

# Modeling of systems and processes

# More on Git

- Microsoft's 30 mins [Introduction to Git](#)
- GitHub's hands-on training course (< 1 hour) [Introduction to GitHub](#)
- tl;dr:
  - `git status`
  - `git pull`
  - `git add .`
  - `git commit -m "<your message here>"`
  - `git push`

# Board Question

Deck of 52 cards

- 13 ranks: 2, 3, ..., 9, 10, J, Q, K, A
- 4 suits: ♥, ♠, ♦, ♣,

Poker hands

- Consists of 5 cards
- A one-pair hand consists of two cards having one rank and the remaining three cards having three other ranks
- Example:  $\{2♥, 2♠, 5♥, 8♣, K♦\}$

Question

- (a) How many different 5 card hands have exactly one pair?

Hint: practice with how many 2 card hands have exactly one pair. Hint for hint: use the rule of product.

- (b) What is the probability of getting a one pair poker hand?

# Probability Cast

## Introduced so far

- Experiment: a repeatable procedure
- Sample space: set of all possible outcomes  $S$  (or  $\Omega$ ). Event:
  - a subset of the sample space.
- Probability function,  $P(\omega)$ : gives the probability for each outcome  $\omega \in S$ 
  1. Probability is between 0 and 1
  2. Total probability of all possible outcomes is 1.

## Example

Experiment: toss a fair coin, report heads or tails.

Sample space:  $\Omega = \{ H, T \}$ .

Probability function:  $P(H) = .5$ ,  $P(T) = .5$ .

Use tables:

Outcomes	H	T
Probability	1/2	1/2

(Tables can really help in complicated examples)

## Discrete sample space

Discrete = listable

Examples:

$\{a, b, c, d\}$  (finite)

$\{0, 1, 2, \dots\}$  (infinite)

# Events

Events are sets:

- Can describe in words
- Can describe in notation
- Can describe with Venn diagrams

Experiment: toss a coin 3 times.

Event:

You get 2 or more heads = { HHH, HHT, HTH, THH }

CQ: Events, sets and words

Experiment: toss a coin 3 times.

Which of following equals the event “exactly two heads”?

$A = \{ THH, HTH, HHT, HHH \}$

$B = \{ THH, HTH, HHT \}$

$C = \{ HTH, THH \}$

(1) A

(2) B

(3) C

(4) A or B



## CQ: Events, sets and words

Experiment: toss a coin 3 times.

Which of the following describes the event  $\{THH, HTH, HHT\}$ ?

- (1) “exactly one head”
- (2) “exactly one tail”
- (3) “at most one tail”
- (4) none of the above

CQ: Events, sets and words

Experiment: toss a coin 3 times.

The events “exactly 2 heads” and “exactly 2 tails” are disjoint.

(1) True              (2) False

CQ: Events, sets and words

Experiment: toss a coin 3 times.

The event “at least 2 heads” implies the event “exactly two heads”.

(1) True                      (2) False

# Probability rules in mathematical notation

Sample space:  $S = \{ \omega_1, \omega_2, \dots, \omega_h \}$

Outcome:  $\omega \in S$

Probability between 0 and 1:

Total probability is 1:

Event A:  $P(A)$

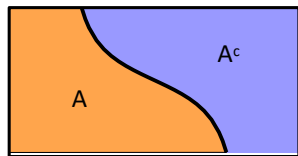
# Probability and set operations on events

Events  $A$ ,  $L$ ,  $R$

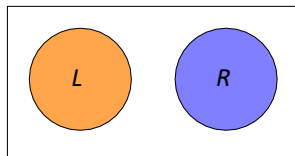
**Rule 1.** Complements:  $P(A^c) = 1 - P(A)$ .

**Rule 2.** Disjoint events: If  $L$  and  $R$  are disjoint then  
 $P(L \cup R) = P(L) + P(R)$ .

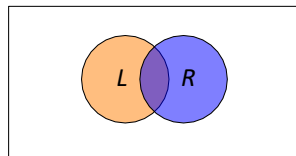
**Rule 3.** Inclusion-exclusion principle: For any  $L$  and  $R$ :  
 $P(L \cup R) = P(L) + P(R) - P(L \cap R)$ .



$\Omega = A \cup A^c$ , no overlap



$L \cup R$ , no overlap



$L \cup R$ , overlap =  $L \cap R$

# References

*Dr. Jeremy Orloff. Jonathan Bloom. Introduction to Probability and Statistics. Spring 2014.* Massachusetts Institute of Technology: MIT OpenCourseWare, <https://ocw.mit.edu/>. License: Creative Commons BY-NC-SA.