Machine learning network-constrained regression of epigenetic data

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Declaration

I Sivo V. Daskalov of Corpus Christi College, being a candidate for the M.Phil in Advanced Computer Science, hereby declare that this report and the work described in it are my own work, unaided except as may be specified below, and that the report does not contain material that has already been used to any substantial extent for a comparable purpose.

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Abstract

Computational biology often involves working with high-dimensional data. Penalized regression methods are often used on such data, as they can effectively perform feature selection. Several approaches for network-constrained regression have been suggested in literature over the recent years. They use prior knowledge in the form of a network to exploit known relationships between predictors. Synthetic datasets have been generated to do parameter tuning for the various implemented methods.

We suggest an approach for cooperative parameter tuning in the context of multiple alternative methods that share common input and goals. The aim is to tune the different regression methods iteratively, in a way that increases agreement between their coefficients. Neighboring values on the tuning parameter grid are considered for each method and iteration, selecting the set of values that achieves largest correlation with the averaged coefficients of all other methods for the previous iteration. Given enough iterations and granularity of the tuning grids, this process converges.

We also implement a simple approach to aggregate the coefficients produced by the various regression methods. Each predictor is considered relevant if it corresponds to a non-zero coefficient in a certain fraction of the underlying methods. Once a consensus has been reached through this form of voting, ordinary least squares estimation is used to fit only the relevant predictors to the data.

The common way of parameter tuning by minimization of the prediction mean squared error is implemented alongside our suggested approach. The comparison is discussed and a set of tuning parameters is assembled for use on real data. Gene methylation and expression data has been processed with the implemented algorithms. A map is created that shows methylation of which genes affects the expression levels of each gene.

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Chapter 1

Introduction

Epigenetics [1] studies the heritable traits that cannot be explained by changes in the DNA sequence. Examples of epigenetic mechanisms include DNA methylation and histone modification. These mechanisms adjust the expression level of genes [2], which allows organisms to dynamically adapt to changes in the environment.

Disruption of gene expression levels is related to the development of various diseases [3]. For example, the epigenetic deactivation of certain tumor suppressor genes commonly leads to the development of cancer [4]. The expression levels of certain genes can therefore be used as additional tools in early diagnostics of cancer, as prognosis factors and as predictors of response to treatment.

Good understanding of the relationship between DNA methylation and gene expression is important for both cancer prevention and epigenetic disease treatment. We have used the gene methylation and expression level data discussed in [5] to explore this relationship. One of the goals in this project is to produce a map that shows the methylation of which genes affects the expression levels of each gene.

Several methods [6, 7, 8, 9, 10, 11, 12] have been implemented and considered for use with real data. The hyperparameters for each method have been

tuned with the use of synthetic datasets as suggested in [8]. This is done because ground truth remains unknown for the relationship between gene methylation and expression.

A novel method of hyperparameter tuning is developed as an alternative to the widely used method of minimizing the cross-validated mean squared test error. In our context we have a bundle of regression methods that operate on the same training data and share a common goal - to correctly identify the relationship between predictor and target variables. Instead of tuning the various regression methods independently, our approach performs cooperative hyperparameter tuning on all methods simultaneously. It uses an iterative algorithm to increase the similarity of estimated coefficients for the various methods by tuning their hyperparameters. For each method and iteration, the method's parameter grid neighborhood is searched for a set of parameters that maximizes the correlation between its estimated coefficients and the averaged estimates of all other methods for the previous iteration. When this process converges a set of parameters is defined for each method that maximizes the overall agreement across the whole set of methods.

The various regression methods discussed in this project minimize different cost functions. As a result, each method exhibits specific strengths and weaknesses. The relative performance of the methods depends on the dataset used. For this reason it is impossible to predict their effectiveness on an arbitrary real data set with no access to ground truth. We have developed a simple way to merge the estimation results of the method bundle. It is designed to balance the behavior of any individual method. Each of the predictor variables is considered important if it has non-zero coefficients in a fraction of the methods above a given threshold. This approach for variable selection in practice implements a voting system where each predictor must achieve a certain electoral threshold to be selected. Ordinary least squares estimation is then performed only using the set of selected variables.

The following chapter discusses the details of each linear regression approach. After introducing the synthetic dataset generation process, we define our parameter tuning method and compare the results with those from the standard

approach. Next we present the real dataset used for exploration of the relationship between gene methylation and expression. After introducing of our result merging approach we present and discuss the results.

Chapter 2

Background and Related Work

Some introduction of the chapter

2.1 Linear Regression

$$y_i = \beta_0 1 + \beta_1 x_{i1} + \beta_2 x_{i2} + ... + \beta_p x_{ip} \tag{2.1}$$

$$Y_i = \beta_0 + \beta_1 X_i + \epsilon_i \tag{2.2}$$

2.2 Ordinary Least Squares Estimation

Sum of squared residuals; objective function

$$S(\beta) = \sum_{i=1}^{N} (y_i - x_i^T \beta)^2 \tag{2.3}$$

2.3 Lasso

least absolute shrinkage and selection operator lambda 1 is alpha because sklearn said so

$$S(\beta) = \sum_{i=1}^{n}(y_i - x_i^T\beta)^2 + \lambda_1 \sum_{i=1}^{p}|\beta_i| \tag{2.4}$$

$alpha = \lambda_1$

2.4 Elastic Net

$$S(\beta) = \sum_{i=1}^{n}(y_i - x_i^T\beta)^2 + \lambda_1 \sum_{i=1}^{p}|\beta_i| + \lambda_2\sqrt{\sum_{i=1}^{p}\beta_i^2} \tag{2.5}$$

$alpha = \lambda_1 + \lambda_2$ and $l1\_ratio = \lambda_1/(\lambda_1 + \lambda_2)$

2.5 Grace

2.6 aGrace

2.7 GBLasso

2.8 Linf and aLinf

2.9 TTLP and LTLP

A more extensive coverage of what's required to understand your work. In general you should assume the reader has a good undergraduate degree in computer science, but is not necessarily an expert in the particular area you've been working on. Hence this chapter may need to summarize some "text book" material.

This is not something you'd normally require in an academic paper, and it may not be appropriate for your particular circumstances. Indeed, in some cases it's possible to cover all of the "background" material either in the introduction or at appropriate places in the rest of the dissertation.

This chapter covers relevant (and typically, recent) research which you build upon (or improve upon). There are two complementary goals for this chapter:

1. to show that you know and understand the state of the art; and
2. to put your work in context

Ideally you can tackle both together by providing a critique of related work, and describing what is insufficient (and how you do better!)

The related work chapter should usually come either near the front or near the back of the dissertation. The advantage of the former is that you get to build the argument for why your work is important before presenting your solution(s) in later chapters; the advantage of the latter is that don't have to forward reference to your solution too much. The correct choice will depend on what you're writing up, and your own personal preference.

Chapter 3

Design and Implementation

This chapter may be called something else... but in general the idea is that you have one (or a few) "meat" chapters which describe the work you did in technical detail.

Chapter 4

Evaluation

For any practical projects, you should almost certainly have some kind of evaluation, and it's often useful to separate this out into its own chapter.

Chapter 5

Summary and Conclusions

As you might imagine: summarizes the dissertation, and draws any conclusions. Depending on the length of your work, and how well you write, you may not need a summary here.

You will generally want to draw some conclusions, and point to potential future work.

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