6 Forces in Equilibrium

6.1 Vectors and Scalars

- A **vector** is any physical quantity that has a direction as well as a magnitude.
 - Displacement, velocity, acceleration, force.
- A scalar is any physical quantity that is not directional.
 - Mass, density, volume, energy.

A vector can be **represented as an arrow** - the length of the arrow represents the magnitude of the vector quantity, the direction arrow gives the direction of the vector.

Distance travelled depends on the route, whereas the direct distance is always the same.

- **Displacement** is distance in a given direction.
- Velocity is speed in a given direction.

Vector Addition

Vectors can be added using a scale diagram.

$$OB = OA + AB$$

Vector addition gives the **overall effect** of the vectors. Adding two forces gives the **resultant** of the forces.

• The **resultant** is the combined effect of two forces.

Vectors can also be added using a calculator.

In general, if the two perpendicular forces are F_1 and F_2

- The **magnitude** of the resultant $F = \sqrt{{F_1}^2 + {F_2}^2}$
- The angle θ between the resultant and F_1 is given by $\tan \theta = F_2/F_1$.

Resolving a Vector into Two Perpendicular Components

Is the process of working out the **components of a vector** in two perpendicular directions given the magnitude and direction of the vector.

A force F can be resolved into two perpendicular components

- $F\cos\theta$ parallel to a line at angle θ to the line of action of the force.
- $F \sin \theta$ perpendicular to the line.