

3 Data Representation

3.13 Numbering Systems

- An **integer** is any whole number.
 $\mathbb{Z} = \{\dots, -2, -1, 0, 1, 2, \dots\}$
- A **natural number** is a whole number that is used for counting.
 $\mathbb{N} = \{0, 1, 2, \dots\}$
- A **rational number** is any value that can be expressed as a fraction.
 \mathbb{Q}
- An **irrational number** cannot be expressed as a fraction, and has an endless series of non-repeating digits.

An irrational number cannot be correctly represented using a finite number of digits, therefore a **rounding error** will occur.

A **real number** is any natural, rational or irrational number. The **set of real numbers** \mathbb{R} is defined as the set of all possible real world quantities.

Ordinal numbers describe the numerical position of objects - first, second, etc.

- Natural numbers are used for **counting**.
- Real numbers are used for **measurement**.
- Ordinal numbers are used as **pointers** to a particular element in a sequence, or to define the position of something in a list.

Number Bases

- **Denary** uses the digits 0 through 9 and has a base of 10.
- **Binary** uses only the digits 0 and 1 and has a base of 2.
- **Hexadecimal** uses digits 0-9 and letters A to F and has a base of 16.

The numbering base can be written as a subscript 11_{16} .

The hexadecimal system is used as the **shorthand for binary**, since

- It is simple to represent a byte in just two digits.
- **Fewer mistakes** are likely to be made in writing a hex number than a string of binary digits.
- It is easier for computer users to **remember a hex number** than a binary number.

Colour codes often use hexadecimal to represent the RGB values, as their are easier to remember than a 24-bit binary string.

3.14 Bits, Bytes and Binary

- A **bit** is the **fundamental unit of information** in the form of either a single 1 or 0.
- A **byte** is a set of eight bits.
- A **nibble** is a set of four bits.

The number of values that can be represented with n bits is 2^n .

A **kibibyte** KiB is 1024 bytes, whereas a **kilobyte** KB is 1000 bytes.

Character Sets

ASCII (Americal standard code for information interchange) is a code for **representing characters** on the keyboard.

- Uses 7 bits which form 128 different **bit combinations**.
- The first 32 codes represent **non-printing characters** used for control, such as backspace, enter, escape, etc.
- An 8-bit version **extended ASCII** was developed to include an additional 128 combinations.

By the 1980s, several coding systems had been introduced all around the world that were all **incompatible with one another**. A new 16-bit code called the **Unicode** (UTF-16) was introduced

- Allows for 65,536 different combinations that could represent alphabets from dozens of languages.
- The first 128 codes were the **same as ASCII** so compatibility was retained.
- A further version of Unicode called UTF-32 was developed to include just over a million character - more than enough to handle most of the characters from **all the languages**.

Unicode encodings take **more storage space** than ASCII, significantly **increasing file sizes** and transmission times.

Error Checking and Correction

Bits can change erroneously during transmission owing to **interference**.

- A **parity bit** is an additional bit used to check that the other bits transmitted are likely to be correct.
- **Majority voting** is a system that requires each bit to be sent three times.

If a bit value is flipped erroneously during transmission, the recipient computer would use the **majority rule** and assume that the two bits that have not been changed is correct.

Majority voting **triples the volume of data** that is sent.

- A **checksum** is a mathematical algorithm that is applied to a unit of data.
 1. The data in the block is used to **create a checksum** value, which is **transmitted with the block**.
 2. The same algorithm is applied to the block after transmission.
 3. If the **two checksums match**, the transmission is deemed successful.

Otherwise, an error must have occurred during transmission, and the block should be **transmitted again**.

- A **check digit** is an additional digit at the end of a string designed to check for mistakes in an **input or transmission**.

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