

| Type      | Equation  | Solved for Y   | D                           | R                           | Keywords                          |  |
|-----------|---|--|-----------------------------|-----------------------------|-----------------------------------|--|
| Ellipse   | $\frac{x^2}{121} + \frac{y^2}{441} = 1$                   | $y = \pm \sqrt{441(1 - \frac{x^2}{121})}$                    | all reals                   | $-13.617 \leq y \leq -4.56$ | Head: Main Face                   |  |
| Parabola  | $y = -\frac{9}{144}x^2 - 18$                              | $y = -\frac{9}{144}x^2 - 18$                                 | $X \leq -3.086$             | $y \leq -13.559$            | Head: Chin                        |  |
| Parabola  | $y = \frac{9}{144}x^2 - 18$                               | $y = \frac{9}{144}x^2 - 18$                                  | $X \geq 3.086$              | $y \leq -13.559$            | Head: Chin                        |  |
| Parabola  | $y = -\frac{1}{121}x^2 + 8$                               | $y = -\frac{1}{121}x^2 + 8$                                  | $-11 \leq x \leq 11$        | All reals                   | Head: Hairline                    |  |
| Parabola  | $y = \frac{-31}{729}x^2 - 17$                             | $y = \frac{-31}{729}x^2 - 17$                                | $-3.09 \leq x \leq 3.09$    | All reals                   | Head: Chin 2                      |  |
| Ellipse   | $\frac{x^2}{121} + \frac{(y-7)^2}{55} = 1$                | $y = 7 \pm \sqrt{25 - \frac{55x^2}{121}}$                    | all reals                   | $Y \geq 7$                  | Head: Top of Hair                 |  |
| Line      | $x = 11$  | undefined  | all reals                   | $1 \leq y \leq 7$           | Head: Side 1 of Face              |  |
| Line      | $x = -11$   | undefined  | all reals                   | $1 \leq y \leq 7$           | Head: Side 2 of Face              |  |
| Hyperbola | $\frac{x^2}{100} - \frac{(y+2)^2}{300/7} = 1$             | $y = \pm \sqrt{\frac{-300}{7}(1 - \frac{x^2}{100})} - 2$     | all reals                   | $1 \geq y \geq -5$          | Ear: Head intersect               |  |
| Ellipse   | $\frac{(x-11)^2}{4} + \frac{(y+2)^2}{9} = 1$              | $y = \pm \sqrt{9 - \frac{9(x-11)^2}{4}} - 2$                 | $x \geq 11$                 | $Y \geq -2$                 | Ear: Right Ellipse                |  |
| Ellipse   | $\frac{(x-11)^2}{4} + \frac{(y+2)^2}{9} = 1$              | $y = \pm \sqrt{9 - \frac{9(x-11)^2}{4}} - 2$                 | $x \geq 11$                 | $Y \leq -4.645$             | Ear: Right Ellipse                |  |
| Parabola  | $y = \frac{7}{25}(x-8)^2 - 9$                             | $y = \frac{7}{25}(x-8)^2 - 9$                                | $X \geq 11$                 | $-2 \geq y \geq -4.645$     | Ear: Right Parabola               |  |
| Ellipse   | $\frac{(x+11)^2}{4} + \frac{(y+2)^2}{9} = 1$              | $y = \pm \sqrt{9 - \frac{9(x+11)^2}{4}} - 2$                 | $X \leq -11$                | $Y \geq -2$                 | Ear: Left Ellipse                 |  |
| Ellipse   | $\frac{(x+11)^2}{4} + \frac{(y+2)^2}{9} = 1$              | $y = \pm \sqrt{9 - \frac{9(x+11)^2}{4}} - 2$                 | $X \leq -11$                | $Y \leq -4.645$             | Ear: Left Ellipse                 |  |
| Parabola  | $y = \frac{7}{25}(x+8)^2 - 9$                             | $y = \frac{7}{25}(x+8)^2 - 9$                                | $X \leq -11$                | $-2 \geq y \geq -4.645$     | Ear: Left Parabola                |  |
| Line      | $y = 3x$  | $y = 3x$   | all reals                   | $0 \geq y \geq -6$          | Nose: Bridge                      |  |
| Circle    | $(y+6)^2 + x^2 = 4$                                       | $y = \pm \sqrt{(4 - x^2)} - 6$                               | all reals                   | $y \leq -6$                 | Nose: Bulb                        |  |
| Ellipse   | $\frac{(x+4.5)^2}{20.25} + \frac{y^2}{9} = 1$             | $y = \pm \sqrt{9 - \frac{9(x+4.5)^2}{20.25}}$                | all reals                   | $Y \geq 2$                  | Eye: Right bottom ellipse         |  |
| Ellipse   | $1 = \frac{(x+4.5)^2}{20.25} + \frac{(y-4)^2}{9}$         | $y = \pm \sqrt{9 - \frac{9(x+4.5)^2}{20.25}} + 4$            | all reals                   | $Y \leq 2$                  | Eye: Right top ellipse            |  |
| Circle    | $(x+4.5)^2 + (y-2)^2 = 1$                                 | $y = 2 \pm \sqrt{1 - (x+4.5)^2}$                             | all reals                   | All reals                   | Eye: Right pupil                  |  |
| Ellipse   | $\frac{(x-4.5)^2}{20.25} + \frac{y^2}{9} = 1$             | $y = \pm \sqrt{9 - \frac{9(x-4.5)^2}{20.25}}$                | all reals                   | $Y \geq 2$                  | Eye: Left bottom ellipse          |  |
| Ellipse   | $\frac{(x-4.5)^2}{20.25} + \frac{(y-4)^2}{9} = 1$         | $y = \pm \sqrt{9 - \frac{9(x-4.5)^2}{20.25}} + 4$            | all reals                   | $Y \leq 2$                  | Eye: Left top ellipse             |  |
| Circle    | $(x-4.5)^2 + (y-2)^2 = 1$                                 | $y = 2 \pm \sqrt{1 - (x-4.5)^2}$                             | all reals                   | All reals                   | Eye: Left pupil                   |  |
| Ellipse   | $\frac{(x+5.75)^2}{3.0625} + \frac{(y-3.5)^2}{20.25} = 1$ | $y = 3.5 \pm \sqrt{20.25(1 - \frac{(x+5.75)^2}{3.0625})}$    | $X \leq -6$                 | $3.057 \leq y \leq 4.251$   | Eyebrow: Right brow right barrier |  |
| Ellipse   | $\frac{(x+2.25)^2}{3.0625} + \frac{(y-3.5)^2}{20.25} = 1$ | $y = 3.5 \pm \sqrt{20.25(1 - \frac{(x+2.25)^2}{3.0625})}$    | $X \geq -2$                 | $2.579 \leq y \leq 3.375$   | Eyebrow: Right brow left barrier  |  |
| Ellipse   | $\frac{(x+4.5)^2}{20.25} + \frac{(y-2)^2}{9} = 1$         | $y = 2 \pm \sqrt{9 - \frac{9(x+4.5)^2}{20.25}}$              | $-7.475 \leq x \leq -0.5$   | $Y \geq 3.374$              | Eyebrow: Right brow outer edge    |  |
| Ellipse   | $\frac{(x+4.5)^2}{20.25} + \frac{(y-1.75)^2}{3.0625} = 1$ | $y = 1.75 \pm \sqrt{3.0625 - \frac{3.0625(x+4.5)^2}{20.25}}$ | $-7.492 \leq x \leq -0.537$ | $Y \geq 2.579$              | Eyebrow: Right brow inner edge    |  |
| Ellipse   | $\frac{(x-5.75)^2}{3.0625} + \frac{(y-3.5)^2}{20.25} = 1$ | $y = 3.5 \pm \sqrt{20.25(1 - \frac{(x-5.75)^2}{3.0625})}$    | $X \geq 6$                  | $3.057 \leq y \leq 4.251$   | Eyebrow: Left brow right barrier  |  |
| Ellipse   | $\frac{(x-2.25)^2}{3.0625} + \frac{(y-3.5)^2}{20.25} = 1$ | $y = 3.5 \pm \sqrt{20.25(1 - \frac{(x-2.25)^2}{3.0625})}$    | $X \leq 2$                  | $2.579 \leq y \leq 3.375$   | Eyebrow: Left brow left barrier   |  |
| Ellipse   | $\frac{(x-4.5)^2}{20.25} + \frac{(y-2)^2}{9} = 1$         | $y = 2 \pm \sqrt{9 - \frac{9(x-4.5)^2}{20.25}}$              | $7.475 \geq x \geq 0.5$     | $Y \geq 3.374$              | Eyebrow: Left brow outer edge     |  |
| Ellipse   | $\frac{(x-4.5)^2}{20.25} + \frac{(y-1.75)^2}{3.0625} = 1$ | $y = 1.75 \pm \sqrt{3.0625 - \frac{3.0625(x-4.5)^2}{20.25}}$ | $7.492 \geq x \geq 0.537$   | $Y \geq 2.579$              | Eyebrow: Left brow inner edge     |  |
| Ellipse   | $\frac{(y+14)^2}{16} + \frac{(x+1.5)^2}{30.25} = 1$       | $y = -14 \pm \sqrt{16 - \frac{16(x+1.5)^2}{30.25}}$          | $-4.235 \leq x \leq 0$      | $Y \geq -10.529$            | Lip: Upper Right                  |  |
| Ellipse   | $\frac{(y+14)^2}{16} + \frac{(x-1.5)^2}{30.25} = 1$       | $y = -14 \pm \sqrt{16 - \frac{16(x-1.5)^2}{30.25}}$          | $0 \leq x \leq 4.235$       | $Y \geq -10.529$            | Lip: Upper Left                   |  |
| Ellipse   | $\frac{(y+7)^2}{16} + \frac{x^2}{81} = 1$                 | $y = -7 \pm \sqrt{16 - \frac{16x^2}{81}}$                    | $-4.235 \leq x \leq 4.235$  | $Y \leq -10.529$            | Lip: Middle                       |  |
| Ellipse   | $\frac{(y+9)^2}{16} + \frac{x^2}{21} = 1$                 | $y = -9 \pm \sqrt{16 - \frac{16x^2}{21}}$                    | $-4.235 \leq x \leq 4.235$  | $Y \leq -10.529$            | Lip: Lower                        |  |