_linear_model(linear_model)
```

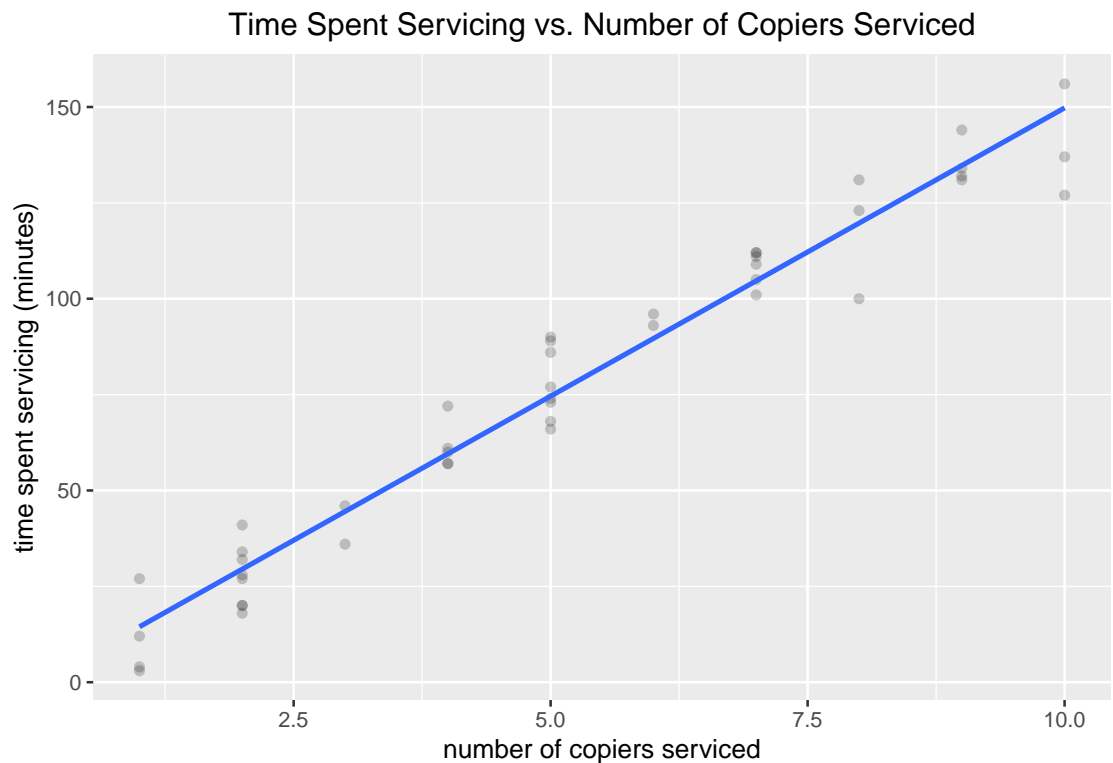
```
##
## Call:
## lm(formula = Minutes ~ Serviced, data = data_set)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -22.7723  -3.7371   0.3334   6.3334  15.4039
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -0.5802     2.8039  -0.207   0.837
## Serviced     15.0352     0.4831  31.123 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.914 on 43 degrees of freedom
## Multiple R-squared:  0.9575, Adjusted R-squared:  0.9565
## F-statistic: 968.7 on 1 and 43 DF, p-value: < 2.2e-16
##
## E(y | x) = B_0 + B_1 * x = -0.5802 + 15.0352 * x
```

```
## Number of observations: 45
## Estimated variance of errors: 79.459396
## Multiple R: 0.978516981701943 Adjusted R: 0.978008179924892
```

- (a) Produce an appropriate scatterplot and comment on the relationship between the total time spent by the service person and the number of copiers serviced.

The response variable is **Minutes**, the total number of minutes spent by the service person. The predictor is **Serviced**, the number of copiers serviced.

```
library(ggplot2)
ggplot(
  times_spent_servicing_and_numbers_of_copiers_serviced,
  aes(x = Serviced, y = Minutes)
) +
  geom_point(alpha = 0.2) +
  geom_smooth(method = "lm", se = FALSE) +
  labs(
    x = "number of copiers serviced",
    y = "time spent servicing (minutes)",
    title = "Time Spent Servicing vs. Number of Copiers Serviced"
  ) +
  theme(
    plot.title = element_text(hjust = 0.5),
    axis.text.x = element_text(angle = 0)
  )
)
```



The relationship between time spent servicing and number of copiers serviced appears linear. A line of best fit has been rendered to aid in this determination. A simple linear regression model appears reasonable for time spent servicing and number of copiers data.

- (b) What is the correlation between the total time spent by the service person and the number of copiers serviced? Interpret this correlation contextually.

We assume that the sample of service calls is simple random. We assume that (Serviced, Minutes) matched pairs of data for the service calls are independent. We assume that errors / residuals between actual and predicted times spent servicing are normally and independently distributed with mean 0 and constant variance. The linear model for time spent servicing vs. number of copiers serviced has an adjusted sample linear Pearson coefficient $R = 0.978$. The adjusted sample linear Pearson correlation coefficient measures the strength of the linear relationship between (Serviced, Minutes) matched pairs of data for the sample of service calls. The linear model has a positive linear Pearson correlation. The value of the adjusted sample linear Pearson correlation coefficient lies between -1 and 1 inclusive. Since the scatterplot shows a reasonable linear association, the adjusted sample linear Pearson correlation coefficient is reliable. Since the above probability $p < 2.2 \times 10^{-16}$ is less than a significance level $\alpha = 0.05$, we reject a null hypothesis of a linear regression t test that there is no correlation between time spent servicing and number of copiers serviced, and conclude that there is a correlation between time spent servicing and number of copiers serviced. The linear model has an adjusted sample coefficient of determination of $R^2 = 0.957$. The adjusted sample coefficient of determination is the proportion of variation in time spent servicing that is explained by the linear relationship / number of copiers. The adjusted sample coefficient of determination lies between 0 and 1. Since the adjusted sample coefficient of determination is greater than 0.8, the linear model is precise and good for prediction.

- (c) Can the correlation found in part 1b be interpreted reliably?

As above, since the scatterplot shows a reasonable linear association, the correlation coefficient $R = 0.978$ is reliable.

- (d) Obtain the 95 percent confidence interval for the slope β_1 .

```
confidence_level <- 0.95
confint(linear_model, level = confidence_level)
```

```
##                2.5 %    97.5 %
## (Intercept) -6.234843  5.074529
## Serviced    14.061010 16.009486
```

The 95 percent confidence interval for the slope β_1 is $[14.061 \frac{\text{min}}{1}, 16.009 \frac{\text{min}}{1}]$. Since the confidence interval does not contain 0, we reject the null hypothesis $H_0 : \beta_1 = 0 \frac{\text{min}}{1}$ that the slope of the linear model for time spent servicing vs. number of copiers serviced is 0. We have sufficient evidence to support the alternate hypothesis $H_1 : \beta_1 \neq 0$.

- (e) Suppose a service person is sent to service 5 copiers. Obtain an appropriate 95 percent interval that predicts the total service time spent by the service person.

```
predict(
  linear_model,
  data.frame(Serviced = 5),
  level = 0.95,
  interval = "prediction"
)

##      fit      lwr      upr
## 1 74.59608 56.42133 92.77084
```

An appropriate 95 percent prediction interval that predicts the total service time spent by a service person sent to service 5 copiers is $[56.421 \text{ min}, 92.771 \text{ min}]$.

- (f) What is the value of the residual for the first observation? Interpret this value contextually.

Let $\hat{\beta}_0 = -0.5802 \text{ min}$ and $\hat{\beta}_1 = 15.0352 \frac{\text{min}}{1}$ be the estimated intercept and slope of the linear model for time spent servicing vs. number of copiers serviced.

The residual e_i for the i th observation $(x_i, y_i) = (\text{Serviced}_i, \text{Minutes}_i)$ is the difference between the observed time spent servicing $y_i = \text{Serviced}_i$ given the observed number of copiers serviced x_i and the predicted time spent servicing $\hat{y}_i = \hat{\beta}_0 + \hat{\beta}_1 x_i$. Mathematically,

$$e_i = y_i - \hat{y}_i$$

The residual e_1 for the first observation $(x_1, y_1) = (\text{Serviced}_1, \text{Minutes}_1) = (2, 20 \text{ min})$ in `copier.txt` is the difference between the observed time spent servicing $y_1 = \text{Serviced}_1 = 20 \text{ min}$ given the observed number of copiers serviced $x_1 = 2$ and the predicted time spent servicing $\hat{y}_1 = \hat{\beta}_0 + \hat{\beta}_1 x_1 = (-0.5802 \text{ min}) + (15.0352 \frac{\text{min}}{1})(2) = 29.4884 \text{ min}$.

$$e_i = y_i - \hat{y}_i = (20 \text{ min}) - (29.4884 \text{ min}) = -9.4884 \text{ min}$$

- (g) What is the average value of all the residuals? Is this value surprising?

```
mean(linear_model$residuals)
```

```
## [1] -2.612204e-16
```

The average value of all the residuals $E(e_i) = -2.612 \times 10^{-16} \text{ min} \approx 0 \text{ min}$. This value is unsurprising and confirms our assumption that errors / residuals between actual and predicted times spent servicing have a mean of 0 min.

2. A substance used in biological and medical research is shipped by airfreight to users in cartons of 1000 ampules. The sample consists of 10 shipments. A variable $x = \text{transfer}$ represents the number of times a carton was transferred from one aircraft to another during the shipment route. A variable $y = \text{broken}$ represents the number of ampules found to be broken upon arrival. A simple linear regression model is fitted using R. The corresponding output from R is shown next, with some values missing.

Call:

```
lm(formula = broken ~ transfer)
```

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	10.2000	0.6633	-----	----- ***
transfer	4.0000	0.4690	-----	----- ***

Residual standard error: 1.483 on 8 degrees of freedom

...

Analysis of Variance Table

Response: broken

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
transfer	1	160.0	160.0	-----	----- ***
Residuals	8	17.6	2.2		

The following values are also provided for you.

$$\bar{x} = 1$$

$$\sum_{i=1}^{n=10} [(x_i - \bar{x})^2] = 10$$

- (a) Carry out a hypothesis test to assess if there is a linear relationship between the variables $y = \text{broken}$ and $x = \text{transfer}$.

The regression mean square

$$MS_R = \frac{SS_R}{df_R} = \frac{160.0}{1} = 160.0$$

Errors / residuals are assumed to be normally and independently distributed with mean 0 and unknown constant variance σ^2 . The residual standard error and estimated standard deviation of errors / residuals $\hat{\sigma} = 1.483 \text{ min}$. The residual mean square and estimated variance of errors / residuals

$$MS_{Res} = \hat{\sigma}^2 = (1.483 \text{ min})^2 = \frac{SS_{Res}}{df_{Res}} = \frac{SS_{Res}}{n - p} = \frac{SS_{Res}}{n - 2} = \frac{17.6}{8} = 2.2$$

By definition of a test statistic,

$$t_{\hat{\beta}_1, \beta_{10}, SE(\hat{\beta}_1)} = \frac{\hat{\beta}_1 - \beta_{10}}{SE(\hat{\beta}_1)} = \frac{\hat{\beta}_1 - \beta_{10}}{\sqrt{MS_{Res}/S_{xx}}}$$

follows a $[t_{df_{Res}} = t_{n-p} =] t_{n-2}$ distribution if the null hypothesis $H_0 : \beta_1 = \beta_{10}$ is true.

$$t_{\hat{\beta}_1, \beta_{10}, SE(\hat{\beta}_1)} = \frac{\hat{\beta}_1 - \beta_{10}}{SE(\hat{\beta}_1)} = \frac{\hat{\beta}_1 - 0}{SE(\hat{\beta}_1)} = \frac{\hat{\beta}_1}{SE(\hat{\beta}_1)} = \frac{4.0000}{0.4690} = 8.528$$

$$t_{\hat{\beta}_1, \beta_{10}, SE(\hat{\beta}_1)} = \sqrt{\frac{\hat{\beta}_1^2}{SE(\hat{\beta}_1)^2}} = \sqrt{\frac{\hat{\beta}_1^2}{MS_{Res}/S_{xx}}} = \sqrt{\frac{\hat{\beta}_1^2 S_{xx}}{MS_{Res}}} = \sqrt{\frac{\hat{\beta}_1 S_{xy}}{MS_{Res}}} = \sqrt{F_0}$$

$$t_{\hat{\beta}_1, \beta_{10}, SE(\hat{\beta}_1)} = \sqrt{\frac{MS_R}{MS_{Res}}} = \sqrt{\frac{160.0}{2.2}} = 8.528$$

The quantile of a Student's t probability distribution with $df_{Res} = n - p = n - 2$ degrees of freedom for which the probability that a random test statistic is greater is equal to the significance level $\alpha = 0.05$

$$t_{\alpha, df_{Res}} = qt(\alpha, df_{Res}, lower.tail = FALSE) = 1.860$$

The quantile of a Student's t probability distribution with $df_{Res} = n - p = n - 2$ degrees of freedom for which the probability that a random test statistic is greater is equal to half the significance level $\alpha = 0.05$

$$t_{\alpha/2, df_{Res}} = qt(\alpha/2, df_{Res}, lower.tail = FALSE) = 2.306$$

```
significance_level <- 0.05
number_of_observations <- 10
number_of_parameters <- 2
degrees_of_freedom <- number_of_observations - number_of_parameters
qt(significance_level, degrees_of_freedom, lower.tail = FALSE)
```

```
## [1] 1.859548
```

```
qt(significance_level / 2, degrees_of_freedom, lower.tail = FALSE)
```

```
## [1] 2.306004
```

Given a significance level $\alpha = 0.05$, we test a null hypothesis $H_0 : \beta_1 = 0$ that the slope of a linear model for the number of broken ampules, $y = \text{broken}$, vs. the number of transfers, $x = \text{transfer}$, is equal to 0. If we have sufficient evidence to reject the null hypothesis, we have sufficient evidence to support an alternate hypothesis $H_1 : \beta_1 \neq 0$ that the slope of the linear

model for the number of broken ampules vs. the number of transfers is not equal to 0. Since the alternate hypothesis H_1 involves “ \neq ”, we have sufficient evidence to reject the null hypothesis if the magnitude $\left|t_{\hat{\beta}_1, \beta_{10}, SE(\hat{\beta}_1)}\right|$ is greater than the quantile $t_{\alpha/2, df_{Res}}$. If the alternative H_1 were to involve “ $<$ ” or “ $>$ ”, we would have sufficient evidence to reject the null hypothesis if the magnitude $\left|t_{\hat{\beta}_1, \beta_{10}, SE(\hat{\beta}_1)}\right|$ is greater than $t_{\alpha, df_{Res}}$. Since $\left|t_{\hat{\beta}_1, \beta_{10}, SE(\hat{\beta}_1)}\right| > t_{\alpha/2, df_{Res}}$, we reject the null hypothesis. We have sufficient evidence to support the alternate hypothesis.

We have sufficient evidence to reject the null hypothesis if the probability p that a the test statistic for a random sample of shipments is less than $-|t_{\hat{\beta}_1, \beta_{10}, SE(\hat{\beta}_1)}|$ or greater than $|t_{\hat{\beta}_1, \beta_{10}, SE(\hat{\beta}_1)}|$, assuming the null hypothesis is true, is less than significance level α .

```
p <- pt(8.528, degrees_of_freedom, lower.tail = FALSE) * 2
# 2 if the alternate hypothesis involves "\neq"
# 1 if the alternate hypothesis involves "<" or ">"
p
```

```
## [1] 2.748737e-05
```

Since $p < \alpha$, we reject the null hypothesis. We have sufficient evidence to support the alternate hypothesis.

- (b) Calculate a 95 percent confidence interval that estimates the unknown slope of the linear model that fits observations / ($x = transfer, y = broken$) matched pairs of data for a population of shipments.

The estimated slope

$$\hat{\beta}_1 = 4.0000$$

The standard error of the estimated slope

$$SE(\hat{\beta}_1) = 0.4690$$

The 95 percent confidence interval that estimates the unknown slope of the linear model that fits observations for a population of shipments

$$\begin{aligned} & \left[\hat{\beta}_1 - t_{\alpha/2, df_{Res}} SE(\hat{\beta}_1), \hat{\beta}_1 + t_{\alpha/2, df_{Res}} SE(\hat{\beta}_1) \right] \\ & [(4.0000) - (2.306)(0.4690), (4.0000) + (2.306)(0.4690)] \\ & [2.918, 5.082] \end{aligned}$$

- (c) A consultant believes the mean number of broken ampules when no transfers are made is different from 9. Conduct an appropriate hypothesis test. State the hypotheses, calculate the test statistic, and write the corresponding conclusion in context, in response to his belief.

The estimated expected value of the number of broken ampules y given the number of transfers $x_0 = 0$

$$E(\widehat{y|x_0=0}) = 10.2000$$

The assumed expected value of the number of broken ampules y given the number of transfers $x_0 = 0$

$$E(y|x_0=0) = 9$$

The standard error of the estimated expected value of the number of broken ampules y given the number of transfers $x_0 = 0$

$$SE\left\{E(\widehat{y|x_0=0})\right\} = 0.6633$$

By definition of a test statistic,

$$t_{\hat{E}, E, SE(\hat{E})} = \frac{\widehat{E(y|x_0)} - E(y|x_0)}{SE\{\widehat{E(y|x_0)}\}} = \frac{\widehat{E(y|x_0)} - E(y|x_0)}{\sqrt{MS_{Res} \left[\frac{1}{n} + \frac{(x_0 - \bar{x})^2}{s_{xx}} \right]}} = \frac{\widehat{E(y|x_0)} - E(y|x_0)}{\sqrt{MS_{Res} \left[\frac{1}{n} + \frac{(x_0 - \bar{x})^2}{\sum_{i=1}^{n=10} [(x_i - \bar{x})^2]} \right]}}$$

follows a $[t_{df_{Res}} = t_{n-p} =] t_{n-2}$ distribution if the null hypothesis $H_0 : E(y|x_0) = \mu$ is true.

$$t_{\hat{E}, E, SE(\hat{E})} = \frac{\widehat{E(y|x_0=0)} - E(y|x_0=0)}{SE\{\widehat{E(y|x_0=0)}\}} = \frac{10.2000 - 9}{0.6633} = \frac{10.2000 - 9}{\sqrt{2.2 \left[\frac{1}{10} + \frac{(0-1)^2}{10} \right]}} = 1.809$$

Given a significance level $\alpha = 0.05$, we test a null hypothesis $H_0 : E(y|x_0 = 0) = 9$ that the mean number of broken ampules when 0 transfers are made is equal to 9. If we have sufficient evidence to reject the null hypothesis, we have sufficient evidence to support an alternate hypothesis $H_1 : E(y|x_0 = 0) \neq 9$ that the mean number of broken ampules when 0 transfers are made is not equal to / different from 9. Since the alternate hypothesis H_1 involves “ \neq ”, we have sufficient evidence to reject the null hypothesis if the magnitude $|t_{\hat{E}, E, SE(\hat{E})}|$ is greater than the quantile $t_{\alpha/2, df_{Res}}$. If the alternative H_1 were to involve “ $<$ ” or “ $>$ ”, we would have sufficient evidence to reject the null hypothesis if the magnitude $|t_{\hat{E}, E, SE(\hat{E})}|$ is greater than $t_{\alpha, df_{Res}}$. Since $|t_{\hat{E}, E, SE(\hat{E})}| < t_{\alpha/2, df_{Res}}$, we fail reject the null hypothesis. We have insufficient evidence to support the alternate hypothesis.

We have sufficient evidence to reject the null hypothesis if the probability p that a the test statistic for a random sample of shipments is less than $-|t_{\hat{E}, E, SE(\hat{E})}|$ or greater than $|t_{\hat{E}, E, SE(\hat{E})}|$, assuming the null hypothesis is true, is less than significance level α .

```
p <- pt(1.809, degrees_of_freedom, lower.tail = FALSE) * 2
# 2 if the alternate hypothesis involves "\neq"
# 1 if the alternate hypothesis involves "<" or ">"
p
```

```
## [1] 0.1080558
```

Since $p > \alpha$, we fail to reject the null hypothesis.

- (d) Calculate a 95 percent confidence interval for the mean number of broken ampules and a 95 percent prediction interval for the number of broken ampules when the number of transfers is 2.

The estimated expected value of the number of broken ampules y given the number of transfers $x_0 = 2$

$$E(\widehat{y|x_0=2}) = \hat{\beta}_0 + \hat{\beta}_1 x_0 = (10.2000) + (4.0000)(2) = 18.2000$$

The standard error of the estimated expected value of the number of broken ampules y given the number of transfers $x_0 = 2$

$$SE\{\widehat{E(y|x_0=2)}\} = \sqrt{MS_{Res} \left[\frac{1}{n} + \frac{(x_0 - \bar{x})^2}{\sum_{i=1}^{n=10} [(x_i - \bar{x})^2]} \right]} = \sqrt{2.2 \left[\frac{1}{10} + \frac{(2-1)^2}{10} \right]} = 0.6633$$

A 95 percent confidence interval for the mean number $E(y|x_0 = 2)$ of broken ampules when the number of transfers $x_0 = 2$

$$\left[\widehat{E(y|x_0=2)} - t_{\alpha/2, df_{Res}} SE\{\widehat{E(y|x_0=2)}\}, \widehat{E(y|x_0=2)} + t_{\alpha/2, df_{Res}} SE\{\widehat{E(y|x_0=2)}\} \right]$$

$$[18.2000 - (2.306)(0.6633), 18.2000 + (2.306)(0.6633)]$$

$$[16.670, 19.730]$$

The predicted number of broken ampules given the number of transfers $x_0 = 2$

$$\hat{y}_{x_0=2} = \hat{\beta}_0 + \hat{\beta}_1 x_0 = 18.2000$$

The standard error of the predicted number of broken ampules given the number of transfers $x_0 = 2$

$$SE(\hat{y}_{x_0=2}) = \sqrt{MS_{Res} \left[1 + \frac{1}{n} + \frac{(x_0 - \bar{x})^2}{\sum_{i=1}^{n=10} [(x_i - \bar{x})^2]} \right]} = \sqrt{2.2 \left[1 + \frac{1}{10} + \frac{(2 - 1)^2}{10} \right]} = 1.625$$

A 95 percent prediction interval for the number of broken ampules when the number of transfers $x_0 = 2$

$$[\hat{y}_{x_0=2} - t_{\alpha/2, df_{Res}} SE(\hat{y}_{x_0=2}), \hat{y}_{x_0=2} + t_{\alpha/2, df_{Res}} SE(\hat{y}_{x_0=2})]$$

$$[(18.2000) - (2.306)(1.625), (18.2000) + (2.306)(1.625)]$$

$$[14.453, 21.947]$$

- (e) What happens to the intervals from part d when the number of transfers is 1?

When the number of transfers becomes $x_0 = 1$, a term in the formulas for the standard error of the estimated expected value of the number of broken ampules y given the number of transfers $x_0 = 2$, and the standard error of the predicted value of the number of broken ampules given the number of transfers $x_0 = 2$, become 0. These standard errors becomes smaller, the corresponding margins of error becomes smaller, and the intervals narrow.

- (f) What is the value of the F statistic for the ANOVA table?

As suggested in part a,

$$F_0 = t_{\hat{\beta}_1, \beta_{10}, SE(\hat{\beta}_1)}^2 = \frac{160.0}{2.2} = 72.727$$

- (g) Calculate the value of R^2 .

$$SS_R = 160.0$$

$$SS_{Res} = 17.6$$

$$SS_T = SS_R + SS_{Res} = 160.0 + 17.6 = 177.6$$

$$R^2 = \frac{SS_R}{SS_T} = \frac{160.0}{177.6} = 0.901$$

$$R = +\sqrt{R^2} = \sqrt{0.901} = 0.949$$

We assume that the sample of shipments is simple random. We assume that (x = transfer, y = broken) matched pairs of data for the shipments are independent. We assume that errors / residuals between actual and predicted numbers of broken ampules are normally and independently distributed with mean 0 and constant variance. The linear model for number of broken ampules vs. number of transfers has an adjusted sample linear Pearson coefficient coefficient $R = 0.949$. The adjusted sample linear Pearson correlation coefficient measures the strength of the linear relationship between (x = transfer, y = broken) matched pairs of data for the sample of shipments. The linear model has a positive linear Pearson correlation. The value of the adjusted sample linear Pearson correlation coefficient lies between -1 and 1 inclusive. Assuming the simple linear regression was fitted to (x = transfer, y = broken) matched pairs of data for the shipments after

a scatterplot of the matched pairs showed a reasonable linear association, the adjusted sample linear Pearson correlation coefficient is reliable. Since the above probability $p = 2.749 \times 10^{-5}$ is less than a significance level $\alpha = 0.05$, we rejected a null hypothesis of a linear regression t test that there is no correlation between number of ampules broken and number of transfers, and concluded that there is a correlation between number of ampules broken and number of transfers. The linear model has an adjusted sample coefficient of determination of $R^2 = 0.901$. The adjusted sample coefficient of determination is the proportion of variation in number of ampules broken that is explained by the linear relationship / number of transfers. The adjusted sample coefficient of determination lies between 0 and 1. Since the adjusted sample coefficient of determination is greater than 0.8, the linear model is precise and good for prediction.

3. Suppose that the slope of the linear model that fits observations / (x, y) matched pairs of data for a population is 0.

- (a) Describe how the linear model would look in a plot of y versus x .

In a scatterplot of observations / (x, y) matched pairs of data for a population and a fitted linear model with slope 0, the linear model would look horizontal.

- (b) Explain why a slope that is equal to 0 would indicate that y and x are not linearly related, and why a slope that is not equal to 0 would indicate that y and x are linearly related.

A slope that is equal to 0 indicates that y and x are not linearly related because a slope that is equal to 0 implies either that x is of little value in explaining the variation in y and that the best estimator of y for any x is $\hat{y} = \bar{y}$, or that the true relationship between x and y is not linear.

A slope that is not equal to 0 indicates that y and x are linearly related because a slope that is not equal to 0 implies that x is of value in explaining the variability in y . However, a slope that is not equal to 0 could mean either that a linear model is adequate or, that even though there is a linear effect of x , better results could be obtained with the addition of higher order polynomial terms in x .