

Discrete Mathematics

Discrete mathematics deals with finite or countably infinite sets, this includes integers and related concepts.

Definitions

Keyword	Definition
Statement	Something that is either true or false.
Predicate	A statement whose truth depends on one or more variables.
Theorem	An important true statement.
Proposition	A less important true statement.
Lemma	A statement used to prove other true statements.
Corollary	A true statement that is a simple deduction from a theorem or proposition.
Conjecture	A statement believed to be true, but not proved yet.
Proof	A way to show a statement is true.
Logic	The study of methods and principles used to distinguish correct reasoning from incorrect reasoning.
Axiom	A basic assumption about a mathematical situation.
Definition	An explanation of the mathematical meaning of a word.
Simple statement	A simple statement cannot be broken down.
Composite statement	A composite statement is built using several other statements connected by logical expressions.

Proof Structure

Definitions

Keyword	Definition
Assumptions	Statements that may be used for deduction.
Goals	Statements to be established.

Start by listing out assumptions and write down the goal.

Implication

collection of hypotheses \implies some conclusion

To prove $P \implies Q$

- Add P to the list of assumptions.
- Replace $P \implies Q$ in goal with Q .

Types of Real Numbers

Definitions

Keyword	Definition
Rational	A number is rational if it is in form m/n for some integer m, n , otherwise it is irrational.
Positive	A number is positive if it is greater than 0, otherwise it is nonpositive.
Negative	A number is negative if it is less than 0, otherwise it is nonnegative.
Natural	A number is natural if it is a nonnegative integer.

Modus Ponens (Implication Elimination)

The main rule for logical deduction is

- From statements P and $P \Rightarrow Q$.
- Q follows.

$$\frac{P \quad P \Rightarrow Q}{Q}$$

Bi-implications

Some theorems are in form $P \Leftrightarrow Q$, to prove it

- Prove $P \Rightarrow Q$
 - Prove $Q \Rightarrow P$
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