CHAPTER-11 TRIANGLES

1 Exercise 11.2

Q2. Construct a triangle ABC in which $BC = 8cm, \angle B = 45^{0}$ and AB - AC = 3.5cm.

Solution:

Let A,B and C are the vertices of the triangle with coordinates. Given BC = 8cm.So the coordinates of vertices B,C are:

$$\mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 8 \\ 0 \end{pmatrix}$$

Also given $\angle B = 45^{\circ}$, so by finding the coordinates of the other side we can form a required triangle.

The input parameters for this construction are

Symbol	Value	Description
a	8	BC
θ	45°	$\angle BC$ in $\triangle ABC$
k	3.5	AB - AC i.e $c - b$
$\mathbf{e_2}$	$\begin{pmatrix} 0 \\ 1 \end{pmatrix}$	basis vector

Table 1: Parameters

Caluclating Other Coordinate:

$$\mathbf{A} = c \begin{pmatrix} \cos \theta \\ \sin \theta \end{pmatrix} \tag{1}$$

We know that

$$c = \frac{1}{2(1 - \frac{a\cos\mathbf{B}}{k})} \mathbf{e_2}^{\top} \begin{pmatrix} 1 & 1\\ 1 & -1 \end{pmatrix} \begin{pmatrix} \frac{-a^2}{k}\\ -k \end{pmatrix}$$
 (2)

$$c = \frac{1}{2(1 - \frac{a\cos\mathbf{B}}{k})} \mathbf{e_2}^{\top} \begin{pmatrix} \frac{-a^2}{k} - k \\ \frac{-a}{k} + k \end{pmatrix}$$
(3)

$$c = \frac{1}{2(1 - \frac{8\cos 45^0}{3.5})} \begin{pmatrix} 0 & 1 \end{pmatrix} \begin{pmatrix} \frac{-64}{3.5} - 3.5 \\ \frac{-64}{3.5} + 3.5 \end{pmatrix}$$
(4)

$$c = \frac{1}{2\left(\frac{3.5 - 5.65}{3.5}\right)} \left(\frac{-64 + 12.25}{3.5}\right) \tag{5}$$

$$c = 12 \tag{6}$$

The vertices of $\Delta~ABC$ are

$$\mathbf{A} = 12 \begin{pmatrix} \cos 45^{\circ} \\ \sin 45^{\circ} \end{pmatrix} = \begin{pmatrix} 8.48 \\ 8.48 \end{pmatrix} \tag{7}$$

$$\mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \tag{8}$$

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$$\mathbf{C} = \begin{pmatrix} 8 \\ 0 \end{pmatrix} \tag{9}$$

Construction:

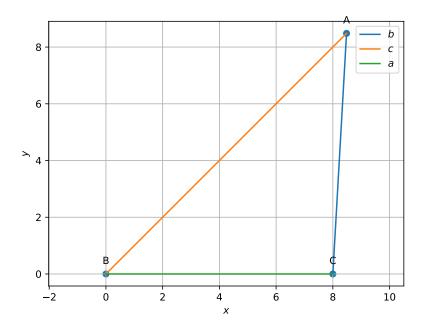


Figure 1: Triangle ABC