Computational Causal Discovery

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Computational Causal Discovery

Discoverying Causal Structure From Observational Data

Applications of Causal Discovery

Computational Causal Discovery and its Applications

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University of Minnesota

April 6, 2019

Computational Causal Analytics at U of Minnesota

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Discoverying Causal Structure From Observationa Data

Applications of Causal Discovery Constantin Aliferis, Professor, Director of IHI at UMN



Gyorgy Simon, Associate Professor



Computational Causal Analytics at U of Minnesota

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Applications of Causal Discovery Methods Erich Kummerfeld, Assisstant Professor



Sisi Ma, Assisstant Professor



Where to find material related to this talk?

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Applications of Causal Discovery github.com/SisiMa1729/CausalAnalytics_Intro
github.com/SisiMa1729/Causal_Feature_Selection

Overview

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Discoverying Causal Structure From Observationa Data

Applications of Causal Discovery Methods 1 Computational Causal Discovery

2 Discoverying Causal Structure From Observational Data

What is Computational Causal Discovery?

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Applications of Causal Discovery

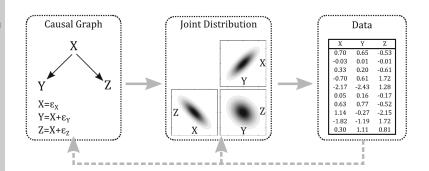
- Discovery of Causal Structure
- Estimation of Causal Effect
- Using a combination of observational data, experimental data, and prior knowledge.

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Estimation of Causal Effect

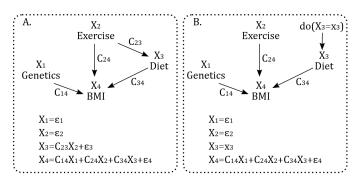
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Causal Structure From Observational Data

Applications of Causal Discovery Methods E(Y|do(X=x)) - E(Y|do(X=x')) is the average effect on Y when changing X from x to x'



* comment: SEM?

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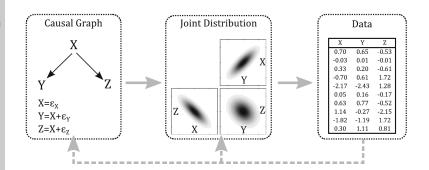
Applications of Causal Discovery Correct effect estimation depends on identifying the correct causal structure.

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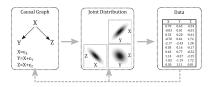


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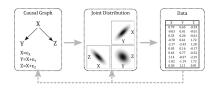
- score based method (maximize likelihood of data given causal structure)
- constraint-based (joint distribution of data is constrained by causal structure)
- hybrid of the above two

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- score based method (maximize likelihood of data given causal structure)
- constraint-based (joint distribution of data is constrained by causal structure)
- hybrid of the above two

Discovery of Causal Structures: Assumptions

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Applications of Causal Discovery Causal Markovian Condition: Every Markovian causal model M induces a distribution $P(X_1,...X_i,...,X_n)$ that satisfies the parental Markov condition relative to to causal diagram G associated with M; that is, each variable X_i is independent of all its nondescendants, given its parents in G. i.e. $X_i \perp V - DE_i|PA_i$

Discovery of Causal Structures: Assumptions

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Applications of Causal Discovery Faithfulness Condition: Let G be a causal graph and P a probability distribution generated by G. G and P satisfies the faithfulness condition if and only if every conditional independence true in P is entailed by the Causal Markovian condition applied to G.

Discovery of Causal Structures: Assumptions

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Applications of Causal Discovery Intuitively, causal Markov condition and faithfullness condition establish a one to one relationship between the causal graph (more precisely, Markov equivalent class) and the joint probablity distribution. This correspondance makes causal discovery possible.

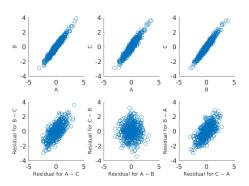
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Applications of Causal Discovery Methods Conditional independence, What does it look like: A - > B - > C: A < -B < -C: or A < -B - > C



 $A \not\perp B, A \not\perp C, B \not\perp C$ $A \not\perp B|C, A \perp C|B, B \not\perp C|A$

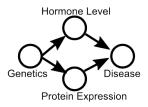
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The concept of conditional independence:

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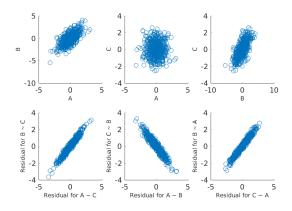
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Applications of Causal Discovery Methods Conditional independence, What does it look like:

$$A->B<-C$$



 $A \not\perp B, A \perp C, B \not\perp C$ $A \not\perp B|C, A \not\perp C|B, B \not\perp C|A$



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Applications of Causal Discovery Methods

Conditional Independence Tests:

- fisher's test
- \blacksquare χ^2 , g^2
- conditional mutual information, distance correlation
- comparison of nested models

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Applications of Causal Discovery Methods The demonstrated relationships among three variables can be extended to discover causal graphs among any number of variables. Some popular algorithms:

■ constraint based: SGS, PC, HITON-PC, FCI

■ score based: GES, FGES

■ hybrid: MMHC,GFCI

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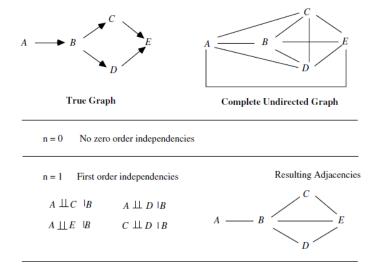
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Applications of Causal Discovery Methods

Example: PC algorithm: Skeleton Phase:



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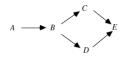
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Applications of Causal Discovery Methods

Example: PC algorithm:



True Graph

Skeleton Phase (continued):

n = 2: Second order independencies

$$B \perp \!\!\!\perp E + \{C,D\}$$

Resulting Adjacencies

$$A \longrightarrow B \longrightarrow E$$

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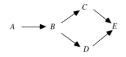
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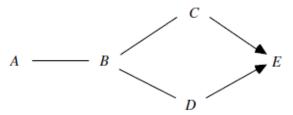
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${\sf Example:\ PC\ algorithm:}$



True Graph

Orientation Phase:



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Discoverying Causal Structure From Observational Data

- Causal Mechanism from Observational Data
- Causal Graph Guided Experimentation
- Causal Feature Selection

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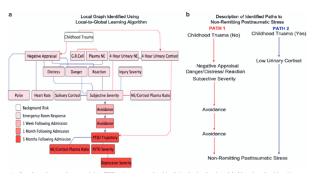
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Causal Structure From Observationa

Applications of Causal Discovery Methods

Biological Mechanisms of PTSD:



[Galatzer-Levy et al., 2017]

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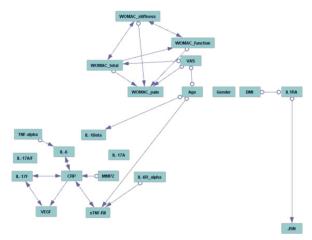
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Biological Mechanisms of Osteoarthritis:



Causal Graph Guided Experimentation

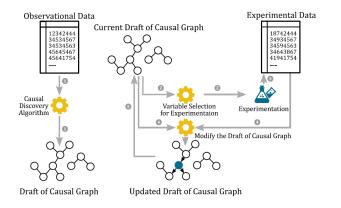
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Applications of Causal Discovery Methods Reduce number of Experiments needed to fully resolve the causal relations



[Statnikov et al., 2015]

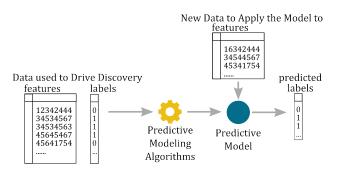
Causal Feature Selection for Predictive Models

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Causal Feature Selection for Predictive Models

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Applications of Causal Discovery Methods

Goals of Feature Selection:

- Improve model predictivity
- Enhance model interpretability
- Increase cost-efficiency for model deployment

Causal feature selection is well-suited for these goals.

Optimal Feature Set

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Applications of Causal Discovery Methods **Optimal feature set**: Given a data set \mathbb{D} (a sample from distribution \mathbb{P}) for variables \mathbf{V} , a learning algorithm \mathbb{L} , and a performance metric \mathbb{M} , a feature set $\mathbf{X} \subseteq \mathbf{V}$ is an optimal feature set of T if \mathbf{X} maximizes the performance metric \mathbb{M} for predicting T using learner \mathbb{L} in the dataset \mathbb{D} . [Statnikov et al., 2013, Kohavi and John, 1997] Note: Optimal here is defined with respect to predictivity. There could be redundent features in a optimal feature set according to this definition.

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Applications of Causal Discovery Methods The contribution of a given feature to the predictive performance of a model depends on what other features are present in the model.

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Applications of Causal Discovery Methods Let $\mathbf{S_i} = \mathbf{V} - V_i$, the set of all features except V_i **Strong relevance**: A feature V_i is strongly relevant to T iff there exists some v_i , t, and s_i for which $p(V_i = v_i, \mathbf{S_i} = s_i) > 0$, such that $p(T = t | V_i = v_i, \mathbf{S_i} = s_i) \neq p(T = t | \mathbf{S_i} = s_i)$. [Kohavi and John, 1997]

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Applications of Causal Discovery Methods Strongly relevant features are conditionally dependent of T given all other measured variables. In other words, knowing the value of features V_i gives additional information regarding the target of interest, even when we know the value of all other features.

[Kohavi and John, 1997]

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Applications of Causal Discovery Methods Let $\mathbf{S_i} = \mathbf{V} - V_i$, the set of all features except V_i Weak relevance: A feature V_i is weakly relevant to T iff it is not strongly relevant, and $\exists S_i' \subset S_i$ and some v_i, t , and s_i' for which $p(V_i = v_i, \mathbf{S}_i' = s_i') > 0$, such that $p(T = t | X_i = v_i, S_i' = s_i') \neq p(T = t | S_i' = s_i')$. [Kohavi and John, 1997]

Selection based on combination of features

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Applications of Causal Discovery Methods Knowing the value of weakly relevant variable V_i do not give additional information regarding the target of interest, when we know the value of all other features; however if we only know the value of a subset of all other measured variables, knowing the value of V_i may provide additional information. [Kohavi and John, 1997]

Selection based on combination of features

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Applications of Causal Discovery Methods **Irrelevance**: A feature V_i is relevant if it is either weakly relevant or strongly relevant; otherwise, it is irrelevant.

Irrelevant features neither provide information regarding the target by itself nor in combination with any other features.

[Kohavi and John, 1997]

Selection based on combination of features

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Causal Structure From Observationa Data

Applications of Causal Discovery Methods Given the definition of strong, weak and irrelevant variables, what is our stratergy?

- Strongly relevant features should always be selected. Omitting Strongly relevant features will compromise predictive performance.
- Weakly relevant features do not improve predictive performance if all strongly relevant features are selected.
- Irrelevant features do not improve predictive performance.

[Kohavi and John, 1997]

Relationship between Causality and Feature Selection

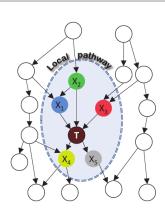
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Applications of Causal Discovery Methods



The Markov Boundary (direct causes + direct effects + direct causes of direct effects) is the minimal feature set that contain all information regarding the target of interest (i.e. strongly relevant) under faithfulness.

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Applications of Causal Discovery Methods

- selected features have causal interpretations
- selected feature set is generally smaller compared to non-causal methods
- model generalize better under certain type of distribution shift

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Discoverying Causal Structure From Observationa Data

Applications of Causal Discovery Methods Example: selected features have causal interpretations.



[Aliferis et al., 2010a]

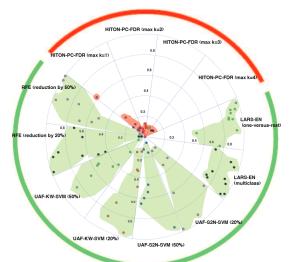
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Applications of Causal Discovery Methods Example: selected features have causal interpretations.



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Causal Structure From Observational

Applications of Causal Discovery Methods Example: selected feature set is generally smaller compared to non-causal methods, without compromising predictive performance.

Feature selection method	Predicitivity		Reduction	
	P-value	Nominal winner	P-value	Nominal winner
No feature selection	0.1890	Other	< 0.0001	HITON-PC
RFE: 4 variants	0.9754	Other	0.0046	HITON-PC
	0.8030	Other	0.0042	HITON-PC
	0.1312	HITON-PC	0.3634	HITON-PC
	0.1008	HITON-PC	0.6816	Other
UAF-KruskalWallis-SVM: 4 variants	0.2248	Other	0.0028	HITON-PC
	0.0098	Other	0.0004	HITON-PC
	1.0000	HITON-PC	0.1414	HITON-PC
	0.3232	HITON-PC	0.3998	HITON-PC
	0.0710	Other	0.0018	HITON-PC
UAF-Signal2Noise-SVM: 4	0.0752	Other	0.0030	HITON-PC
variants	0.4420	HITON-PC	0.7850	HITON-PC
	0.2820	HITON-PC	0.6604	HITON-PC
UAF-Neal-SVM: 4 variants	0.5046	Other	< 0.0001	HITON-PC
	0.9782	HITON-PC	< 0.0001	HITON-PC
	0.6980	HITON-PC	0.0044	HITON-PC
	0.3806	HITON-PC	0.0186	HITON-PC
Random Forest Variable	0.6064	HITON-PC	0.3252	HITON-PC
Selection: 2 variants	0.5050	HITON-PC	0.1338	Other
LARS-Elastic Net: 2 variants	1.0000	Other	0.1112	HITON-PC
	0.0832	HITON-PC	0.5216	Other
	0.0000	I	<0.0001	THEONE DO

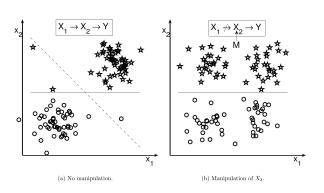
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Applications of Causal Discovery Methods Example: Model built with causal feature selection methods generalize better under certain distribution shifts.



[Guyon et al., 2007]

Markov Boundary

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Applications of Causal Discovery Methods There are a number of algorithms that discovery the local causal neibourhood of the data.

- PC-simple[Bühlmann et al., 2010]
- HITON-PC[Aliferis et al., 2003, Aliferis et al., 2010a, Aliferis et al., 2010b]
- HITON-MB[Aliferis et al., 2010a, Aliferis et al., 2010b]
- MMPC [Tsamardinos et al., 2006]
- IAMB[Tsamardinos et al., 2003]
- MBFS[Ramsey, 2006]

Take Home Message

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Applications of Causal Discovery Methods

- Causal structural discovery methods can identify causal relationships from observational and experimental data with and without domain knowledge.
- Computational causal discovery methods have wide applications in knowledge discovery and predictive modeling.
- github.com/SisiMa1729/CausalAnalytics_Intro
- github.com/SisiMa1729/Causal_Feature_Selection

References I

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