

# ICPC Notebook

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## template

### hash.sh

```
# 使い方: sh hash.sh -> コピペ -> Ctrl + D
# コメント・空白・改行を削除して md5 でハッシュする
g++ -dD -E -P -fpreprocessed - | tr -d '[:space:]' | md5sum | cut -c-6
```

### settings.sh

```
# Clion の設定
Settings → Build → CMake → Reload CMake Project
add_compile_options(-D_GLIBCXX_DEBUG)
# Caps Lock を Ctrl に変更
setxkbmap -option ctrl:nocaps
```

### template.hpp

md5: 586639

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
const ll INF = LLONG_MAX / 4;
const ll LINF = LLONG_MAX / 4;
#define rep(i, a, b) for(ll i = a; i < (b); i++)
#define all(a) begin(a), end(a)
#define sz(a) ssize(a)
bool chmin(auto& a, auto b) { return a > b ? a = b, 1 : 0; }
bool chmax(auto& a, auto b) { return a < b ? a = b, 1 : 0; }

#define fi first
#define se second
#define eb emplace_back
#define pb push_back

void solve() {}

signed main() {
    cin.tie(0)->sync_with_stdio(0);
    int t = 1;
    cin >> t;
    while(t--) { solve(); }
}
```

## data-structure

### BIT.hpp

md5: 8133c8

```
struct BIT {
    vector<ll> a;
    BIT(ll n) : a(n + 1) {}
    void add(ll i, ll x) { // A[i] += x
        i++;
        while(i < sz(a)) {
            a[i] += x;
            i += i & -i;
        }
    }
}
```

```
ll sum(ll r) {
    ll s = 0;
    while(r) {
        s += a[r];
        r -= r & -r;
    }
    return s;
}
ll sum(ll l, ll r) { // sum of A[l, r)
    return sum(r) - sum(l);
}
};
```

FastSet.hpp

md5: 2cb8c9

```
// using u64 = uint64_t;
const u64 B = 64;
struct FastSet {
    u64 n;
    vector<vector<u64>> a;
    FastSet(u64 n_) : n(n_) {
        do a.emplace_back(n_ = (n_ + B - 1) / B);
        while(n_ > 1);
    }
    // bool operator[](ll i) const { return a[0][i / B] >> (i % B) & 1; }
    void set(ll i) {
        for(auto& v : a) {
            v[i / B] |= 1ULL << (i % B);
            i /= B;
        }
    }
    void reset(ll i) {
        for(auto& v : a) {
            v[i / B] &= ~(1ULL << (i % B));
            if(v[i / B]) break;
            i /= B;
        }
    }
    ll next(ll i) { // i を超える最小の要素
        rep(h, 0, sz(a)) {
            i++;
            if(i / B >= sz(a[h])) break;
            u64 d = a[h][i / B] >> (i % B);
            if(d) {
                i += countr_zero(d);
                while(h--) i = i * B + countr_zero(a[h][i]);
                return i;
            }
            i /= B;
        }
        return n;
    }
    ll prev(ll i) { // i より小さい最大の要素
        rep(h, 0, sz(a)) {
            i--;
            if(i < 0) break;
            u64 d = a[h][i / B] << (~i % B);
            if(d) {
                i -= countl_zero(d);
                while(h--) i = i * B + __lg(a[h][i]);
                return i;
            }
        }
    }
};
```

```
    }
    i /= B;
}
return -1;
};
```

Rangetree.hpp

md5: 31d0a1

```
// rangeset(merge-sort tree) 静态结构, 高效查询但不支持更新
// 一组点集上, 查询矩形区域
// RangeSet rs(x); x为vector<pair<>>;
// rs.count(x1,x2,y1,y2), [x1,x2) * [y1,y2)
using ll = int64_t;
using pll = pair<ll, ll>;
const LINF = 0x1fffffffffffffff;

struct RangeSet {
    vector<vector<ll>> data;
    vector<ll> x;
    ll siz_x = 1;
    RangeSet(vector<pll> a) {
        sort(a.begin(), a.end());
        if(a.size()) x.push_back(a[0].first);
        for(auto& i : a) {
            if(x.back() != i.first) x.push_back(i.first);
            while(x.size() > siz_x) siz_x *= 2;
            while(x.size() < siz_x) x.push_back(LINF);
            data.resize(siz_x * 2);
            ll at = 0;
            for(auto& i : a) {
                if(x[at] != i.first) at++;
                data[siz_x + at].push_back(i.second);
            }
            for(ll i = siz_x; --i;) {
                data[i].resize(data[i * 2].size() + data[i * 2 + 1].size());
                merge(data[i * 2].begin(), data[i * 2].end(), data[i * 2 + 1].begin(), data[i * 2 + 1].end(), data[i].begin());
            }
        }
        ll count(ll x1, ll x2, ll y1, ll y2) const { // [x1, x2) * [y1, y2)
            ll l = lower_bound(x.begin(), x.end(), x1) - x.begin(), r = lower_bound(x.begin(), x.end(), x2) - x.begin();
            l += siz_x;
            r += siz_x;
            ll ans = 0;
            for(; l < r; l /= 2, r /= 2) {
                if(l & 1) {
                    ans += lower_bound(data[l].begin(), data[l].end(), y2) - lower_bound(data[l].begin(), data[l].end(), y1);
                    l++;
                }
                if(r & 1) {
                    r--;
                    ans += lower_bound(data[r].begin(), data[r].end(), y2) - lower_bound(data[r].begin(), data[r].end(), y1);
                }
            }
            return ans;
        }
    };
};
```

ST.hpp

md5: 007a88

```
namespace ds {
template<typename T> struct ST {
    vector<vector<T>> table;
    vector<int> Lg;
    int n;
    static T default_func(const T& t1, const T& t2) { return max(t1, t2); }
    function<T(const T&, const T&> op = default_func;
    ST() {
        table.clear();
        Lg = vector<int>{0, 0};
        n = 0;
    }
    ST(vector<T> v, function<T(const T&, const T&> func = default_func) {
        Lg = vector<int>{0, 0};
        init(v, func);
    }
    void init(vector<T> v, function<T(const T&, const T&> func) {
        op = func;
        table.clear();
        n = v.size();
        if((int)Lg.size() <= n) {
            int tmp = Lg.size();
            Lg.resize(n + 1);
            for(int i = tmp; i <= n; i++) Lg[i] = Lg[i >> 1] + 1;
        }
        int l = Lg[n];
        table.push_back(v);
        for(int i = 1, tmp; i <= l; i++) {
            table.push_back(vector<int>(tmp = n - (1 << i) + 1));
            for(int j = 0; j < tmp; j++) table[i][j] = op(table[i - 1][j], table[i - 1][j +
(1 << (i - 1))]));
        }
    }
    T query(int l, int r) {
        int u = Lg[r - l + 1];
        return op(table[u][l], table[u][r - (1 << u) + 1]);
    }
};
} // namespace ds
using ds::ST;
```

SWAG.hpp

md5: 980cd3

```
// 滑动窗口！
// 用法：需要自定义 using T = ;
//     inline T f(T a, T b) {}; 聚合函数
//     const T def_value = -INF; 默认空窗口的数据
//     函数实例：a+b,min(a,b),max(a,b),gcd(a,b)
struct SWAG {
    using T = <#ll #>;
    inline T f(T a, T b) const { return <#gcd(a, b) #>; }
    const T def_value = <# - LINF #>;
    ll size = 0;
    vector<T> fold_l, r;
    T fold_r;
    T get() const {
```

```
if(r.empty()) {
    if(fold_l.empty()) return def_value;
    return fold_l.back();
}
if(fold_l.empty()) return fold_r;
return f(fold_l.back(), fold_r);
}
void push(T a) {
    if(r.empty()) fold_r = a;
    else fold_r = f(fold_r, a);
    r.push_back(a);
    size++;
}
void pop() {
    if(fold_l.empty()) {
        for(ll i = size; i--;) fold_l.push_back(r[i]);
        r.clear();
        for(ll i = 1; i < size; i++) fold_l[i] = f(fold_l[i], fold_l[i - 1]);
    }
    fold_l.pop_back();
    size--;
}
};
```

Segtree-easy.hpp

md5: dc45c7

```
// easy version

struct SegmentTree {
    ll size = 1;
    vector<ll> data;
    SegmentTree(ll n) {
        while(size < n) size *= 2;
        data.assign(size * 2, -LINF);
    }
    void update(ll at) {
        while(at /= 2) data[at] = max(data[at * 2], data[at * 2 + 1]);
    }
    void set(ll at, ll val) {
        at += size;
        data[at] = val;
        update(at);
    }
    ll get(ll l, ll r) {
        ll ans = -LINF;
        l += size;
        r += size;
        for(; l < r; l /= 2, r /= 2) {
            if(l & 1) chmax(ans, data[l++]);
            if(r & 1) chmax(ans, data[--r]);
        }
        return ans;
    }
};
```

math

BinaryGCD.hpp

md5: f3ab31

```
u64 ctz(u64 x) { return countr_zero(x); }
u64 binary_gcd(u64 x, u64 y) {
    if(!x || !y) return x | y;
    u64 n = ctz(x), m = ctz(y);
    x >>= n, y >>= m;
    while(x != y) {
        if(x > y) x = (x - y) >> ctz(x - y);
        else y = (y - x) >> ctz(y - x);
    }
    return x << min(n, m);
}
```

ExtGCD.hpp

md5: c3fa9b

```
// returns gcd(a, b) and assign x, y to integers
// s.t. ax + by = gcd(a, b) and |x| + |y| is minimized
ll extgcd(ll a, ll b, ll& x, ll& y) {
    // assert(a >= 0 && b >= 0);
    if(!b) return x = 1, y = 0, a;
    ll d = extgcd(b, a % b, y, x);
    y -= a / b * x;
    return d;
}
```

Permutation.hpp

md5: 9c154e

```
// 置换类： 组合，逆置换，幂运算，0-based
// 直接初始化: Permutation p = {}, q(vector<>{});
// p.inv() 求逆置换
// p * q 置换组合，p *= q 就地组合；
// p.pow(k) 置换的幂
// Permutation::identity 生成恒等置换；
using ll = long long;

struct Permutation { // 0-indexed
    vector<ll> perm;
    Permutation(initializer_list<ll>& perm) : perm(perm) {}
    Permutation(vector<ll>& perm) : perm(perm) {}
    template<class T> Permutation(const initializer_list<T>& perm) : perm(perm.begin(), perm.end()) {}
    template<class T> Permutation(const vector<T>& perm) : perm(perm.begin(), perm.end()) {}
}

static Permutation identity(ll n) {
    vector<ll> ans(n);
    iota(ans.begin(), ans.end(), 0);
    return ans;
}

Permutation inv() const {
    vector<ll> ans(perm.size());
    for(ll i = 0; i < perm.size(); i++) ans[perm[i]] = i;
    return ans;
}

Permutation operator*(const Permutation& x) const {
    vector<ll> ans(perm.size());
```

```
    for(ll i = 0; i < perm.size(); i++) ans[i] = perm[x.perm[i]];
    return ans;
}

Permutation& operator*=(const Permutation& x) {
    vector<ll> ans(perm.size());
    for(ll i = 0; i < perm.size(); i++) ans[i] = perm[x.perm[i]];
    perm.swap(ans);
    return *this;
}

Permutation pow(ll x) const {
    Permutation ans = identity(perm.size()), cnt = *this;
    while(x) {
        if(x & 1) ans *= cnt;
        x /= 2;
        cnt *= cnt;
    }
    return ans;
}

};
```

modint

BarrettReduction.hpp

md5: 2ca7f3

```
// using u64 = uint64_t;
struct Barrett { // mod < 2^32
    u64 m, im;
    Barrett(u64 mod) : m(mod), im(-1ULL / m + 1) {}
    // input: a * b < 2^64, output: a * b % mod
    u64 mul(u64 a, u64 b) const {
        a *= b;
        u64 x = ((__uint128_t)a * im) >> 64;
        a -= x * m;
        if((ll)a < 0) a += m;
        return a;
    }
};
```

modint.hpp

md5: 81b530

```
const ll mod = 998244353;
struct mm {
    ll x;
    mm(ll x_ = 0) : x(x_ % mod) {
        if(x < 0) x += mod;
    }
    friend mm operator+(mm a, mm b) { return a.x + b.x; }
    friend mm operator-(mm a, mm b) { return a.x - b.x; }
    friend mm operator*(mm a, mm b) { return a.x * b.x; }
    friend mm operator/(mm a, mm b) { return a * b.inv(); }

    // 下面四行 虚数
    friend mm& operator+=(mm& a, mm b) { return a = a.x + b.x; }
    friend mm& operator-=(mm& a, mm b) { return a = a.x - b.x; }
    friend mm& operator*=(mm& a, mm b) { return a = a.x * b.x; }
    friend mm& operator/=(mm& a, mm b) { return a = a * b.inv(); }
    mm inv() const { return pow(mod - 2); }
    mm pow(ll b) const {
        mm a = *this, c = 1;
        while(b) {
            if(b & 1) c *= a;
```

```
        a *= a;
        b >>= 1;
    }
    return c;
}
};
```

FPS

FFT.hpp

md5: 3138c7

```
// {998244353, 3}, {1811939329, 13}, {2013265921, 31}
mm g = 3; // 原始根
void fft(vector<mm>& a) {
    ll n = sz(a), lg = __lg(n);
    assert((1 << lg) == n);
    vector<mm> b(n);
    rep(l, 1, lg + 1) {
        ll w = n >> l;
        mm s = 1, r = g.pow(mod >> l);
        for(ll u = 0; u < n / 2; u += w) {
            rep(d, 0, w) {
                mm x = a[u << 1 | d], y = a[u << 1 | w | d] * s;
                b[u | d] = x + y;
                b[n >> 1 | u | d] = x - y;
            }
            s *= r;
        }
        swap(a, b);
    }
}
vector<mm> conv(vector<mm> a, vector<mm> b) {
    if(a.empty() || b.empty()) return {};
    size_t s = sz(a) + sz(b) - 1, n = bit_ceil(s);
    // if(min(sz(a), sz(b)) <= 60) 愚直に掛け算
    a.resize(n);
    b.resize(n);
    fft(a);
    fft(b);
    mm inv = mm(n).inv();
    rep(i, 0, n) a[i] *= b[i] * inv;
    reverse(1 + all(a));
    fft(a);
    a.resize(s);
    return a;
}
```

FFT\_fast.hpp

md5: c8c567

```
// modint を u32 にして加減算を真面目にやると速い
mm g = 3; // 原始根
void fft(vector<mm>& a) {
    ll n = sz(a), lg = __lg(n);
    static auto z = [] {
        vector<mm> z(30);
        mm s = 1;
        rep(i, 2, 32) {
            z[i - 2] = s * g.pow(mod >> i);
            s *= g.inv().pow(mod >> i);
        }
    };
```

```
    }
    return z;
}();
rep(l, 0, lg) {
    ll w = 1 << (lg - l - 1);
    mm s = 1;
    rep(k, 0, 1 << l) {
        ll o = k << (lg - l);
        rep(i, o, o + w) {
            mm x = a[i], y = a[i + w] * s;
            a[i] = x + y;
            a[i + w] = x - y;
        }
        s *= z[countr_zero<uint64_t>(~k)];
    }
}
}
// コピペ
void ifft(vector<mm>& a) {
    ll n = sz(a), lg = __lg(n);
    static auto z = [] {
        vector<mm> z(30);
        mm s = 1;
        rep(i, 2, 32) { // g を逆数に
            z[i - 2] = s * g.inv().pow(mod >> i);
            s *= g.pow(mod >> i);
        }
        return z;
    }();
    for(ll l = lg; l--;) { // 逆順に
        ll w = 1 << (lg - l - 1);
        mm s = 1;
        rep(k, 0, 1 << l) {
            ll o = k << (lg - l);
            rep(i, o, o + w) {
                mm x = a[i], y = a[i + w]; // *s を下に移動
                a[i] = x + y;
                a[i + w] = (x - y) * s;
            }
            s *= z[countr_zero<uint64_t>(~k)];
        }
    }
}
vector<mm> conv(vector<mm> a, vector<mm> b) {
    if(a.empty() || b.empty()) return {};
    size_t s = sz(a) + sz(b) - 1, n = bit_ceil(s);
    // if(min(sz(a), sz(b)) <= 60) 愚直に掛け算
    a.resize(n);
    b.resize(n);
    fft(a);
    fft(b);
    mm inv = mm(n).inv();
    rep(i, 0, n) a[i] *= b[i] * inv;
    ifft(a);
    a.resize(s);
    return a;
}
```

# graph

## UnionFindMonoid.hpp

md5: 1120a6

```
// 带权并查集
template<class S, auto op, auto e> class UnionFindMonoid {
    static_assert(std::is_convertible_v<decltype(op), std::function<S(S, S)>>, "op must work as S(S, S)");
    static_assert(std::is_convertible_v<decltype(e), std::function<S()>>, "e must work as S()");
    int _n;
    std::vector<int> parent_or_size;
    std::vector<S> data;

public:
    UnionFindMonoid(int n = 0) : _n(n), parent_or_size(n, -1), data(n, e()) {}
    UnionFindMonoid(const std::vector<S>& a) : _n((int)a.size()), parent_or_size(a.size(), -1), data(a) {}

    int leader(int a) {
        assert(0 <= a && a < _n);
        while(true) {
            const int b = parent_or_size[a];
            if(b < 0) return a;
            const int c = parent_or_size[b];
            if(c < 0) return b;
            a = parent_or_size[a] = c; // path halving
        }
    }
    bool is_leader(int a) const {
        assert(0 <= a && a < _n);
        return parent_or_size[a] < 0;
    }
    int merge(int a, int b) {
        assert(0 <= a && a < _n);
        assert(0 <= b && b < _n);
        a = leader(a);
        b = leader(b);
        if(a == b) return a;
        if(-parent_or_size[a] < -parent_or_size[b]) swap(a, b);
        parent_or_size[a] += parent_or_size[b];
        parent_or_size[b] = a;
        data[a] = op(data[a], data[b]);
        return a;
    }
    bool same(int a, int b) {
        assert(0 <= a && a < _n);
        assert(0 <= b && b < _n);
        return leader(a) == leader(b);
    }
    int size(int a) {
        assert(0 <= a && a < _n);
        return -parent_or_size[leader(a)];
    }
    S get(int a) {
        assert(0 <= a && a < _n);
        return data[leader(a)];
    }
    void set(int a, S x) {
        assert(0 <= a && a < _n);
```

```
        data[leader(a)] = x;
    }
};
```

## fast\_graph.hpp

md5: 7c9c15

```
// CSR压缩邻接表, 静态模型
//
class fast_graph {
    using I = vector<int>::iterator;
    struct edges {
        I l, r;
        bool empty() const { return l == r; }
        size_t size() const { return r - l; }
        auto begin() const { return l; }
        auto end() const { return r; }
        int operator[](size_t i) const { return l[i]; }
    };

    vector<int> mem;
    vector<edges> g;

public:
    fast_graph() {}
    fast_graph(int n, vector<pair<int, int>> edge) : g(n), mem(edge.size() * 2) {
        for(auto [a, b] : edge) {
            g[a].r++;
            g[b].r++;
        }
        I sum = mem.begin();
        for(int i = 0; i < n; i++) { tie(g[i].l, g[i].r, sum) = tuple{sum, sum, sum + (g[i].r - g[i].l)}; }
        for(auto [a, b] : edge) {
            *g[a].r++ = b;
            *g[b].r++ = a;
        }
    }
    bool empty() const { return g.empty(); }
    size_t size() const { return g.size(); }
    auto begin() const { return g.begin(); }
    auto end() const { return g.end(); }
    const auto& operator[](size_t i) const { return g[i]; }
};
```

## graphALL.hpp

md5: d03b78

```
// 勿忘, 图基础算法模板大全!!!!
struct WeightedEdge {
    ll to, cost;
    WeightedEdge() {}
    WeightedEdge(ll to, ll cost) : to(to), cost(cost) {}
    operator ll() const { return to; }
};
struct WeightedGraph {
    using E = WeightedEdge;
    vector<vector<E>> g;
    WeightedGraph() {}
    WeightedGraph(ll n) : g(n) {}
    vector<E>& operator[](ll at) { return g[at]; }
    operator vector<vector<E>>&() { return g; }
    auto begin() const { return g.cbegin(); }
```

```
auto end() const { return g.cend(); }
ll size() const { return g.size(); }
const vector<E>& operator[](ll at) const { return g[at]; }
operator const vector<vector<E>>&() const { return g; }
void resize(ll a) { g.resize(a); }
void add_edge(ll a, ll b, ll cost) {
    g[a].emplace_back(b, cost);
    g[b].emplace_back(a, cost);
}
void add_directed_edge(ll from, ll to, ll cost) { g[from].emplace_back(to, cost); }
template<ll start_index = 1, bool directed = false> void input_graph(ll m) {
    while(m--) {
        ll a, b, c;
        scanf("%lld%lld%lld", &a, &b, &c);
        a -= start_index;
        b -= start_index;
        g[a].emplace_back(b, c);
        if(!directed) g[b].emplace_back(a, c);
    }
}
template<ll start_index = 1> void input_tree(ll n) { input_graph<start_index>(n - 1); }
};

struct UnWeightedEdge {
    ll to;
    static constexpr ll cost = 1;
    UnWeightedEdge() {}
    UnWeightedEdge(ll to) : to(to) {}
    operator ll() const { return to; }
};

struct UnWeightedGraph {
    using E = UnWeightedEdge;
    vector<vector<E>> g;
    UnWeightedGraph() {}
    UnWeightedGraph(ll n) : g(n) {}
    vector<E>& operator[](ll at) { return g[at]; }
    operator vector<vector<E>>&() { return g; }
    auto begin() const { return g.cbegin(); }
    auto end() const { return g.cend(); }
    ll size() const { return g.size(); }
    const vector<E>& operator[](ll at) const { return g[at]; }
    operator const vector<vector<E>>&() const { return g; }
    void resize(ll a) { g.resize(a); }
    void add_edge(ll a, ll b) {
        g[a].emplace_back(b);
        g[b].emplace_back(a);
    }
    void add_directed_edge(ll from, ll to) { g[from].emplace_back(to); }
    template<ll start_index = 1, bool directed = false> void input_graph(ll m) {
        while(m--) {
            ll a, b;
            scanf("%lld%lld", &a, &b);
            a -= start_index;
            b -= start_index;
            g[a].emplace_back(b);
            if(!directed) g[b].emplace_back(a);
        }
    }
    template<ll start_index = 1> void input_tree(ll n) { input_graph<start_index>(n - 1); }
};
```

```
template<class Graph> vector<ll> Dijkstra(const Graph& g, ll start) {
    vector<ll> cost(g.size(), LINF);
    vector<bool> used(g.size());
    pq<pll> q;
    cost[start] = 0;
    q.emplace(0, start);
    while(q.size()) {
        ll at = q.top().second;
        q.pop();
        if(used[at]) continue;
        used[at] = 1;
        each(i, g[at]) if(chmin(cost[i], cost[at] + i.cost)) q.emplace(cost[i], i);
    }
    return cost;
}

vector<ll> BFS(const UnWeightedGraph& g, ll start) {
    vector<ll> cost(g.size(), LINF);
    queue<ll> q;
    cost[start] = 0;
    q.push(start);
    while(q.size()) {
        ll at = q.front();
        q.pop();
        each(i, g[at]) if(chmin(cost[i], cost[at] + i.cost)) q.push(i);
    }
    return cost;
}

template<class Graph> vector<vector<ll>> MarshallFloyd(const Graph& g) {
    ll n = g.size();
    vector<vector<ll>> cost(n, vector<ll>(n, LINF));
    queue<ll> q;
    for(ll i = 0; i < n; i++) cost[i][i] = 0;
    for(ll i = 0; i < n; i++)
        for(auto& j : g[i]) cost[i][j] = j.cost;
    for(ll k = 0; k < n; k++)
        for(ll i = 0; i < n; i++)
            for(ll j = 0; j < n; j++) chmin(cost[i][j], cost[i][k] + cost[k][j]);
    return cost;
}
```

graph/tree
flow

燃やす埋める.md

原始约束条件	网络流形式的约束 (变形后)
当 $x = 0$ 时, $z$ 不可获得 (或失去 $z$ )	在网络中添加边 $(x, T, z)$ , 表示若 $x$ 取 $0$ , 则 $z$ 与汇点 $T$ 相连 (流量受限)
当 $x = 0$ 时, $z$ 可获得	视为无条件获得 $z$ ; 在网络中添加边 $(S, x, z)$ , 即从源点 $S$ 到 $x$ 再到 $z$
当 $x = 1$ 时, $z$ 不可获得 (或失去 $z$ )	在网络中添加边 $(S, x, z)$ , 表示若 $x$ 取 $1$ , 则 $S$ 经 $x$ 控制 $z$ 的流动

原始约束条件	网络流形式的约束（变形后）
当 $x = 1$ 时, $z$ 可获得	视为无条件获得 $z$ ; 在网络中添加边 $(x, T, z)$ , 即 $x$ 通向汇点 $T$ 并激活 $z$
当 $x, y, \dots$ 全为 $0$ 时, $z$ 可获得	视为无条件获得 $z$ ; 引入辅助节点 $w$ , 并添加边: $(S, w, z)$ 、 $(w, x, \infty)$ 、 $(w, y, \infty)$ , 表示 $w$ 由多个变量控制, 均为 $0$ 时可达
当 $x, y, \dots$ 全为 $1$ 时, $z$ 可获得	视为无条件获得 $z$ ; 引入辅助节点 $w$ , 并添加边: $(w, T, z)$ 、 $(x, w, \infty)$ 、 $(y, w, \infty)$ , 表示 $w$ 仅在所有变量取 $1$ 时与汇点 $T$ 连通

string

KMP.hpp

md5: 886c63

```
// kmp[i] := max{ l ≤ i | s[:l] == s[(i+1)-l:i+1] }
// abacaba -> 0010123
auto KMP(string s) {
    vector<ll> p(sz(s));
    rep(i, 1, sz(s)) {
        ll g = p[i - 1];
        while(g && s[i] != s[g]) g = p[g - 1];
        p[i] = g + (s[i] == s[g]);
    }
    return p;
}
```

Manacher.hpp

md5: 5882fb

```
// 各位置での回文半径を求める
// aaabaaa -> 1214121
// 偶数長の回文を含めて直径を知るには, N+1 個の $ を挿入して 1 を引く
// $a$a$a$b$a$a$a$a$ -> 123432181234321
auto manacher(string s) {
    ll n = sz(s), i = 0, j = 0;
    vector<ll> r(n);
    while(i < n) {
        while(i >= j && i + j < n && s[i - j] == s[i + j]) j++;
        r[i] = j;
        ll k = 1;
        while(i >= k && i + k < n && k + r[i - k] < j) {
            r[i + k] = r[i - k];
            k++;
        }
        i += k, j -= k;
    }
    return r;
}
```

RollingHash.hpp

md5: adb8d3

```
// using u64 = uint64_t;
const u64 mod = INF;
u64 add(u64 a, u64 b) {
    a += b;
    if(a >= mod) a -= mod;
    return a;
}
u64 mul(u64 a, u64 b) {
```

```
    auto c = (__uint128_t)a * b;
    return add(c >> 61, c & mod);
}
random_device rnd;
const u64 r = ((u64)rnd() << 32 | rnd()) % mod;
struct RH {
    ll n;
    vector<u64> hs, pw;
    RH(string s) : n(sz(s)), hs(n + 1), pw(n + 1, 1) {
        rep(i, 0, n) {
            pw[i + 1] = mul(pw[i], r);
            hs[i + 1] = add(mul(hs[i], r), s[i]);
        }
    }
    u64 get(ll l, ll r) const { return add(hs[r], mod - mul(hs[l], pw[r - l])); }
};
```

SuffixArray.hpp

md5: 1d70ce

```
// returns pair{sa, lcp}
// sa 長さ n : s[sa[0]:] < s[sa[1]:] < ... < s[sa[n-1]:]
// lcp 長さ n-1 : lcp[i] = LCP(s[sa[i]:], s[sa[i+1]:])
auto SA(string s) {
    ll n = sz(s) + 1, lim = 256;
    // assert(lim > ranges::max(s));
    vector<ll> sa(n), lcp(n), x(all(s) + 1), y(n), ws(max(n, lim)), rk(n);
    iota(all(sa), 0);
    for(ll j = 0, p = 0; p < n; j = max(1LL, j * 2), lim = p) {
        p = j;
        iota(all(y), n - j);
        rep(i, 0, n) if(sa[i] >= j) y[p++] = sa[i] - j;
        fill(all(ws), 0);
        rep(i, 0, n) ws[x[i]]++;
        rep(i, 1, lim) ws[i] += ws[i - 1];
        for(ll i = n; i--;) sa[--ws[x[y[i]]]] = y[i];
        swap(x, y);
        p = 1;
        x[sa[0]] = 0;
        rep(i, 1, n) {
            ll a = sa[i - 1], b = sa[i];
            x[b] = (y[a] == y[b] && y[a + j] == y[b + j]) ? p - 1 : p++;
        }
        rep(i, 1, n) rk[sa[i]] = i;
        for(ll i = 0, k = 0; i < n - 1; lcp[rk[i++]] = k) {
            if(k) k--;
            while(s[i + k] == s[sa[rk[i] - 1] + k]) k++;
        }
        sa.erase(begin(sa));
        lcp.erase(begin(lcp));
        return pair{sa, lcp};
    }
}
```

Zalgorithm.hpp

md5: b20b04

```
// Z[i] := LCP(s, s[i:])
// abacaba -> 7010301
auto Z(string s) {
    ll n = sz(s), l = -1, r = -1;
    vector<ll> z(n, n);
    rep(i, 1, n) {
```



```
    ll& x = z[i] = i < r ? min(r - i, z[i - l]) : 0;
    while(i + x < n && s[i + x] == s[x]) x++;
    if(i + x > r) l = i, r = i + x;
}
return z;
```

algorithm

geometry

DynamicConvexPolygon.hpp

md5: b07234

```
struct Polygon {
    map<ll, ll> lower{{0, 0}}, upper{{0, 0}};
    ll size() const {
        return lower.size() + upper.size() - (*lower.begin() == *upper.begin()) -
            (*lower.rbegin() == *upper.rbegin());
    }
    void add(ll x, ll y) {
        {
            auto can_erase = [&](map<ll, ll>::iterator p) -> bool {
                if(p == lower.begin()) return 0;
                if(next(p) == lower.end()) return 0;
                return cross(*next(p) - *p, *prev(p) - *p) <= 0;
            };
            auto [p, f] = lower.try_emplace(x, y);
            chmin(p->second, y);
            if(can_erase(p)) {
                lower.erase(p);
                return;
            }
            while(p != lower.begin() && can_erase(prev(p))) lower.erase(prev(p));
            while(next(p) != lower.end() && can_erase(next(p))) lower.erase(next(p));
        }
        {
            auto can_erase = [&](map<ll, ll>::iterator p) -> bool {
                if(p == upper.begin()) return 0;
                if(next(p) == upper.end()) return 0;
                return cross(*prev(p) - *p, *next(p) - *p) <= 0;
            };
            auto [p, f] = upper.try_emplace(x, y);
            chmax(p->second, y);
            if(can_erase(p)) {
                upper.erase(p);
                return;
            }
            while(p != upper.begin() && can_erase(prev(p))) upper.erase(prev(p));
            while(next(p) != upper.end() && can_erase(next(p))) upper.erase(next(p));
        }
    };
};
```

Geometry2D.hpp

md5: 295c9e

```
template<class T> using P = pair<T, T>;
#define x first
#define y second
```

```
template<class T> P<T> operator+(const P<T>& a, const P<T>& b) { return {a.x + b.x, a.y + b.y}; }
template<class T> P<T> operator-(const P<T>& a, const P<T>& b) { return {a.x - b.x, a.y - b.y}; }
template<class T> P<T> operator-(const P<T>& a) { return {-a.x, -a.y}; }
template<class T, class U> P<T> operator*(const P<T>& a, const U& b) { return {a.x * b, a.y * b}; }
template<class T, class U> P<T> operator/(const P<T>& a, const U& b) { return {a.x / b, a.y / b}; }
template<class T> P<T>& operator+=(P<T>& a, const P<T>& b) { return a = a + b; }
template<class T> P<T>& operator-=(P<T>& a, const P<T>& b) { return a = a - b; }
template<class T, class U> P<T>& operator*=(P<T>& a, const U& b) { return a = a * b; }
template<class T, class U> P<T>& operator/=(P<T>& a, const U& b) { return a = a / b; }
template<class T> P<T> rotate(const P<T>& a) { return {-a.y, a.x}; } // 90 degree ccw
template<class T> T dot(const P<T>& a, const P<T>& b) { return a.x * b.x + a.y * b.y; }
template<class T> T cross(const P<T>& a, const P<T>& b) { return dot(rotate(a), b); }
template<class T> T square(const P<T>& a) { return dot(a, a); }
template<class T> ld abs(const P<T>& a) { return hypotl(a.x, a.y); }
template<class T> T gcd(const P<T>& a) { return gcd(a.x, a.y); }
template<class T> P<T> normalize(P<T> a) {
    if(a == P<T>{}) return a;
    a /= gcd(a);
    if(a < P<T>{}) a = -a;
    return a;
}
```

memo

Primes.md

素数个数

n	10^2	10^3	10^4	10^5	10^6	10^7	10^8	10^9	10^10
$\pi(n)$	25	168	1229	9592	78498	664579	5760000	50800000	455000000

高度合成数

$\leq n$	10^3	10^4	10^5	10^6	10^7	10^8	10^9
x	840	7560	83160	720720	8648640	73513440	735134400
$d^{\wedge}0(x)$	32	64	128	240	448	768	1344

$\leq n$	10^10	10^11	10^12	10^13	10^14	10^15	10^16	10^17	10^18
$d^{\wedge}0(x)$	2304	4032	6720	10752	17280	26880	41472	64512	103680

素数阶乘

n	2	3	5	7	11	13	17	19	23	29
n#	2	6	30	210	2310	30030	510510	9702000	223000000	6470000000

阶乘

4!	5!	6!	7!	8!	9!	10!	11!	12!	13!
24	120	720	5040	40320	362880	3628800	39916800	479001600	6227020800