## FORMULAS – Final Exam

Conversion Factors: 1 inch = 2.54 cm; 1 mi = 1609.3 m; 1 cm= $10^{-2}$ ; 1 mm=  $10^{-3}$  m; 1 g= $10^{-3}$  kg; **Physical constants:**  $g = 9.8 \text{ m/s}^2$ ;  $G = 6.674 \times 10^{-11} \text{ N m}^2/\text{kg}^2$ ;  $M_{Earth} = 5.97 \times 10^{24} \text{ kg}$ ;  $R_{Earth} = 6.37 \times 10^6 \text{ m}$ **Math:**  $360^{\circ} = 2\pi \text{ radians} = 1 \text{ revolution}$ . Arc length  $s = r\theta$ ;  $V_{sphere} = 4\pi R^3 / 3$ ;  $A_{sphere} = 4\pi R^2$ ;  $A_{circle} = \pi R^2$ quadratic formula to solve  $ax^2 + bx + c = 0$ :  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ 

**Vectors:** 
$$\vec{A} = A_x \hat{i} + A_y \hat{j}$$
;  $A_x = |\vec{A}| \cos(\theta)$ ;  $A_y = |\vec{A}| \sin(\theta)$ ;  $|\vec{A}| = \sqrt{A_x^2 + A_y^2}$ ;  $\tan \theta = \frac{A_y}{A_x}$   
 $\vec{C} = \vec{A} + \vec{B}$  implies  $C_x = A_x + B_x$ ;  $C_y = A_y + B_y$   
 $\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos(\theta) = A_x B_x + A_y B_y + A_z B_z$ ;  $\hat{i} \cdot \hat{i} = \hat{j} \cdot \hat{j} = \hat{k} \cdot \hat{k} = 1$ ;  $\hat{i} \cdot \hat{j} = \hat{i} \cdot \hat{k} = \hat{j} \cdot \hat{k} = 0$   
 $|\vec{A} \times \vec{B}| = |\vec{A}| |\vec{B}| \sin \theta$ ;  $\vec{A} \times \vec{B} = \hat{i} (A_y B_z - A_z B_y) + \hat{j} (A_z B_x - A_x B_z) + \hat{k} (A_x B_y - A_y B_x)$   
 $\hat{i} \times \hat{i} = \hat{j} \times \hat{j} = \hat{k} \times \hat{k} = 0$ ;  $\hat{i} \times \hat{j} = \hat{k}$ ;  $\hat{j} \times \hat{k} = \hat{i}$ ;  $\hat{k} \times \hat{i} = \hat{j}$ 

## 1D and 2D motion:

$$\vec{v}_{avg} = \frac{\Delta \vec{r}}{\Delta t} \quad ; \quad \vec{a}_{avg} = \frac{\Delta \vec{v}}{\Delta t} \quad ; \quad \vec{v} = \frac{d\vec{x}}{dt} \quad ; \quad \vec{a} = \frac{d\vec{v}}{dt} = \frac{d^2\vec{r}}{dt^2}$$

$$x = x_i + v_i t + \frac{1}{2}at^2 \quad ; \quad v = v_i + at \quad ; \quad v^2 = v_i^2 + 2a(x - x_i) \quad ; \quad \vec{r} = \vec{r}_i + \vec{v}_i t + \frac{1}{2}\vec{a}t^2 \quad ; \quad \vec{v} = \vec{v}_i + \vec{a}t$$

**Circular motion:**  $T = 2\pi R / v$ ;  $T = 2\pi / \omega$ ;  $a_c = v^2 / R$ 

Newtons Laws: 
$$\sum \vec{F} = m\vec{a}$$
 ;  $\vec{F}_{12} = -\vec{F}_{21}$ 

**Friction:** 
$$f_s \le \mu_s N$$
;  $f_k = \mu_k N$ 

$$\begin{array}{lll} \textbf{Friction:} & f_{\scriptscriptstyle S} \leq \mu_{\scriptscriptstyle S} N \ ; & f_{\scriptscriptstyle k} = \mu_{\scriptscriptstyle k} N \\ \textbf{Energies:} & K = \frac{1}{2} m v^2 \ ; & U_{\scriptscriptstyle g} = m g y \ ; & U_{\scriptscriptstyle S} = \frac{1}{2} k x^2 \ ; W = -\int \vec{F} \cdot d\vec{r} = -\vec{F} \cdot \Delta \vec{r} \\ E_{\scriptscriptstyle total} = K + U_{\scriptscriptstyle g} + U_{\scriptscriptstyle S} \ ; & \Delta E_{\scriptscriptstyle mech} = \Delta K + \Delta U_{\scriptscriptstyle g} + \Delta U_{\scriptscriptstyle s} = -f_{\scriptscriptstyle s} d \quad ; & P = \frac{\mathrm{d} W}{\mathrm{d} t} = \vec{F} \cdot \vec{v} \quad ; & \Delta K = W \\ \end{array}$$

**Momentum and Impulse:** 
$$\vec{p} = m\vec{v}$$
 ;  $\vec{I} = \int \vec{F} dt = \Delta \vec{p}$ 

Center of mass: 
$$\vec{r}_{cm} = \sum_{i} m_i \vec{r}_i / \sum_{i} m_i$$
;  $\vec{v}_{cm} = \sum_{i} m_i \vec{v}_i / \sum_{i} m_i$ 

**Collisions:** 
$$\vec{p} = \text{const}$$
 and  $E \neq \text{const}$  (inelastic) or  $\vec{p} = \text{const}$  and  $E = \text{const}$  (elastic)

**Rotational motion:** 
$$\omega = 2\pi/T$$
 ;  $\omega = d\theta/dt$  ;  $\alpha = d\omega/dt$  ;  $v_t = r\omega$  ;  $a_t = r\alpha$   $a_c = a_r = v_t^2/r = \omega^2 r$ 

$$a_{tot}^2 = a_r^2 + a_t^2$$
;  $v_{cm} = r\omega$  (rolling, no slipping);  $a_{cm} = r\alpha$ 

$$\omega = \omega_o + \alpha t$$
;  $\theta_f = \theta_i + \omega_o t + \alpha t^2 / 2$ ;  $\omega_f^2 = \omega_i^2 + 2\alpha(\theta_f - \theta_i)$ 

$$I_{point} = MR^2 \; ; \; I_{hoop} = MR^2 \; ; \; I_{disk} = MR^2 \; / \; 2 \; ; \; I_{sphere} = 2MR^2 \; / \; 5 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{sphere} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 12 \; ; \; I_{shell} = 2MR^2 \; / \; 3 \; ; \; I_{rod(center)} = ML^2 \; / \; 3 \; ; \; I_$$

$$I_{rod(end)} = ML^2/3 \; ; \; I = \sum_i m_i r_i^2 \; ; \; I = I_{cm} + Mh^2 \; ; \; \vec{\tau} = \vec{r} \times \vec{F} \; ; \; \sum \tau = I\alpha \; ; \; \vec{L} = \vec{r} \times \vec{p} \; ; \; \vec{L} = I\vec{\omega}$$

**Energy:** 
$$K_{rot} = I\omega^2/2$$
;  $K = K_{rot} + K_{cm}$ ;  $\Delta K + \Delta U = 0$ ;  $W = \tau \Delta \theta$ ;  $P_{inst} = \tau \omega$ 

Fluid: 
$$\rho = \frac{M}{V}$$
;  $P = P_0 + \rho g h$ ;  $A_1 v_1 = A_2 v_2$ ;  $P_1 + \rho g y_1 + \frac{1}{2} \rho v_1^2 = P_2 + \rho g y_2 + \frac{1}{2} \rho v_2^2$ 

Gravitation: 
$$\vec{F}_g = -\frac{Gm_1m_2}{r^2}\hat{r}_{12}$$
;  $g(r) = GM/r^2$ ;  $U = -Gm_1m_2/r$ ;  $T^2 = \frac{4\pi^2}{GM}a^3$ 

**Oscillatory motion:** 
$$=\frac{1}{2\pi}\sqrt{\frac{k}{M}}$$
;  $f=\frac{1}{2\pi}\sqrt{\frac{g}{L}}$ ;  $x(t)=Acos(\omega t+\phi)$ ;  $v(t)=\frac{dx}{dt}$ ;  $a(t)=\frac{dv}{dt}$ ;  $E=\frac{1}{2}kA^2$