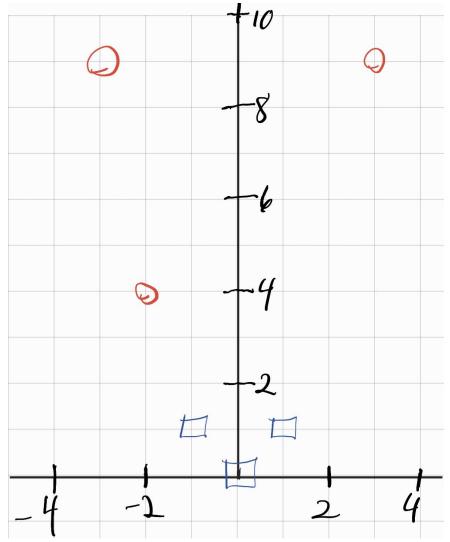
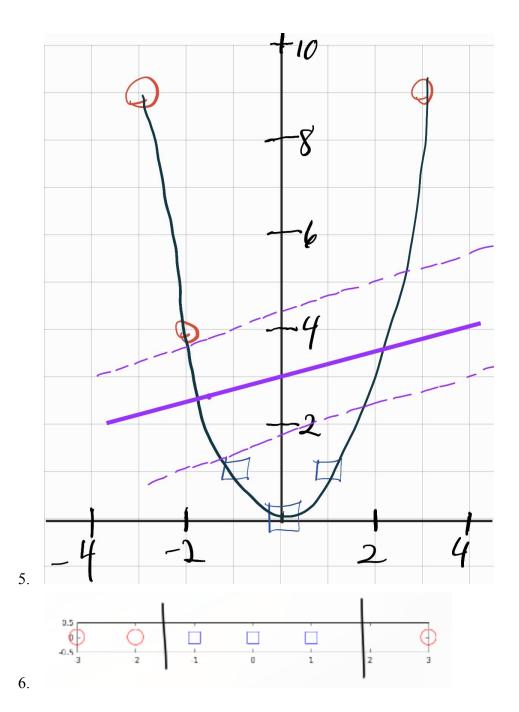
## 1.1 (Finite Features and SVMs)

1. In its current feature space, the dataset can not be perfectly separated by a linear separator. The data's class changes twice along the one dimension and a linear classifier in a single dimension can only separate a single class change.



2.

- 3. Yes, after being translated into 2 dimensional space, a linear separator can perfectly separate the points because there is now a clear path for a line to be drawn between the positive and negative samples.
- 4. In order to fully separate the data with a maximized margin, the line must pass through the midpoint between the two closest opposing points located at (-2,4) and (-1,1). The midpoint between the two points would be the point (-3/5, 5/2) and the hyperplane would be perpendicular to the line formed if one were to connect the points. Because of that, the line would have a slope of 1/3. Using the point and slope you can find that  $w_1$ =-1/3,  $w_2$ =1, and c=-3. The margin would be the The margin would be half of the distance between the two points which is  $\sqrt{10}/2$ .



## 1.2 (Infinite Features Spaces and Kernel Magic)

1. We cannot explicitly construct  $\phi_{\infty}(x)$  because it is infinite-dimensional. This would mean writing down an infinite number of basis functions which is not possible.

2. Yes, 
$$k(a, b) = \sum_{i=1}^{\infty} \frac{e^{-a^{2}/2}a^{i}}{\sqrt{i!}} \frac{e^{-b^{2}/2}b^{i}}{\sqrt{i!}}$$
  

$$= exp[-\frac{a^{2}+b^{2}}{2}] \sum_{i=1}^{\infty} [\frac{(ab)^{i}}{i!}]$$

$$= exp[-\frac{a^{2}+b^{2}}{2}] exp[ab]$$

$$= exp[-\frac{1}{2}(a^{2}-2ab+b^{2})]$$

$$= exp[-\frac{1}{2}(a-b)^{2}]$$

3. No, since model complexity in SVMs is not managed by feature space dimensions and instead by the number of support vectors.

4. 
$$k(x_i + x_0, x_j + x_0) = e^{\frac{-((x_i + x_0) - (x_j + x_0))^2}{2}} = e^{\frac{-(x_i - x_j)^2}{2}} = k(x_i, x_j)$$

## 2 (Naïve Bayes Classifier)

1.

$$P(Y=1|Z=missing) = rac{0.08* heta_{y=1}}{0.02*(1- heta_{y=1})+0.08* heta_{y=1}}$$

2.

3. Log-joint probability for a single example:

$$\log P(X_1 = x_1, X_2 = x_2, X_3 = x_3, Z = z, Y = y) = \log[p(y) \cdot p(x_1|y) \cdot p(x_2|y) \cdot p(x_3|y) \cdot P(Z = z|Y = y)]$$

For n i.i.d. examples:

$$\log P(X, Y, Z) = \sum_{i=1}^{n} \log[p(y_i) \cdot p(x_{i1}|y_i) \cdot p(x_{i2}|y_i) \cdot p(x_{i3}|y_i) \cdot P(Z_i = z_i|Y_i = y_i)]$$

## 4 (Principal Components Analysis)

- 1. Done.
- 2. ~30 eigenvectors.
- 3. Yes, much better.