

Classroom ready research-affirmed tasks and activities for Fractions learning

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Equally partition area, linear, and set models

BACKGROUND

A unit fraction is the basic unit of any fraction and always has a numerator of 1. For example, $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{4}$, $\frac{1}{5}$ are all unit fractions. Every fraction can be decomposed into unit fractions. For example, $\frac{3}{4} = \frac{1}{4} + \frac{1}{4} + \frac{1}{4}$.

One-fourth units (so one-fourth is the unit fraction and we are thinking about 3 of them). Partitioning a model involves determining and creating a unit fraction.

Consider the fraction one and three-fourths. This number can be decomposed using a unit fraction.

One and three-fourths can be composed using a unit fraction.

Use of unit fractions supports a deeper understanding of quantity. Notice that in the student challenge above, early understanding of equivalency is being developed. (i.e., one and one-half is the same as one and two-fourths. Counting by naming the unit fractions helps students to see the parts of the fraction after composing and decomposing. Notice that both counting unit fractions and composing and decomposing fractions are pre-cursors to addition and subtraction. For example, composing 1 one-fourth unit is the same as adding 1 one-fourth unit together to make one and one-half.

TASKS

Overview

Students use paper holding to partition a page of rectangles to create rectangular paper into 4, then 1, then 10 equal portions through a series of steps to create the fraction tasks.

Desktop Fractions

Using their desks or tables, students will estimate and mark fractional amounts along the edge as a linear measure and on the top surface as an area measure. This task is best used after a solid understanding of number line has been established.

A student may say, "One whole is the same as 4 one-fourth units." I added another 2 one-fourth units to the whole to obtain 6 one-fourth units. So I can see that 6 one-fourth units is equal to one and two-fourths.

Use of unit fractions supports a deeper understanding of quantity. Notice that in the student challenge above, early understanding of equivalency is being developed. (i.e., one and one-half is the same as one and two-fourths. Counting by naming the unit fractions helps students to see the parts of the fraction after composing and decomposing. Notice that both counting unit fractions and composing and decomposing fractions are pre-cursors to addition and subtraction. For example, composing 1 one-fourth unit is the same as adding 1 one-fourth unit together to make one and one-half.

Fractions Learning Pathways

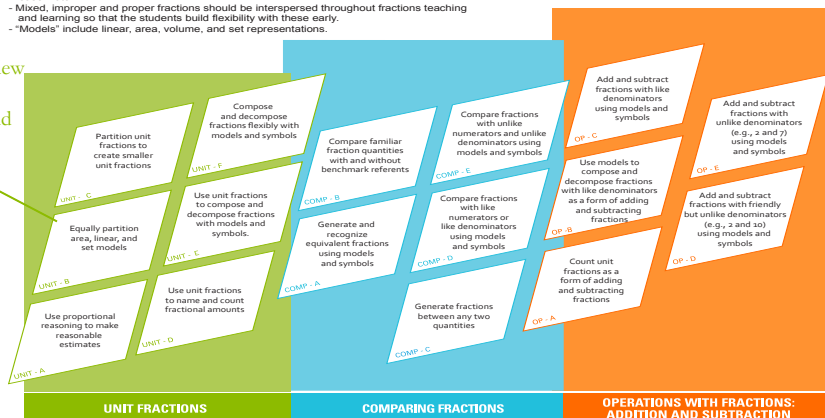
Please Note:

- Mixed, improper and proper fractions should be interspersed throughout fractions teaching and learning so that the students build flexibility with these early.
- "Models" include linear, area, volume, and set representations.

DRAFT v22 Last Revised: Sept 16, 2014

Select a cell to view background information and tasks.

Select a task.



Additional materials added regularly

Coming Soon
Operations with Fractions:
Multiplication and Division

Desktop Fractions

Description

Using their desks or tables, students will estimate and mark fractional amounts along the edge as a linear measure and on the top surface as an area measure. This task is best used after a solid understanding of number line has been established.

Mathematics

This task helps students connect linear models (number lines - which are recommended as a first model), to area models (rectangles). Students learn fractions between 0 and 1, using the edge of their table, and then extend that same fractional amount to cover an area of the desk top. It is important to think flexibly about different representations of the same fractions - not just equivalent fractions but in this case, different models representing the same fractional quantity.

Classroom Connections

Students will:

- develop their understanding of fractional quantities by representing these numbers using different models (linear and area).
- make connections between linear and area models and symbols representations of fractions.

Instructional sequence

1. Pair students and have them select a sheet of which to work. Give each pair of students Set #1. Ask them to place Set #1 at the left edge of the desk, and the 1 at the right edge of the desk. Discuss how the full length of the edge of the desk, which is 1 being used as a number line, is one whole.
2. Ask students to place Set #2 on the desk edge (number line) at the appropriate locations.
3. Have students think about the area of the number line. Ask students to cover one half of the desk top using a material of their choice. Discuss how the area of the top of the desk is an area model.
4. Have students remove Set #2 and provide them with Set #3 to consider for both the linear and area model models.
5. Repeat with Sets #4 and 5. Encourage students to discuss the connections between the models. To consolidate the relationship between the models, play a matching game with linear and area model cards (BLM 1).

Variation: Levels 2, 3, and 4 on desk edge throughout task as benchmarks.

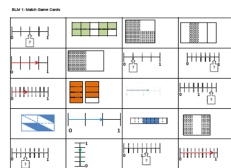
Highlights of student thinking

Students may:

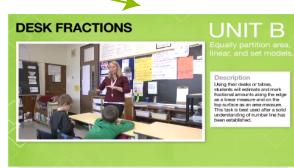
- continue to focus solely on the number line when asked to represent a fraction as an area model.
- not use correct fraction terminology when stating the amount covered (i.e., when discussing 1/2, students may say "1/2" instead of "one-half, two-halves").
- benefit from repetition of the connection between number line and area with prompting and discussion.

Key questions

1. How can both of these (linear and area representations) be showing the same fraction?
2. How is the linear model the same as the area model? How is it different?
3. Where would $\frac{3}{4}$ go?
4. How do you know that your cards are a match?



Blackline Masters



Visuals of Implementation

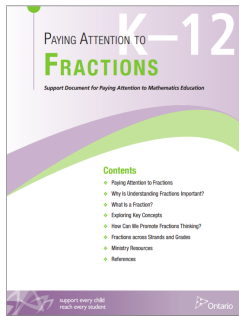


Student Thinking Unpacked

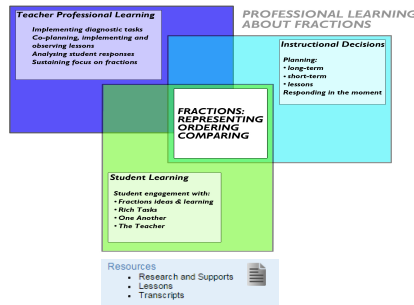
Research Summaries

Created by Dr. Cathy Bruce, Tara Flynn and Shelley Yearley.
Fractions Learning Pathways are inspired by Dr. Jere Confrey's work, based on international and Ontario classroom research, and informed by feedback from classroom teachers and student thinking.

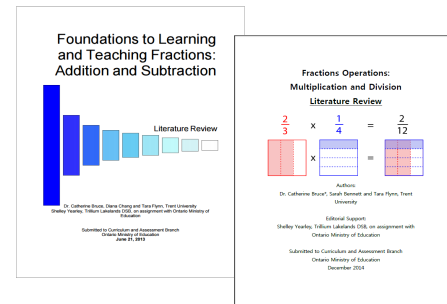
MORE FRACTIONS RESOURCES AVAILABLE



Paying Attention to K-12 Fractions
Deepen your understanding of fractions.
Try some of the tasks with your students.



Digital Paper: Professional Learning about Fractions
Visit the resources section for lessons and lesson bundles.
View the videos to understand the journey and the learning.

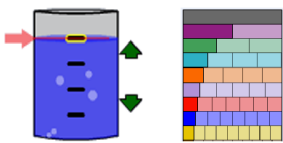


Literature Reviews
Broaden your understanding of the research.
Learn about international teaching practices.

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Learning Tools
for whole class, small group
or individual exploration

Pouring Containers **Fraction Strips**



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Web Conference hosted by Dr. Cathy Bruce: Teaching Fractions – What's the big deal?

Join Dr. Cathy Bruce for a web conference that focuses on the foundations of fraction understanding. Cathy will share current research on what makes fractions challenging for students and key strategies for supporting educators who are teaching fractions.

[Click here to view the recording.](#)



Free resources generated from collaborative action research in Ontario schools.

Research funding and partnerships: Trent University, KNAER,
Ontario Ministry of Education, SSHRC, Ontario School Boards.

Video Studies for professional learning

Video Study 1 – "Thinking about Fractions: moving beyond one half and two quarters"

[Download Full Video Study Guide](#)

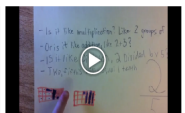
In this video study, we look at a video of a lesson on fractions. The video shows a teacher working with a group of students. The teacher is asking questions that encourage students to think about fractions in a more complex way. The video study guide provides a framework for analyzing the video and reflecting on the teaching practices shown.

The video study guide is available in the following formats:

- Full video study guide
- Shorter version (video 10 min or less)
- Summary of the video study guide (text only)

How do you watch the video?

Transcript
The transcript is available in the following formats:
• Full transcript (video 10 min or less)
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