

CHAPTER - 9  
TRIANGLES

**EXERCISE - 9.4**

1. A point **E** is taken on the side **BC** of a parallelogram **ABCD**. **AE** and **DC** are produced to meet at **F**. Prove that  $\text{ar}(\mathbf{ADF}) = \text{ar}(\mathbf{ABFC})$ .
2. The diagonals of a parallelogram **ABCD** intersect at a point **O**. Through **O**, a line is drawn to intersect **AD** at **P** and **BC** at **Q**. Show that **PQ** divides the parallelogram into two parts of equal area.
3. The medians **BE** and **CF** of a triangle **ABC** intersect at **G**. Prove that the area of  $\triangle \mathbf{GBC}$  = area of the quadrilateral **AFGE**.
4. In Fig.1, **CD**  $\parallel$  **AE** and **CY**  $\parallel$  **BA**. Prove that  $\text{ar}(\mathbf{CBX}) = \text{ar}(\mathbf{AXY})$

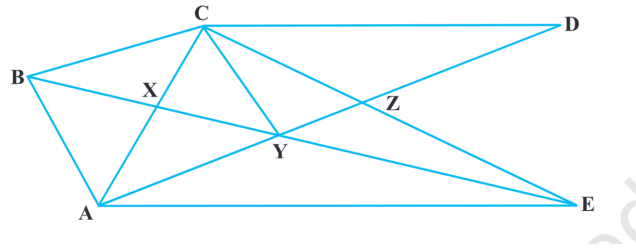


Figure 1

5. **ABCD** is a trapezium in which **AB**  $\parallel$  **DC**, **DC** = 30cm and **AB** = 50cm. If **X** and **Y** are, respectively the mid-points of **AD** and **BC**, prove that  $\text{ar}(\mathbf{DCYX}) = \frac{7}{9} \text{ar}(\mathbf{XYBA})$ .
6. In  $\triangle \mathbf{ABC}$ , if **L** and **M** are the points on **AB** and **AC**, respectively such that **LM**  $\parallel$  **BC**. Prove that  $\text{ar}(\mathbf{LOB}) = \text{ar}(\mathbf{MOC})$ .

7. In Fig.2,  $ABCDE$  is any pentagon.  $BP$  drawn parallel to  $AC$  meets  $DC$  produced at  $P$  and  $EQ$  drawn parallel to  $AD$  meets  $CD$  produced at  $Q$ . Prove that  $\text{ar}(ABCDE) = \text{ar}(APQ)$ .

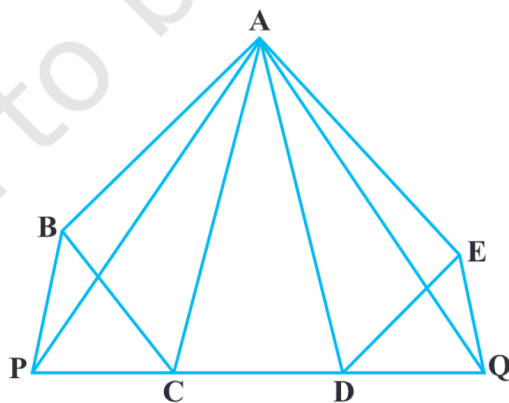


Figure 2

8. If the medians of a  $\triangle ABC$  intersect at  $G$ , show that  $\text{ar}(AGB) = \text{ar}(AGC) = \text{ar}(BGC) = \frac{1}{3} \text{ar}(ABC)$ .
9. In Fig.3,  $X$  and  $Y$  are the mid-points of  $AC$  and  $AB$  respectively,  $QP \parallel BC$  and  $CYQ$  and  $BXP$  are straight lines. Prove that  $\text{ar}(ABP) = \text{ar}(ACQ)$ .

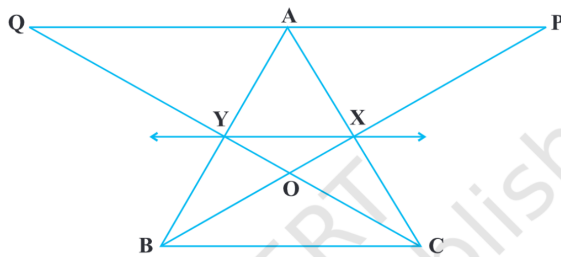


Figure 3

10. In Fig.4, **ABCD** and **AEFD** are two parallelograms. Prove that  $\text{ar}(\mathbf{PEA}) = \text{ar}(\mathbf{QFD})$  [Hint: Join PD].

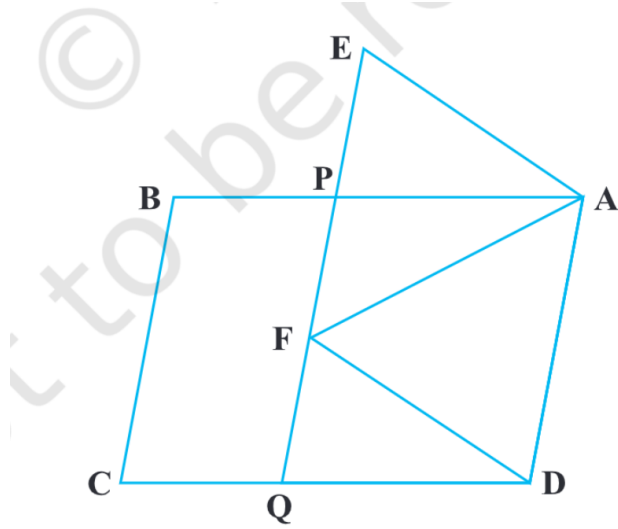


Figure 4