

Control Systems

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Abstract—This manual is an introduction to control systems based on GATE problems. Links to sample Python codes are available in the text.

Download python codes using

svn co <https://github.com/gadepall/school/trunk/control/codes>

1 TYPES OF DAMPING

1.1. Match the transfer functions of the second-order systems with the nature of the systems given below

<u>Transfer functions</u>	<u>Systems</u>
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P : $\frac{15}{s^2+5s+15}$	1: Overdamped
Q : $\frac{25}{s^2+10s+25}$	2: critically damped
R : $\frac{35}{s^2+18s+35}$	3 : Underdamped

$$(A) P - 1, Q - 2, R - 3 \quad (1.1.1)$$

$$(B) P - 2, Q - 1, R - 3 \quad (1.1.2)$$

$$(C) P - 3, Q - 2, R - 1 \quad (1.1.3)$$

$$(D) P - 3, Q - 1, R - 2 \quad (1.1.4)$$

Solution: The standard transfer function is $H(s) = \frac{\omega^2}{s^2 + 2\zeta\omega s + \omega^2}$ where "ω" is natural frequency and "ζ" is damping factor

then compare the given functions with this we get

1. For Transfer function $H(s) = \frac{15}{s^2+5s+15}$,

$$\omega^2 = 15$$

$$2\zeta\omega = 5$$

then we get $\zeta = \sqrt{\frac{5}{12}} < 1$ ref

2. For Transfer function $H(s) = \frac{25}{s^2+10s+25}$,

$$\omega^2 = 25$$

$$2\zeta\omega = 10$$

then we get $\zeta = \sqrt{\frac{5}{5}} = 1$ ref

3. For Transfer function $H(s) = \frac{35}{s^2+18s+35}$,

$$\omega^2 = 35$$

$$2\zeta\omega = 18$$

then we get $\zeta = \sqrt{\frac{81}{35}} > 1$ ref

The damping of a system can be described as being one of the following:

Overdamped : The system returns to equilibrium without oscillating. For this

$$\zeta > 1. \quad (1.1.5)$$

Critically damped: The system returns to equilibrium as quickly as possible without oscillating. For this

$$\zeta = 1 \quad (1.1.6)$$

Underdamped: The system oscillates (at reduced frequency compared to the undamped case) with the amplitude gradually decreasing to zero. For this

$$0 < \zeta < 1 \quad (1.1.7)$$

Undamped : The system oscillates at its natural

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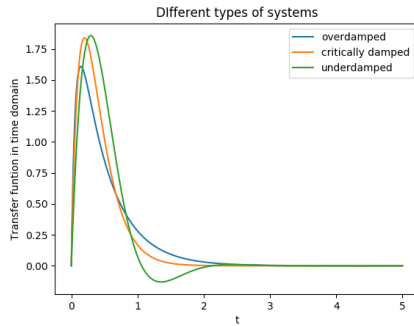


Fig. 1.1: Different systems based on ζ

resonant frequency(ω_0).

For this

$$\zeta = 0 \quad (1.1.8)$$

Final Analysis

- As for P : $\zeta < 1$
It is Underdamped system
- As for Q : $\zeta = 1$
It is critically damped system.
- As for R : $\zeta > 1$
It is an overdamped system.

So, P-3, Q-2, R-1. Option (C) is correct.