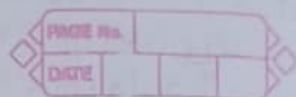


Day 1

Statistics



- Statistics: Statistics is the Science of Collecting, Organizing and analyzing data.
- Data: "facts or pieces of information"
 - 1) Eg: Height of students in a classroom
→ [175 cm, 150 cm, 140 cm, 130 cm, 155 cm]
 - 2) Intelligence Quotient (IQ) of 5 randomly selected individuals (109, 89, 129, 101, 105, 106) → Data.
- Types of Statistics:-

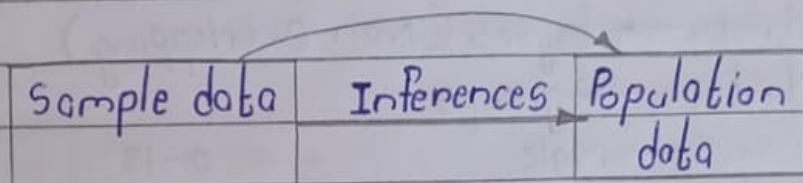
Statistics

Descriptive Stats	Inferential Stats
<ul style="list-style-type: none">• It Consists of Organizing and Summarizing of data.• Eg: Pdf, Histogram, Box plot, Bar Chart, Pie Chart.	<ul style="list-style-type: none">• It Consists of using data that you've measured to form Conclusion.• Eg: Hypothesis Testing, P-value, Z test, t test, Anova, Chisquare.

Eg: Lets say there are 20 maths classes at your university and you've collected the age of students in one class.

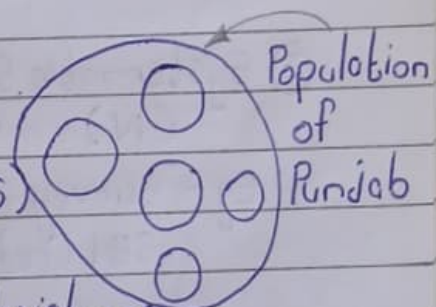
Ages [21, 20, 18, 34, 17, 22, 24, 25, 26, 23, 22]

- Descriptive Stats:- what is the average age of student in your maths class?
- Inferential Stats:- Are the ages of students in this maths classroom similar to what you would expect in a normal maths class at this university?



Population and Sample Data: Inferential Statistics
Ex:-

- 1) Elections - Punjab (Exit Polls)
[AAP, Congress]
(Stratified + Random S)



- 2) Eg - 2015 → Data Scientist
Jackets → Size: 10K, 40K → Christmas
10% Small, 20% XL, 40% L, 2-3% XXL
Only 1-2% → waste.

Population (N) Sample (n)

- Sampling Techniques

 - ① Simple Random Sampling
 - ② Stratified Sampling
 - ③ Systematic Sampling
 - ④ Convenience Sampling



- ① Simple Random Sampling: Every member of the population (N) has an equal chance of being selected for your sample (n).

- ② Stratified Sampling:

Strata \rightarrow Layers (Non Overlapping)

Clusters \rightarrow groups

Gender	Male	Age groups	0-18	Blood Group
			18-35	Tax Slabs
	Female		35-60	Courses

- ③ Systematic Sampling:

(N) \rightarrow select every n^{th} individual

Eg - Survey \rightarrow Mail (luggage checking)
SBI Credit Card

- ④ Convenience Sampling: Only those people who are interested will only be participating.

Eg - Data Science - AI ; Healthcare (Blind People)

Youtube Survey

RBI - House hold Survey - Female

- Variable

A variable is a property that can take on any value.

Eg - Height = 182
150
145
160

[182, 150, 145, 160]

⌋
NO

• Two kinds of Variable :

① Quantitative Variable : Measured Numerically
[Add, Subtract, \times , \div]

② Qualitative Variable :

Eg - Gender - Male [Based on some characteristics
Female we can divide Categorical
variables]

[Quantitative \rightarrow Qualitative Variable]

Eg :- IQ

0 - 10	10 - 50	50 - 100
Less IQ	Medium IQ	Good IQ

Quantitative

Discrete Variable

Eg: whole number

Eg: NO. of Bank Accounts
[2, 3, 4, 5, 6, 7]

Eg: Total No. of Children in
a family

Eg: Total no. of employees
in a Company Eg: 10k.

Continuous Variable

Eg: Height = 172.5,
162.5 cm, 163.5 cm

Rainfall: 1.35, 1.25, 1.75
weight, Temp,
stock Price.

• Assignment Questions -

① What kind of variable Marital Status is?

Ans Categorical

② What kind of variable Nile River Length is?

Ans Continuous Quantitative

③ What kind of variable Movie duration is?

Ans Continuous Quantitative

④ What kind of variable IQ is?

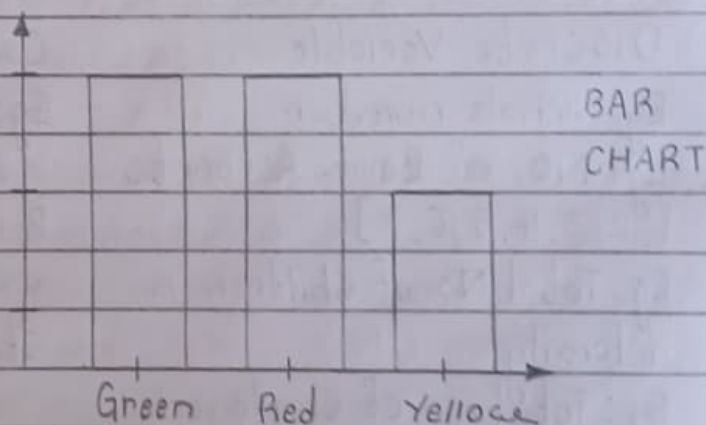
Ans. Continuous Variable

- Frequency Distribution

Sample Dataset: Green, Red, Yellow, Green, Red, Yellow, Green, Red

Colors	Frequency
Green	3
Red	3
Yellow	2

① BAR GRAPH Frequency



- Variable Measurement Scales

4 types of Measured Variable

① Nominal data (Categorical data)

Eg: Colors, Gender, types of flowers

② Ordinal data:

Student (Marks)	Rank	
100	1	} Ordinal Data
96	2	
57	4	
85	3	
44	5	

Degree	Salary
PHD	1
B.E.	3
Master	2
BCA	4
12	5

③ Interval data:

- A variable measured on an interval scale gives information about more or betterness as ordinal scales do.
- Temperature using Celsius or Fahrenheit is a good example.

④ Ratio data:

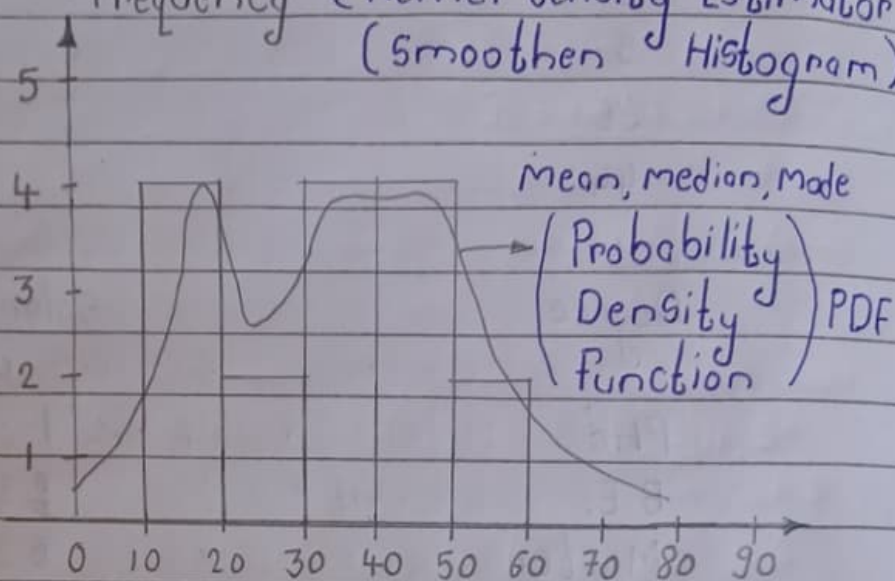
Something measured on ratio scale has the same properties that an interval scale has except, with a ratio scaling, there is an absolute zero point. Temperature measured in Kelvin is an example.

• Histograms: Continuous

Ages = [10, 12, 14, 18, 24, 26, 30, 35, 36, 37, 40, 41, 42, 45, 50, 51]

Bins = 10

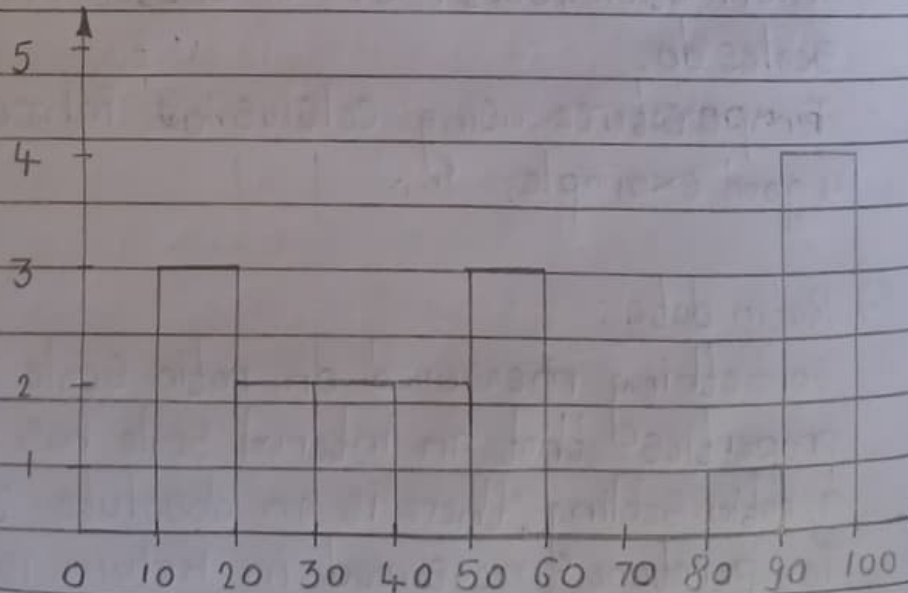
1) Frequency (Kernel density Estimator)
(Smoothed Histogram)



0-50 → 0-5, 5-10, 10-15, 15-20, 20-25, 25-30, 30-35

Assignment

2) Eg: 10, 13, 18, 22, 27, 32, 38, 40, 45, 51, 56, 57, 88, 90, 92, 94, 99 (Bins = 10)



- Intermediate Stats
- ① Measure of Central Tendency
- ② Measure of Dispersion
- ③ Gaussian Distribution
- ④ Z-Score
- ⑤ Standard Normal Distribution
- ⑥ Central Limit Theorem

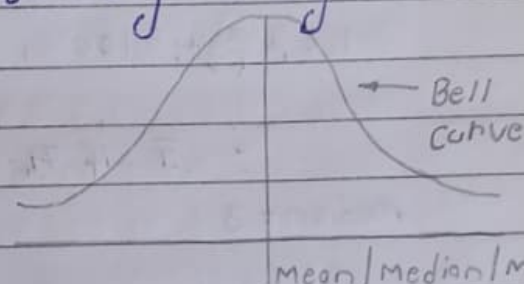
① Measure of Central Tendency Central Position of dataset

• Mean

• Median

• Mode

EDA & Feature Engineering



Population (N)

Sample (n)

i) Mean

$x = [1, 1, 2, 2, 3, 3, 4, 5, 5, 6]$ Sample

$$\mu = \frac{\sum_{i=1}^N x_i}{N}$$

Population mean

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$$

Sample mean

$$= \frac{1+1+2+2+3+3+4+5+5+6}{10}$$

$$= \frac{32}{10} = 3.2$$

2) Median

1, 2, 2, 3, 4, 5

1, 2, 2, 3, 4, 5, 100

$$\bar{x} = \frac{1+2+2+3+4+5}{6} = \frac{17}{6} = 2.83$$

$$\begin{aligned}\bar{x} &= \frac{1+2+2+3+4+5+100}{7} \\ &= \frac{117}{7} = 16.71\end{aligned}$$

Median

1, 2, 2, 3, 4, 5, 100

1, 2, 2, 3, 4, 5

$$\bar{x} = 16.71$$

median = 3

$$\begin{aligned}&\downarrow \\ &2.5 \approx 2.83\end{aligned}$$

3) Mode : Highest Frequency

1, 2, 2, 3, 3, 3, 4, 5, 6, 6, 7

1, 2, 2, 3, 3, 4, 4, 5, 6

Error in Python
in new python
[2, 3, 4]

Feature Engineering

NAN values \Rightarrow Continuous values + outlier

Mean

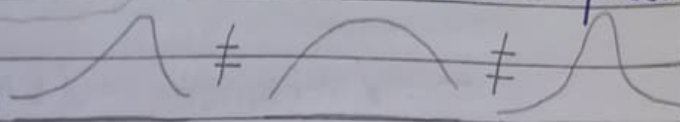
median

Categorical Variable
mode

② Measure of Dispersion: Spread → How data is spread

① Variance

② Standard deviation



① Variance Benes Correction; Degree of Freedom

Population Variance

Sample Variance

$$\sigma^2 = \frac{\sum_{i=1}^N (x_i - \mu)^2}{N}$$

Population mean

$$s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}$$

Sample mean

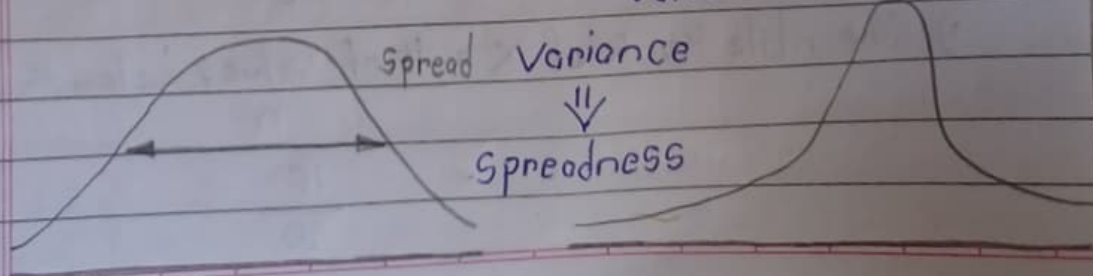
Eg:-

$x = [1, 2, 2, 3, 4, 5]$

x	\bar{x}	$x - \bar{x}$	$(x - \bar{x})^2$	
1	2.83	-1.83	3.34	
2	2.83	-0.83	0.6889	10.84
2	2.83	-0.83	0.6889	5
3	2.83	0.17	0.03	2.168
4	2.83	1.17	1.37	$n=6$
5	2.83	2.17	4.71	
$\bar{x} = 2.83$			10.84	

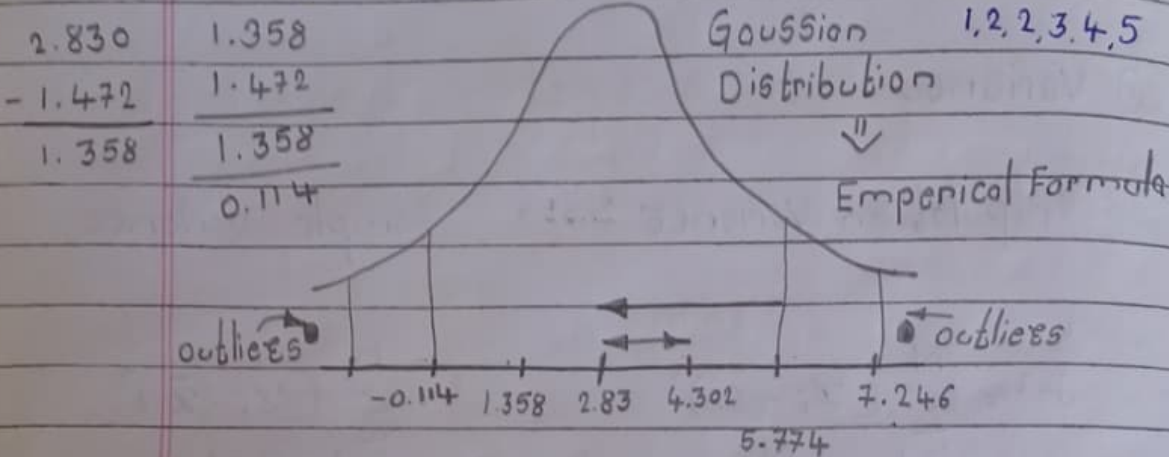
Variance = 6.42 ; Spread ↑↑ σ^2 Variance ↑
Spread ↑

Variance = 2.168



② Standard Deviation:

$$\sigma = \sqrt{\text{variance}} = \sqrt{2.168} = 1.472$$



2.83 • Percentiles and Quartiles

1.472 Percentages: 1, 2, 3, 4, 5

4.302 % of numbers that are odd?

$$\% \text{ of odd} = \frac{3}{5} = 60\%$$

5.774

1.472

Percentile: (CAT, GATE, SAT)

7.246

Defⁿ:- A percentile is a value below which a certain percentage of observation lie

- 99 percentile means the person has got better marks than 99% of the students.

Average $\Rightarrow 5$

Dataset:- 2, 2, 3, 4, 5, 5, 5, 6, 7, 8, 8, 8, 8, 8, 9, 9, 10, 11, 11, 12

$n=20$

What is the percentile ranking of 10?

$$\begin{aligned} \text{1) Percentile Rank of } x &= \frac{\# \text{ of values below } x}{n} \times 100 \\ &= \frac{16}{20} \\ &= 80 \text{ Percent} \end{aligned}$$

2) What value exists at percentile ranking of 25%?

$$\text{value} = \frac{\text{Percentile}}{100} \times (n+1) \text{ Demog 2.2}$$

$$= \frac{25}{100} \times (21)$$

$$= 5.25 \rightarrow \text{Index}$$

$$\text{value} = 5 \text{ Quartiles (25\%)}$$

• Five Number Summary

① Minimum

② First Quartile (25%) Q_1

③ Median

④ Third Quartile (75%) Q_3

⑤ Maximum

Inter Quarter Range (75% - 25%) $Q_3 - Q_1$

Removing the outliers

[1, 2, 2, 2, 3, 3, 4, 5, 5, 5, 6, 6, 6, 6, 7, 8, 8, 9, 27]

(Lower Fence \longleftrightarrow Higher Fence)

$$\text{Lower Fence} = Q_1 - 1.5(IQR)$$

$$\text{Higher Fence} = Q_3 + 1.5(IQR)$$

$$IQR = Q_3 - Q_1 = 7 - 3 = 4$$

$$(25\%) Q_1 = \frac{25}{100} \times (20) = 5^{\text{th}} \text{ index}$$

$$\text{Lower Fence} = 3 - 1.5(4)$$

$$= 3 - 6 = -3$$

$$Q_1 = 3$$

$$\text{Higher Fence} = 7 + 1.5(4)$$

$$= 7 + 6 = 13$$

$$(75\%) Q_3 = \frac{75}{100} \times 20 = 15^{\text{th}} \text{ index}$$

$$[-3 \longleftrightarrow 13]$$

$$Q_3 = 7$$

Remaining

1, 2, 2, 2, 3, 3, 4, 5, 5, 5, 6, 6, 6, 6, 7, 8, 8, 9, 27

5 Number Summary

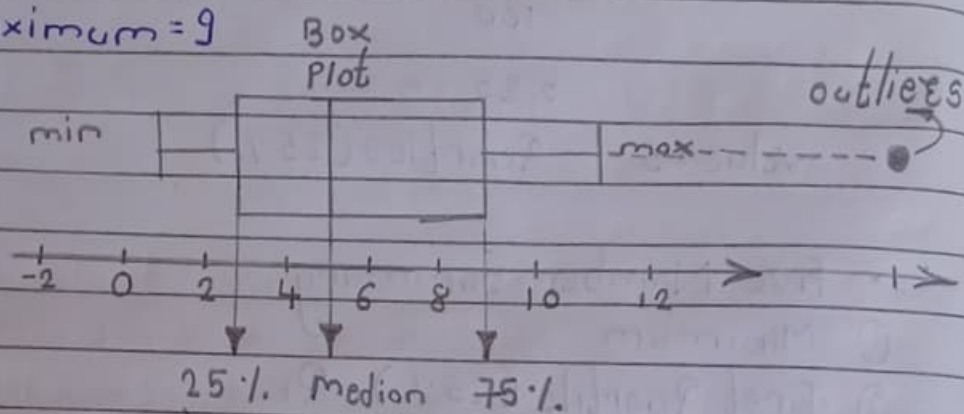
Minimum = 1

$Q_1 = 3$

Median = 5

$Q_3 = 7$

Maximum = 9



• Distribution

- ① Normal / Gaussian Distribution
- ② Standard Normal Distribution
- ③ Z-Score
- ④ Log Normal Distribution
- ⑤ Bernoulli's Distribution
- ⑥ Binomial Distribution

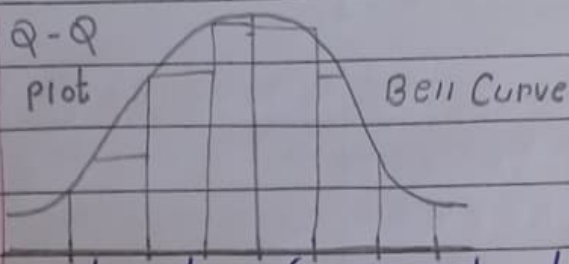
Tossing Coin

P		P		P		P		P	
Q		Q		Q		Q		Q	

① Gaussian / Normal Distribution

80-20%

Q-Q
plot



Properties (Power, Law)

① Empirical Rule of Gaussian Distribution

Dataset \rightarrow (IRIS Dataset) \rightarrow Petal, Sepal length
weight of human Being, Height
68.2 - 95.4 - 99.7

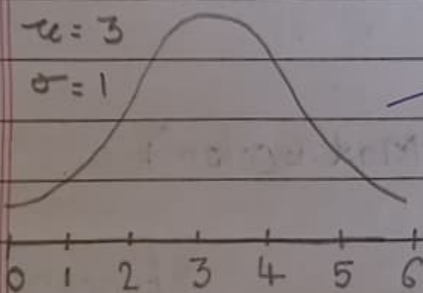
② Standard Normal Distribution

(1, 2, 3, 4, 5)

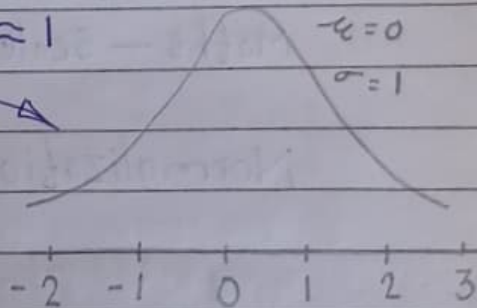
$\mu = 3$

$\sigma = 1.414 \approx 1$

$\mu = 3$
 $\sigma = 1$



$\mu = 0$
 $\sigma = 1$



(1, 2, 3, 4, 5)

$$Z\text{-Score} = \frac{x - \mu}{\sigma}$$

$\mu = 0$
 $\sigma = 1$

$$\frac{2-3}{1} ; \frac{3-3}{1} = 0 ; \frac{1-3}{1} = -2$$

Standardization

Vs

Normalization

Years

kg

INR

Age

weight

Salary

25

75

25k

26

80

30k

28

85

40k

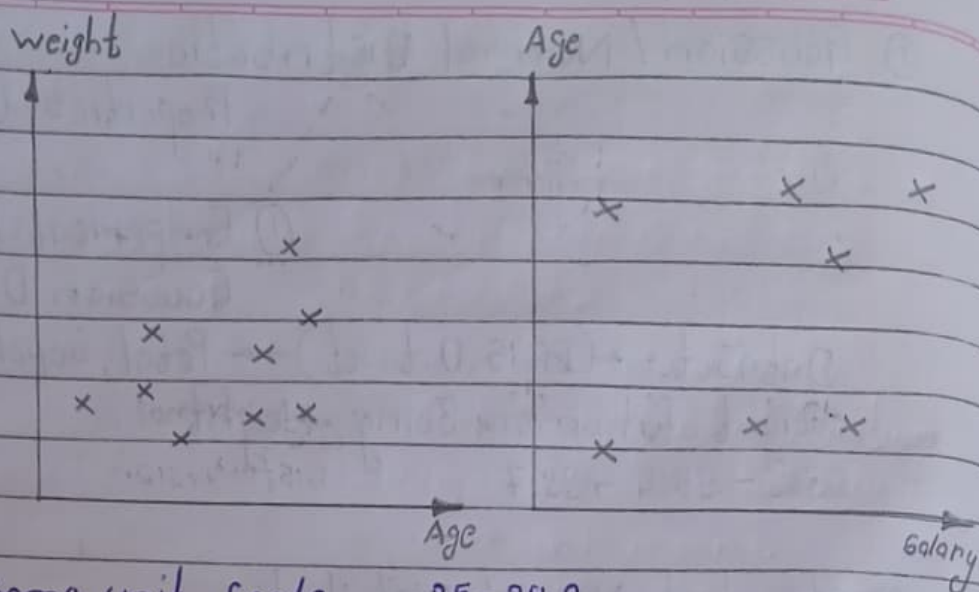
30

60

80k

32

70

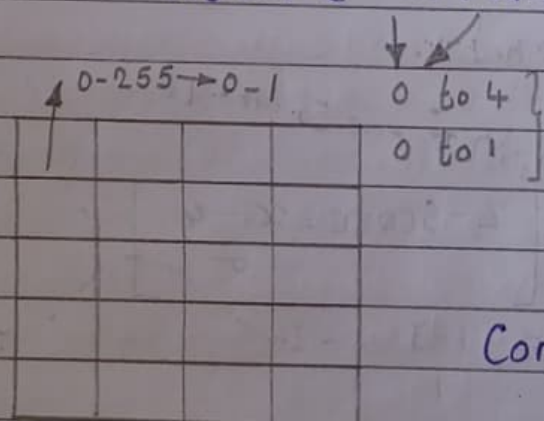


Same unit Scale 25-28.2

2.56

Maths - Scale

Normalization (Min Max Scaler)



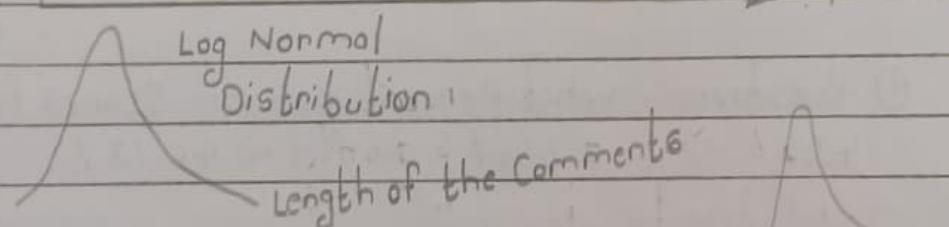
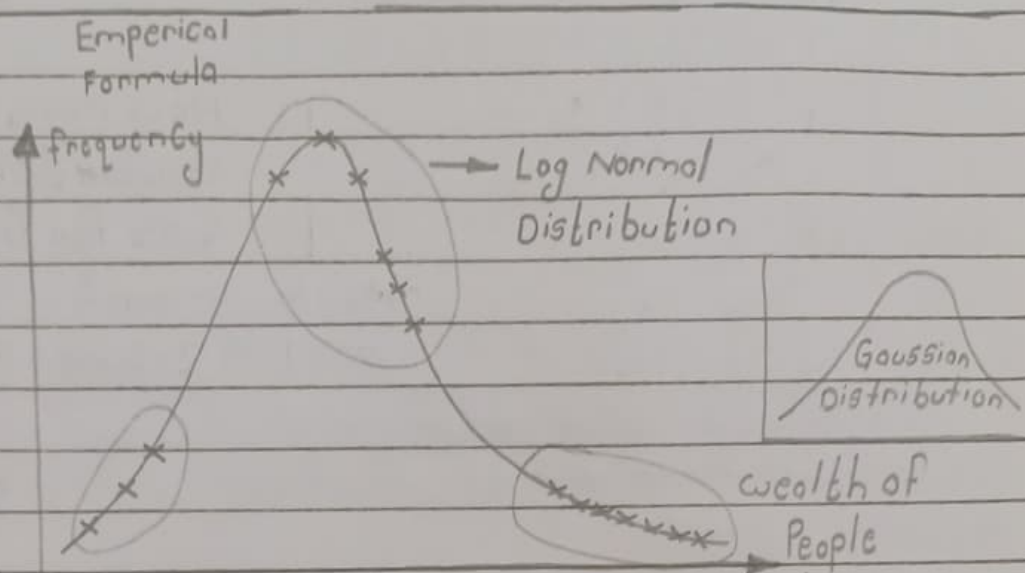
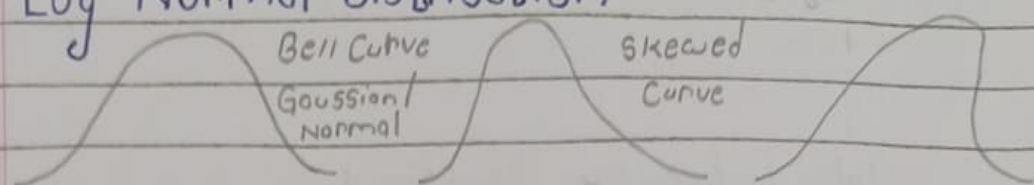
Standardization (ML)

Normalization (CNN)

Convolutional Neural Network

f_1		f'_1
2	$x_{\text{Norm}} = \frac{x_i - x_{\text{min}}}{x_{\text{max}} - x_{\text{min}}}$	0.14
5		0.571
6	\Downarrow	0.71
8	Min Max Scaler	1
1		0
$= \frac{2-1}{8-1} = \frac{1}{7} = 0.142$		$\frac{8-1}{8-1} = 1$
$= \frac{5-1}{8-1} = \frac{4}{7} = 0.571$		$\frac{1-1}{8-1} = 0$

③ Log Normal Distribution

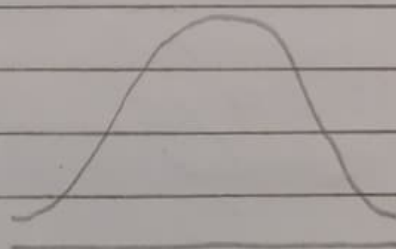
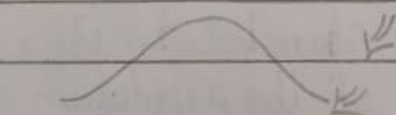


$x = \text{Log Normal Distribution}$

$$y = \ln(x)$$

$$x = \exp(y) \rightarrow e^y$$

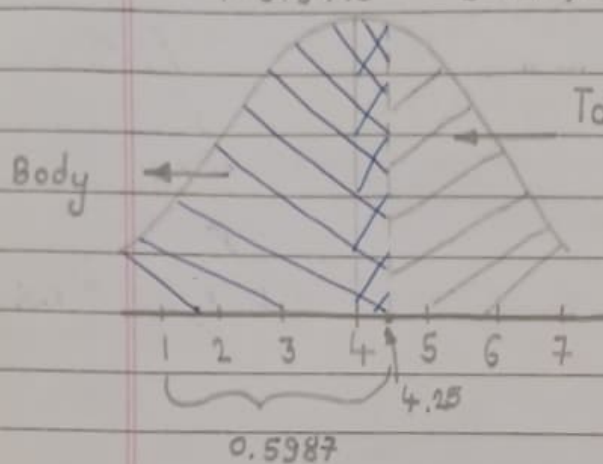
x	$y = \ln(x)$
25	—
30	—
40	—
45	—



④ Bernoulli's Distribution

$$\textcircled{1} Z\text{-Score} = \frac{x_i - \mu}{\sigma}$$

Stats Interview Question

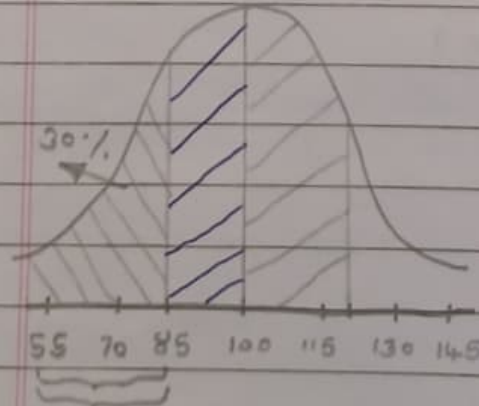
 $1 - 0.5 + \alpha$ {1, 2, 3, 4, 5, 6, 7}


How many standard deviation
4.25 fall from the
 $\mu = 4$ mean?

$$\begin{aligned} \sigma &= 1 \Rightarrow Z\text{-Score} = \frac{x_i - \mu}{\sigma} \\ &= \frac{4.25 - 4}{1} \\ &= 0.25 \end{aligned}$$

$\textcircled{1}$ Question:- what percentages of scores fall above 4.25? $\Rightarrow 1 - 0.5987 = 0.4013 \Rightarrow 40.13\%$

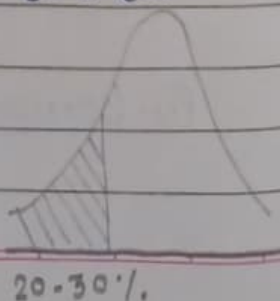
$\textcircled{2}$ Question:- In India the average IQ is 100, with a standard deviation of 15. what is the percentage of the population would you expect to have an IQ lower than 85? \Rightarrow



$$\begin{aligned} Z\text{-Score} &= \frac{85 - 100}{15} \\ &= \frac{-15}{15} = -1 \end{aligned}$$

$\textcircled{1}$ Area under this Curve

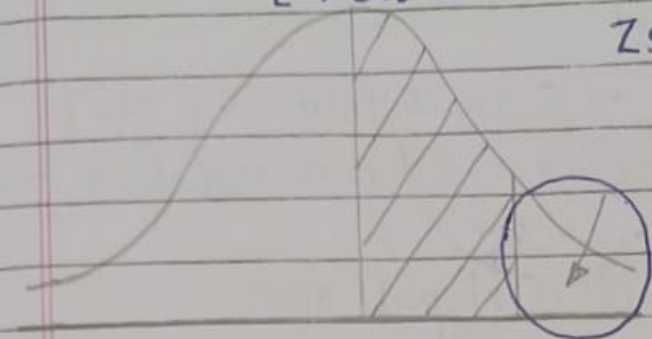
$$0.5 - 0.15866 = 0.34134 \Rightarrow 34.14\%$$



[Greater 100 less than 125]

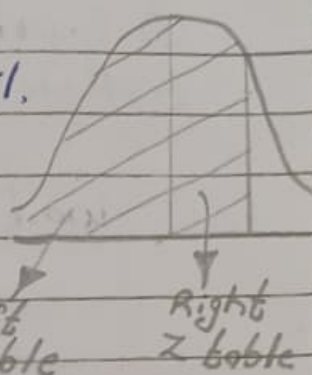
$$Z\text{score} = \frac{125 - 100}{15} = \frac{25}{15}$$

$$= 1.666$$



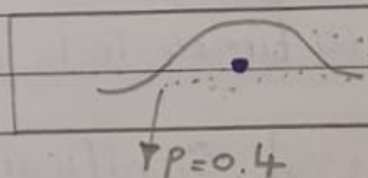
$$\text{Ans} = 0.4515$$

$$= 45.15\%$$



$$0.5 - 0.4515 = 0.0485 = 4.8\%$$

- P value, Hypothesis Testing, Confidence Interval
out of all 100 touches
the no. of touches is



space bar BO
key

out of all 100 touches,
the no. of items times
is 40 times.

- Hypothesis Testing, C.I, Significance value Together

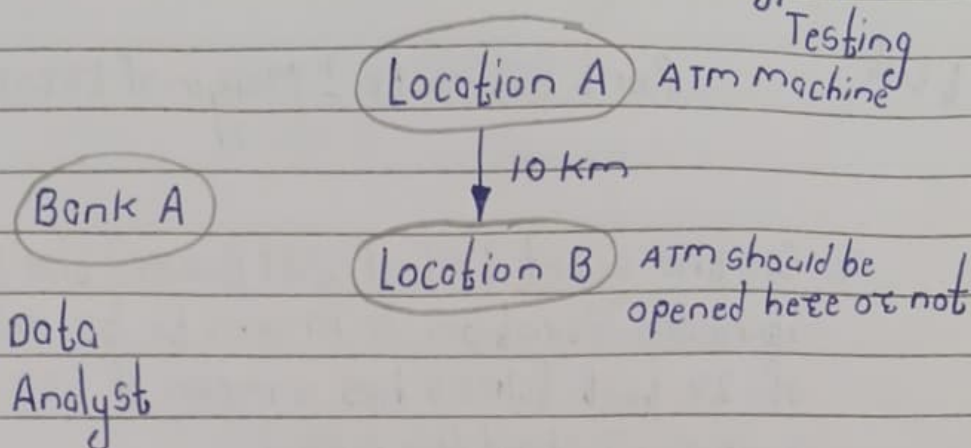
Coin \rightarrow Test whether the coin is a fair coin or
not by performing 100 tosses.

$$P(H) = 0.5$$

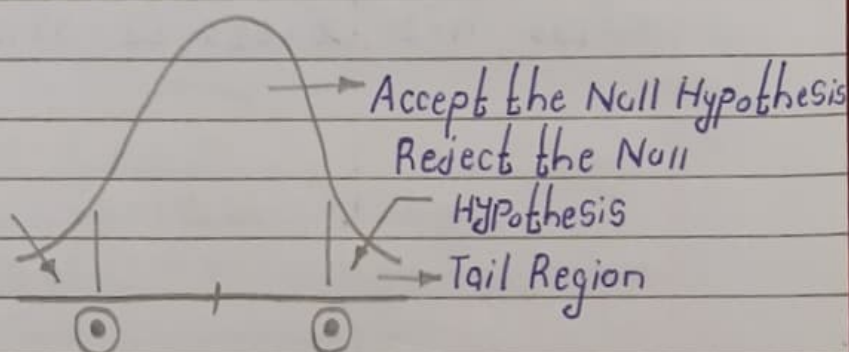
$$P(T) = 0.5$$

Real World Project

Hypothesis Testing

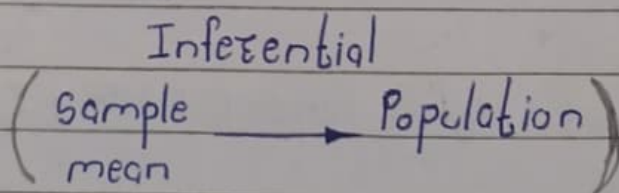
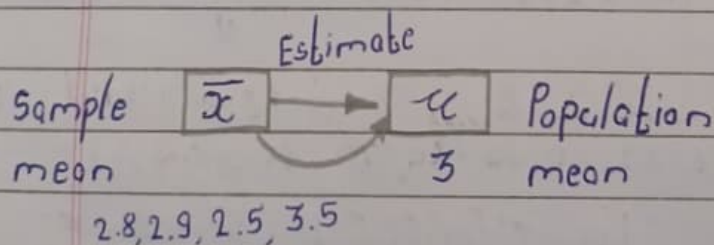


Confidence Interval



Point Estimator

The value of any statistics that estimates the value of a parameter is called point Estimator.



Confidence Interval

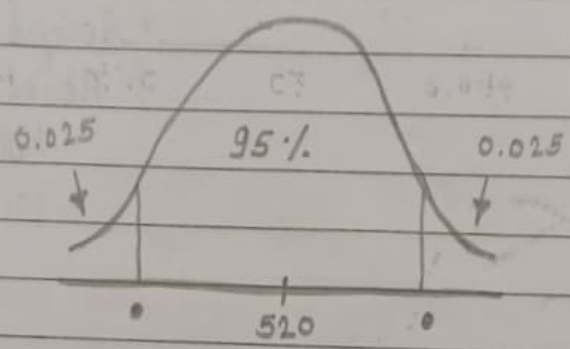
t test

Point Estimate \pm Margin of Error \Rightarrow Population.

Q. On the quant test of CAT Exam, the Population Standard deviation is known to be 100. A sample of 25 test takers has a mean of 520. Construct a 95% CI about the mean?

Ans:-

$\sigma = 100, n = 25, \bar{x} = 520, CI = 95\%, \alpha = 0.05$



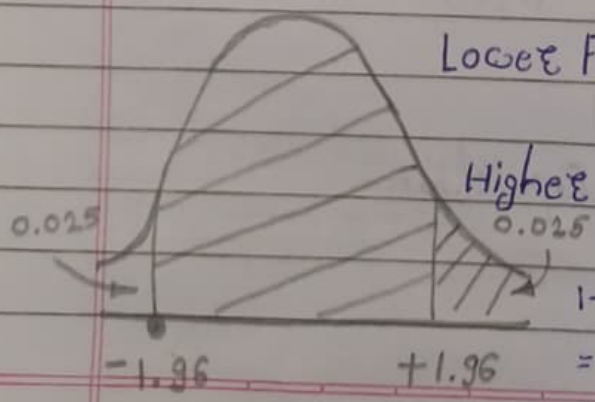
① Population Std is given [Z score] \rightarrow z table

Point Estimator \pm Margin of Error \rightarrow C.I.

$$\bar{x} \pm Z_{\alpha/2} \frac{\sigma}{\sqrt{n}} \leftarrow \text{Standard Error}$$

$$\text{Lower Fence C.I.} = \bar{x} - Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$\text{Higher Fence C.I.} = \bar{x} + Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$



$$1 - 0.025 = 0.9750$$

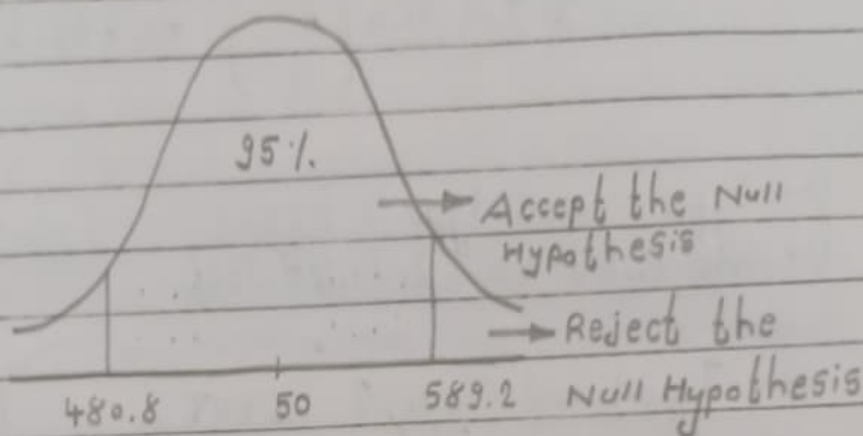
$$Z_{0.05} \Rightarrow Z_{0.025} = 1.96$$

$$\text{Lower Fence} = 520 - (1.96) \times \frac{100}{\sqrt{25}}$$

$$= 520 - (1.96) \times 20$$

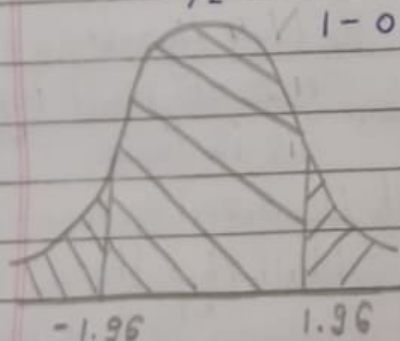
$$= 480.8$$

$$\text{Higher Fence} = 520 + (1.96) \times 20 = 559.2$$



$$Z_{\alpha/2} = Z_{0.025}$$

$$1 - 0.025 = 0.9750$$



$$\uparrow 488.64, 581.36$$

- On the quant test of CAT Exam, a sample of 25 test takers has a mean of 520 with a sample standard deviation of 80. Construct 95% CI about the mean?

Ans $\bar{x} = 520$, $s = 80$, $\alpha = 0.05$, $n = 25$

t-test \rightarrow t-table

(Because population sd is not given)

$$\bar{x} \pm t_{\alpha/2} \left(\frac{s}{\sqrt{n}} \right) \rightarrow \text{standard error}$$

$$t_{0.025}$$

• Degree of freedom = $n - 1 = 25 - 1 = 24$

$$\bar{x} \pm 2.064 \left(\frac{80}{5} \right) \Rightarrow 486.976 \leftrightarrow 553.024$$

- 1) Type 1 and Type 2 Error
- 2) One Tailed Vs 2 Tailed Test

1) Type 1 and Type 2 Error

Reality
check

$H_0 \Rightarrow$ Coin is fair

$H_1 \Rightarrow$ Coin is not fair

Null Hypothesis

$H_0 \rightarrow$ The Criminal is not guilty

$H_1 \rightarrow$ " " is guilty

① Null Hypothesis is

True or Null Hypothesis is False

Decision [Experiments]

Null Hypothesis is True or False

Outcome 1 :-

We reject the Null Hypothesis in reality if it is false \rightarrow Yes

Outcome 2 :-

We reject the Null Hypothesis when in reality it is true. \rightarrow No \rightarrow Type 1 Error \times

Outcome 3 :-

We accept the Null Hypothesis when in reality it is false. \rightarrow Type 2 Error \times

Confusion matrix
(stock market is going
to crash)

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Outcome 4 :- We accept the Null Hypothesis
when in reality it is True. ✓

2) 1 Tail and 2 Tail Test

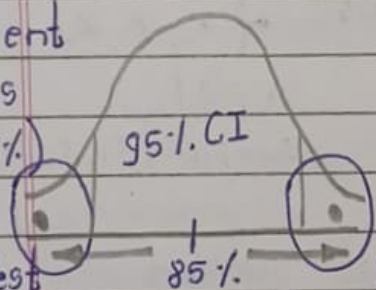
Eg:- Colleges in Karnataka has an 85% placement rate. A new college was recently opened and it was found that a sample of 150 students had a placement rate of 88% with standard deviation of 4%. Does this college has a different Placement rate?

→ 85% $\alpha = 0.05 = 95\%$ CI

Placement
rate less
than 85%

(Placement rate greater
than 85%)

2 Tail Test



① Z test Hypothesis Testing

② T test Hypothesis Testing

③ Significance value and P value

④ ANOVA Test

⑤ CHI SQUARE Test

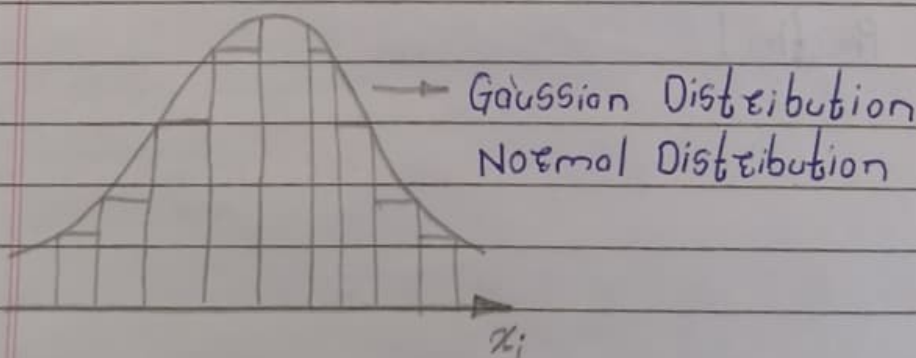
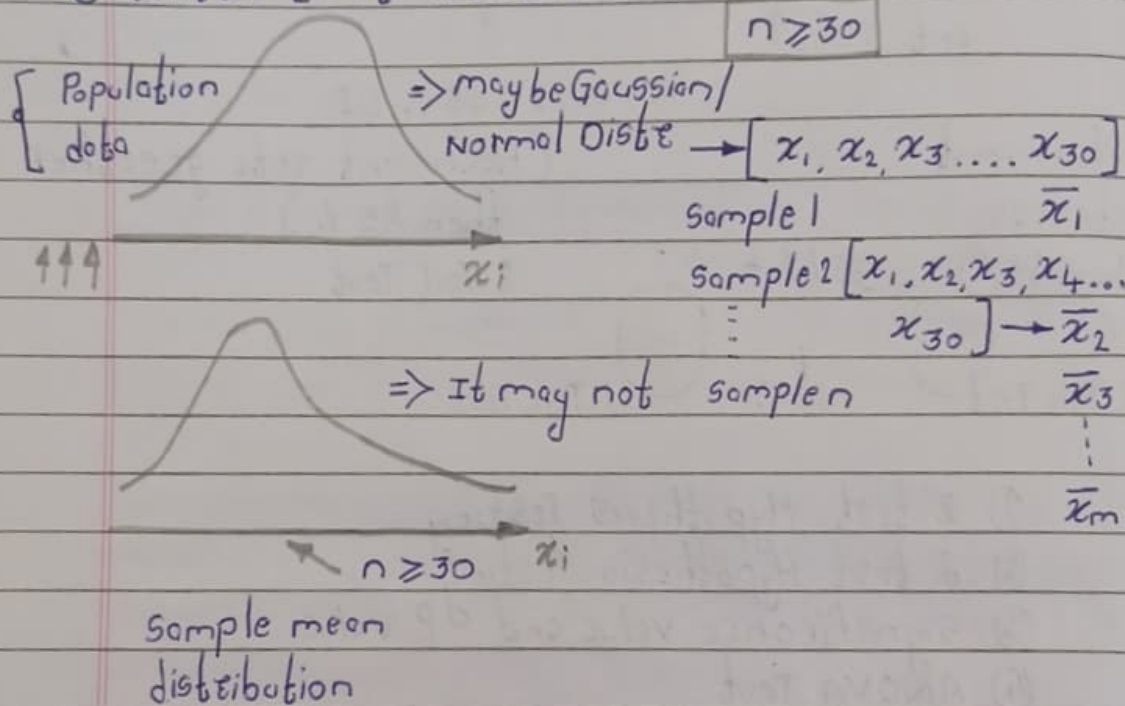
⑥ Practical

① Central Limit Theorem

② Inferential Statistics

- Z test { Z table }
- t test { t table }
- Z test proportion population
- Chi Square (Categorical Test)
- ANOVA (F Test)

① Central Limit Theorem



② Inferential Statistics { Data Analyst, Data Scientist }

• 100 K \Rightarrow T-shirt \rightarrow NO \rightarrow Sample data \rightarrow XL, L, Small

• ineuron \rightarrow Meetup \rightarrow Hitesh \rightarrow 300-400 people \rightarrow T-shirts \rightarrow ordered

$\left[\begin{array}{cc} 20\% \text{ L} & 10\% \text{ XL} \\ 10\% \text{ XL} & 60\% \text{ Medium} \end{array} \right]$ 500 t-shirts

\rightarrow Next Event

• ATM

$\alpha, 5$

• Measure the size of \bar{x} entire shocks C.I. []

• Amazon delivery { Percentile, Quartiles }

• Hypothesis Testing

i) A factory has a machine that fills 80 ml of baby medicine in a bottle. An employee believes the average amount of baby medicine is not 80 ml, using 40 samples, he measures the average amount dispensed by the machine to be 78 ml with a standard deviation of 2.5

① State Null and Alternate hypothesis

② At a 95% C.I., is there enough evidence to support machine is not working properly.

Ans Step 1 :- Given - $n = 40$, $\bar{x} = 78$, $s = 2.5$

$H_0 = \mu = 80$ { Null Hypothesis }

$H_1 = \mu \neq 80$ { Alternate Hypothesis }

Step 2 :-

$\alpha = 0.05$ (1 - 0.95)

C.I = 95%

why Z test?

① $n \geq 30$

② Population std or sample std

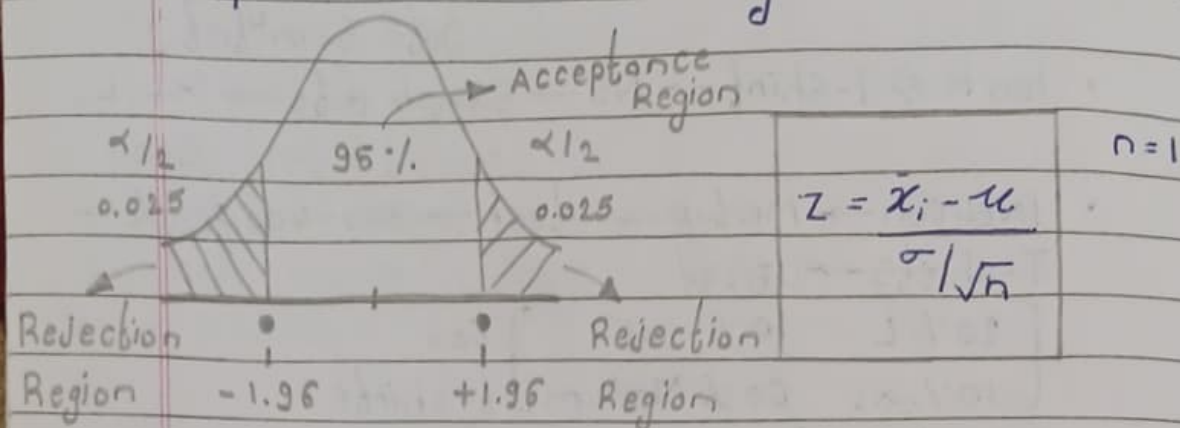
why t test?

① $n < 30$

② sample std

DATE				
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Step 3 :- Decision Boundary



Step 4 :- Calculate Test Statistics

$$Z = \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}}$$

Sample standard deviation $\leftarrow \frac{s}{\sqrt{n}} \rightarrow$ Standard Error

$$= \frac{78 - 80}{2.5 / \sqrt{40}} = \frac{-2 \times \sqrt{40}}{2.5} = \frac{-2 \times 6.32}{2.5} = -5.05$$

Step 5 :- State the Results

Decision Rule :- If $Z = -5.05$ is less than -1.96 or greater than 1.96 , then reject the null hypothesis with 95% C.I

Reject H_0 Null Hypothesis [There is some fault in the machine]

- 2) In the population the average IQ is 100 with a standard deviation of 15. A team of Scientists wants to test new medication to see if it has a +ve or -ve effect, or no effect at all. A sample of 30 participants who have taken the medication has a mean of 140. Did the medication affect Intelligence? C.I = 95%.

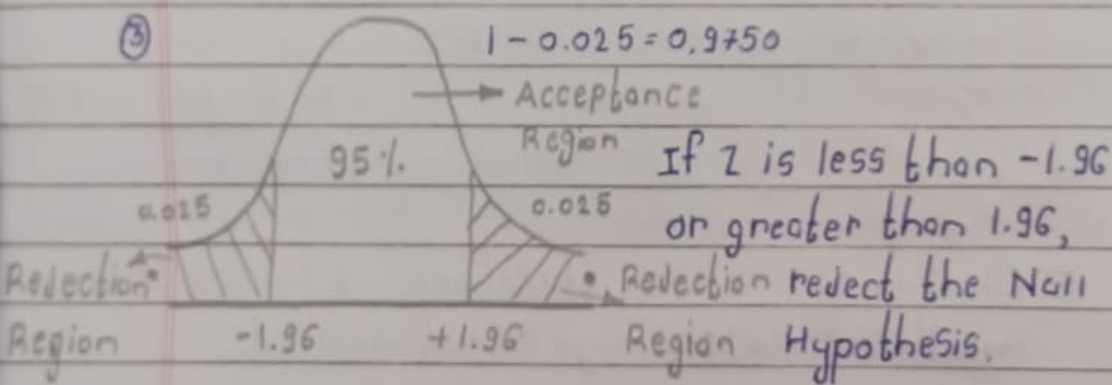
Ans: $\sigma = 15, n = 30, \bar{x} = 140$

① $H_0 = \mu = 100$

$H_1 = \mu \neq 100$

② $\alpha = 0.05$; C.I = 95%

③



④
$$Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}} = \frac{140 - 100}{15 / \sqrt{30}} = 14.60$$

- ⑤ $14.60 > 1.96$, Reject the Null Hypothesis

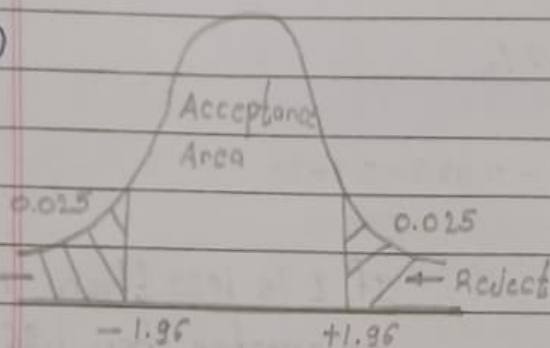
- 3) A Complaint was registered, the boys in the Municipal Primary School are underfed. Average weight of boys of age 10 is 32 Kgs, with S.D = 9 Kgs. A sample of 25 boys was selected from the municipal school and the average weight was found to be 29.5 Kgs. with C.I = 95%, check whether it is True or false?

Ans $\mu = 32 \text{ Kgs}$, $\sigma = 9 \text{ Kgs}$, $n = 25$, $\bar{x} = 29.5$, $\alpha = 0.05$

① $H_0 = \mu = 32$ ② $\alpha = 0.05$

$H_1 = \mu < 32$

③



④
$$Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$$

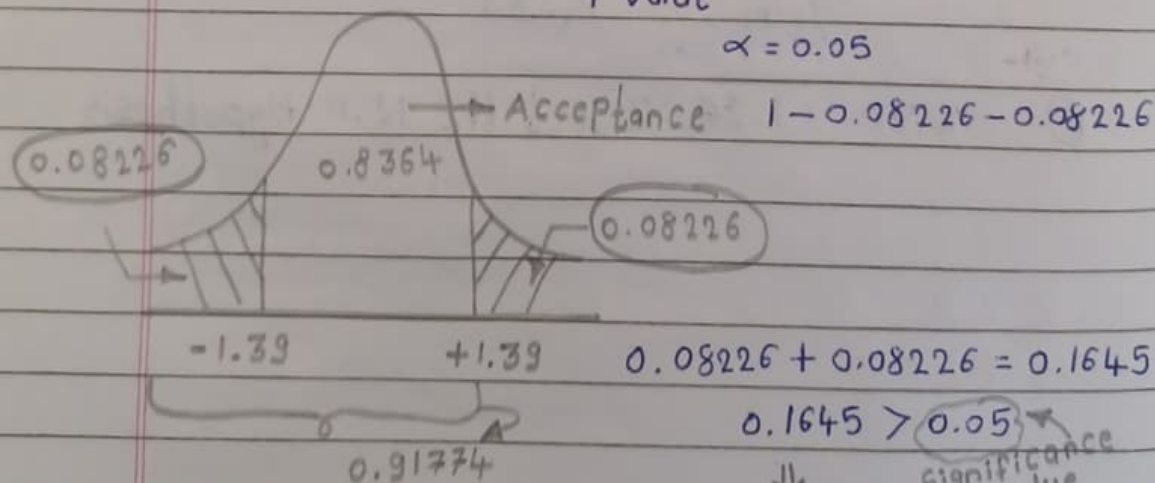
$$= \frac{29.5 - 32}{9 / \sqrt{25}} = -1.39$$

- ⑤ Conclusion: -1.39 therefore we accept the Null Hypothesis. So, the boys are not underfed.

• Significance Value \Rightarrow

P value

$\alpha = 0.05$



$0.08226 + 0.08226 = 0.1645$

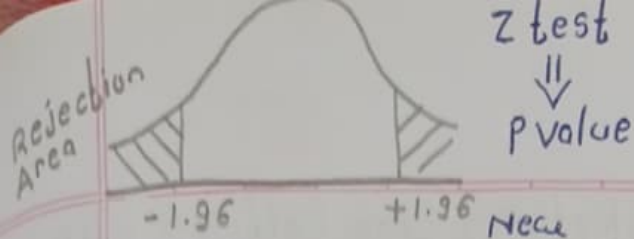
$0.1645 > 0.05$



significance value

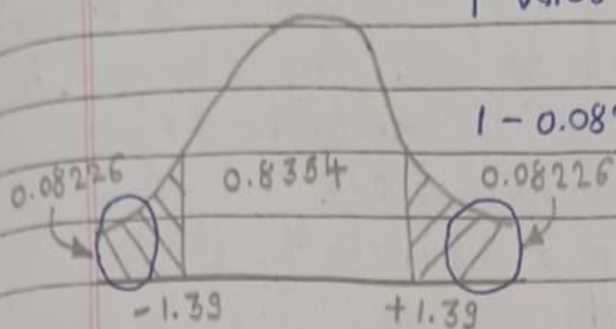
$1 - 0.91774 = 0.08226$

$p > 0.05 \rightarrow$ Accept the Null Hypothesis



$$P \text{ Value} = 0.08226 + 0.08226 = 0.16$$

$$1 - 0.08226 - 0.08226$$



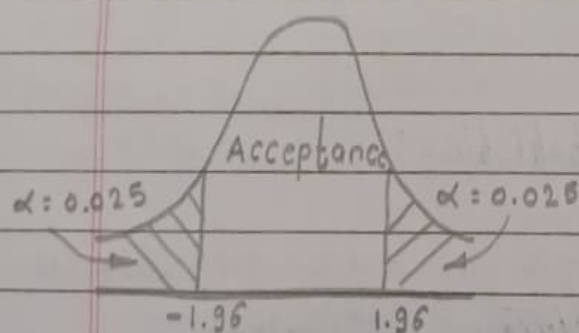
$$0.1645 > \text{Significant Value}$$

Accept the Null Hypothesis is.

- 4) The average weight of all residents in town xyz is 168 Lbs. A nutritionist believes the true mean to be different. She measured the weight of 36 individuals and found the mean to be 169.5 Lbs with a standard deviation of 3.9

Q) At 95% CI is there enough evidence to discard the Null Hypothesis?

Ans $H_0: \mu = 168$ $n = 36$ $\bar{x} = 169.5$ $S = 3.9$
 $H_1: \mu \neq 168$ $C = 0.95$ $\alpha = 1 - C.I. = 0.05$
 Z-test, t-test



$$Z = \frac{\bar{x} - \mu}{S/\sqrt{n}} = 2.31$$

$2.31 > 1.96$; Reject the Null Hypothesis

5) A Company manufactures bike batteries with an average life span of 2 or more years. An Engineer believes this value to be less. Using 10 samples, he measures the average life span to be 1.8 years. with a standard deviation of 0.15.

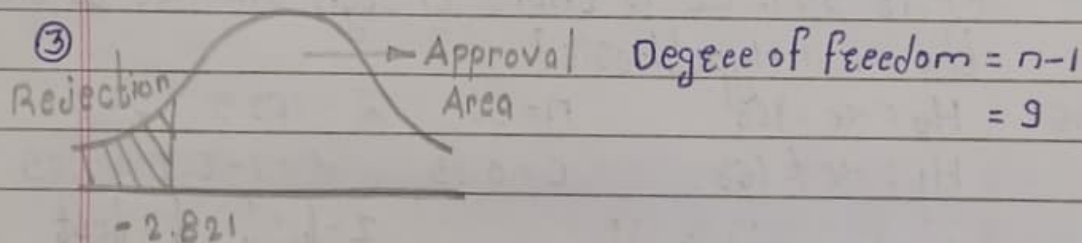
① State the Null and Alternate Hypothesis.

② At a 99% C.I, is there enough evidence to discard the H_0 ?

Ans

① $H_0: \mu \geq 2$, $n=10$, $\bar{x}=1.8$, $s=0.15$ {Sample std is given}
 $H_1: \mu < 2$ < 30
t-test

② $\alpha = 0.01$, $\alpha = 1 - C.I = 1 - 0.99 = 0.01$



④ Calculate t-test statistics:

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}} = \frac{1.8 - 2}{0.15/\sqrt{10}} = \frac{-0.2}{0.15/3.1622} = -4.216$$

⑤ Conclusion

$-4.216 < -2.821$; Reject the Null Hypothesis

⇓

Z test with Proportions

6) A test Company believes that the percentage of residents in town XYZ. That owns a cell phone is 70%. A marketing manager believes that this value to be different. He conducts a survey of 200 individuals and found that 130 responded yes to owning a cell phone.

① State Null and Alternate Hypothesis?

② At a 95% C.I, is there enough evidence to reject the Null Hypothesis?

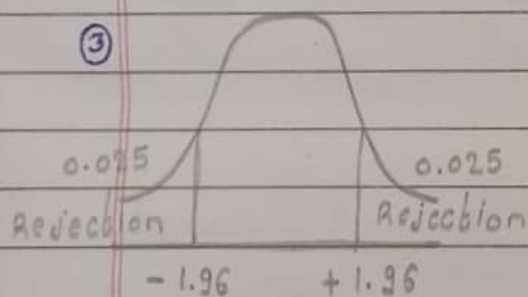
Ans ① $H_0: P_0 = 0.70$, $n = 200$, $x = 130$
 $H_1: P_0 \neq 0.70$

$$\hat{p} = \frac{x}{n} = \frac{130}{200} = \frac{13}{20} = 0.65$$

$$q_0 = 1 - P_0$$

② $\alpha = 0.05$, C.I = 95%

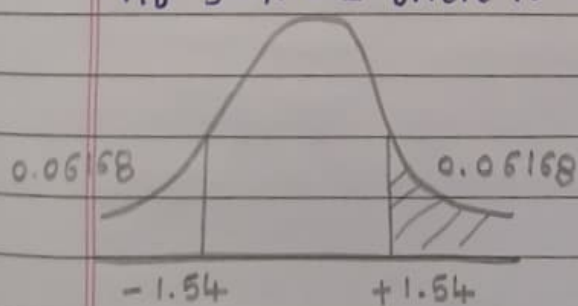
③



$$Z_{test} = \frac{\hat{p} - P_0}{\sqrt{\frac{P_0 q_0}{n}}}$$

$$= \frac{0.65 - 0.70}{\sqrt{\frac{0.7 \times 0.3}{200}}} \approx -1.54$$

At 95% C.I there is $-1.54 > -1.96$, So we accept the Null Hypothesis



P value

$$2 \times 0.06160 > 0.05$$

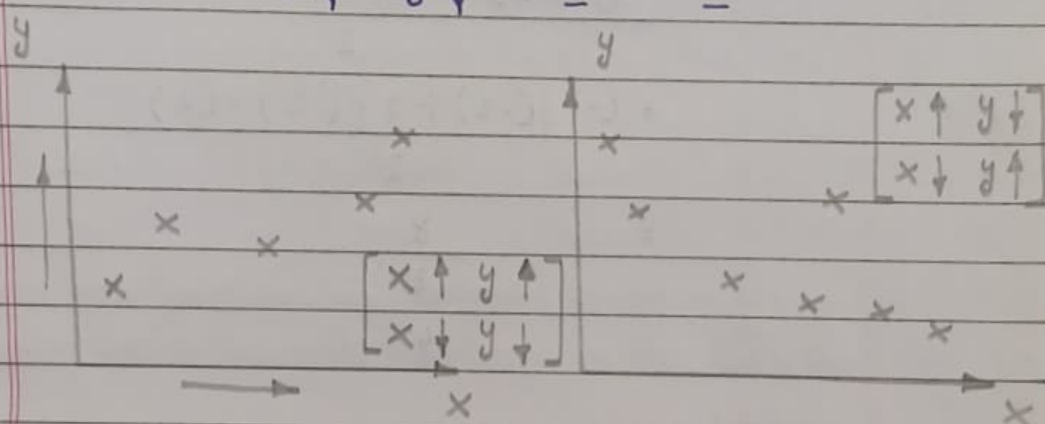
Accept Null Hypothesis

$$1 - 0.93872 = 0.06168$$

- ① Covariance
- ② Pearson Correlation Coefficient
- ③ Spearman Rank Correlation Coefficient
- ④ CHI SQUARE TEST
- ⑤ ANNOVA (F-Test)

① • Covariance

$x \uparrow$	$y \uparrow$	x	y	[Quantity the relationship between x & y]
$x \uparrow$	$y \downarrow$	-	-	
$x \downarrow$	$y \uparrow$	-	-	
$x \downarrow$	$y \downarrow$	-	-	



$$\text{Cov}_{x,y} = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{N-1} \quad \text{Var}(x) = \frac{\sum (x_i - \bar{x})^2}{N-1}$$

$$\text{Cov}(x, x) = \frac{\sum (x_i - \bar{x})^2}{N-1}$$

$$= \frac{\sum (x_i - \bar{x}) \times (x_i - \bar{x})}{N-1}$$

$$\text{Var}(x) = \sum_{i=1}^n \frac{(x - \bar{x})^2}{n-1} \Rightarrow \sum_{i=1}^n \frac{(x - \bar{x}) \times (x - \bar{x})}{n-1}$$

$$\text{Cov}(x, x) = \sum_{i=1}^n \frac{(x - \bar{x}) \times (x - \bar{x})}{n-1}$$

$x \uparrow y \uparrow$ Positively
 $x \downarrow y \downarrow$ Correlation

x	y
2	3
4	5
6	7

$$\bar{x} = 4, \bar{y} = 5$$

$$\text{Cov}(x, y) = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{n-1}$$

$$= \frac{(2-4)(3-5) + (4-4)(5-5) + (6-4)(7-5)}{2}$$

$$= \frac{(-2)(-2) + 0 + (2)(2)}{2}$$

$$= \frac{8}{2}$$

$$= 4$$

$x \uparrow y \downarrow \Rightarrow -ve \text{ Correlation} \Rightarrow -ve \text{ value}$

$x \downarrow y \uparrow$

$$\left. \begin{aligned} \text{Cov}(x, y) &= 500 \\ \text{Cov}(y, z) &= 600 \end{aligned} \right\}$$

Disadvantage Covariance

$\text{Cov}(x, y) \Rightarrow \text{the value}$ } $\Rightarrow \text{Limit } -350$
 $\text{or } -ve \text{ value}$ } $+500 -300$

\Downarrow

$$-400 + 1000$$

Relationship $[-1 \text{ to } 1]$

② • Pearson Correlation Coefficient

$[-1 \text{ to } 1]$

$x, y = \frac{\text{Cov}(x, y)}{\sigma_x \sigma_y}$ The more the value towards 1 more +ve it is correlated

Dataset :- 1000 features

x y z A B C

Independent Features

O/P dependent

features

$x, y \Rightarrow 99\%$

③ • Spearman Rank Correlation

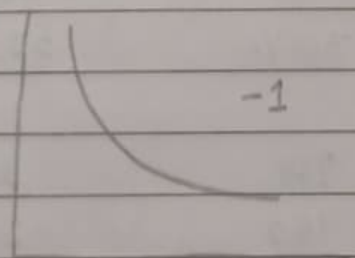
90% 0.9

-ve Correlation keep it

$$r_s = \frac{\text{Cov}(R(x), R(y))}{\sigma_{R(x)} \sigma_{R(y)}}$$

x	y	R _x	R _y
1	2	4	4
3	4	3	3
7	5	2	2
0	7	5	1
8	1	1	5

Spearman
Rank Corr = 1



④ • CHI Square

The Chi Square test claims about population proportions.

It is a non parametric test that is performed on Categorical (Nominal or ordinal) data.

- 1) • In the 2000 U.S Census, the ages of individuals in a small town were found to be the following.

< 18	18-35	> 35
20 %	30 %	50 %

In 2010, ages of $n=500$ individuals were sampled. Below are the results

< 18	18-35	> 35
121	288	91

using $\alpha = 0.05$, would you conclude the population distribution of ages has changed in the last 10 years?

Ans	< 18	18-35	> 35
Expected	20 %	30 %	50 %

$n=500$

95 C.I

Observed	121	288	91
Expected	100	150	250

- ① H_0 = the data meets the expected distribution
 H_1 = the data do not meet the expected dis

- ② Stats Alpha :- $\alpha = 0.05$

- ③ Calculate the degree of freedom

$$df = n - 1 = 3 - 1 = 2 \Rightarrow 3 \text{ Categories}$$

④ Decision Chi Square Test

If χ^2 is greater 5.99 than, Reject H_0

⑤ Calculate Chi Square test

$$\chi^2 = \sum \frac{(f_o - f_e)^2}{f_e} = \frac{(121-100)^2}{100} + \frac{(288-150)^2}{150} + \frac{(91-250)^2}{250}$$

$$\chi^2 = 232.494$$

$232.494 > 5.991$, Reject the Null Hypothesis.

2) A school Principal would like to know which days of the week students are most likely to be absent. The principal expect the students will be absent equally during the 5-day school week. The principal selects the random sample of 100 teachers asking them which day of the week they had the highest number of students absents, occurs with equal frequencies (use 95 C.I)

	Monday	Tuesday	Wed	Thue	Fri
Observed	23	16	14	19	28
Expected	20	20	20	20	20

- ① ANOVA (F-Test)
- ② EDA - (Solve some Example)

ANOVA :- Analysis of Variance

ANOVA is a statistical method used to compare the means of 2 or more group.

ANOVA :-

- | | | |
|--------------------------------------|----------------------|------------------|
| ① Factors
(Variables)
Medicine | ② Levels
[Dosage] | Anxiety reducing |
|--------------------------------------|----------------------|------------------|

	0 mg	50 mg	100 mg
Factor :- Dosage	9	7	4
Levels :- 0 mg, 50 mg, 100 mg	8	6	3
	7	6	2
	8	7	3
	8	8	

• Types of ANOVA

- ① One way ANOVA :- One factor with atleast 2 levels, levels are independent.
- ② Repeated Measures ANOVA :- One factor with atleast 2 levels, but levels are dependent.

Factor	Running Km's		
Levels	Day 1	Day 2	Day 3
	6	18	5

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- Factorial ANOVA:-

Two or more factor each of which with atleast 2 levels, levels can be either independent, dependent, or both (mixed)

	Day 1	Day 2	Day 3
Mean	9	7	4
	8	6	3
	7	5	2
Women	8	7	3
	8	8	4
	9	7	3

One way ANOVA (F-test) \Rightarrow Inferential Stats



Comparing means of 2 or more groups.

- Researchers want to test a new anxiety medication. They split participants into 3 Conditions (0mg, 50mg, 100mg), then ask them to rate their anxiety level on scale of 1-10. Are there any difference between the 3 Conditions using $\alpha = 0.05$

0mg	50mg	100mg
9	7	4
8	6	3
7	6	2
8	7	3
8	8	4
9	7	3
8	6	2

① $H_0 = \mu_{\text{mg}} = 450 \text{ mg} = 4100 \text{ mg}$
 $H_1 = \text{not all } \mu\text{'s are equal}$

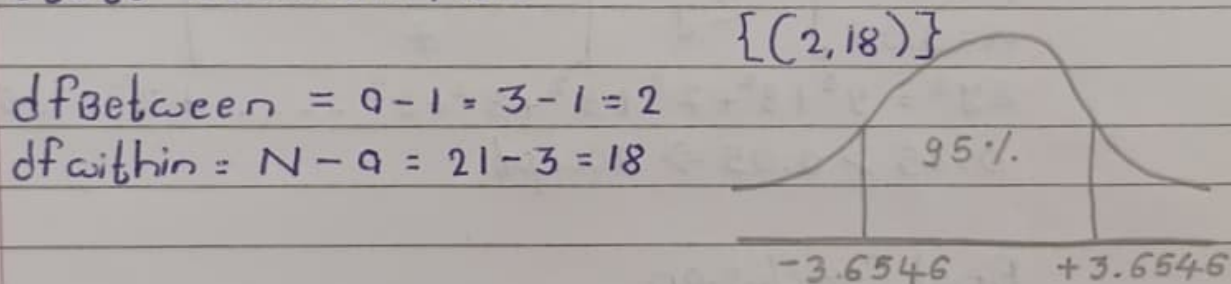
② state α and C.I.
 $\alpha = 0.05$; C.I = 95%.

③ Calculate degree of freedom

$N = 21$ $n = 7$
 $q = 3 \rightarrow (\text{No. of levels})$

$$\left(\begin{array}{l} df_{\text{Between}} = q - 1 = 3 - 1 = 2 \\ df_{\text{within}} = N - q = 21 - 3 = 18 \\ df_{\text{Total}} = N - 1 = 21 - 1 = 20 \end{array} \right)$$

④ State Decision Rule



If F test is greater than 3.5546, Reject the Null Hypothesis.

If F test is less than -3.5546 - " -

⑤ Calculate F Test statistics

$$F_{\text{Test}} = \frac{MS_{\text{between}}}{MS_{\text{within}}} = \frac{49.34}{0.57}$$

	SS	df	MS	F _{test}
Bet ⁿ	98.67	2	49.34	86.56
within	10.29	18	0.57	
Total	108.96	20		

$$SS_{\text{between}} = \frac{\sum (\sum q_i)^2}{n} - \frac{T^2}{N}$$

$$\begin{aligned} \sum (\sum q_i)^2 &= (9+8+7+8+8+9+8)^2 + (7+6+6+7+8+7+6)^2 + (4+3+2+3+4+3+2)^2 \\ &= 57^2 + 47^2 + 21^2 \end{aligned}$$

$$1) SS_{\text{between}} = \frac{57^2 + 47^2 + 21^2}{7} = \frac{125^2}{21} = 98.67$$

$$2) SS_{\text{within}} = \sum y^2 - \frac{\sum (\sum q_i)^2}{n}$$

$$p_{0.75} \left. \begin{array}{l} \alpha = 0.05 \end{array} \right\} = \sum y^2 - \left[\frac{57^2 + 47^2 + 21^2}{7} \right] = 10.29$$

$$\sum y^2 = 9^2 + 8^2 + 7^2 + 8^2 + 8^2 + 9^2 + \dots + 2^2 = 853$$

$$0.75 > 0.05 \Rightarrow \text{Accept}$$

Final Conclusion

86.56 > 35.546 ; So we reject the Null Hypothesis

$H_0 = \mu = \text{some value}$ } $\rightarrow 95\% \text{ C.I}$
 $H_1 = \mu \neq \text{some value}$ }

$H_0 = \mu_{\text{virg}} = \mu_{\text{setosa}} = \mu_{\dots}$

H_1	Pvalue	Reject the Null Hypothesis
0.0118	0.0228 < 0.05	
0.0118	1 - 0.025 = 0.975	
0.0228		