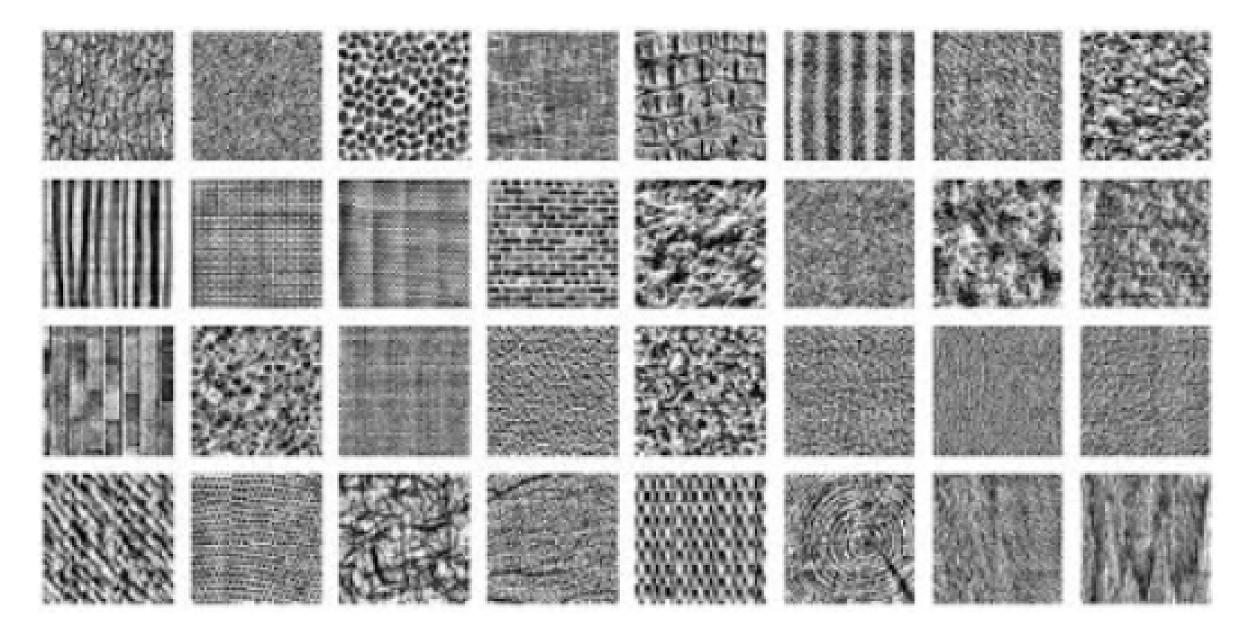
# Texture Analysis

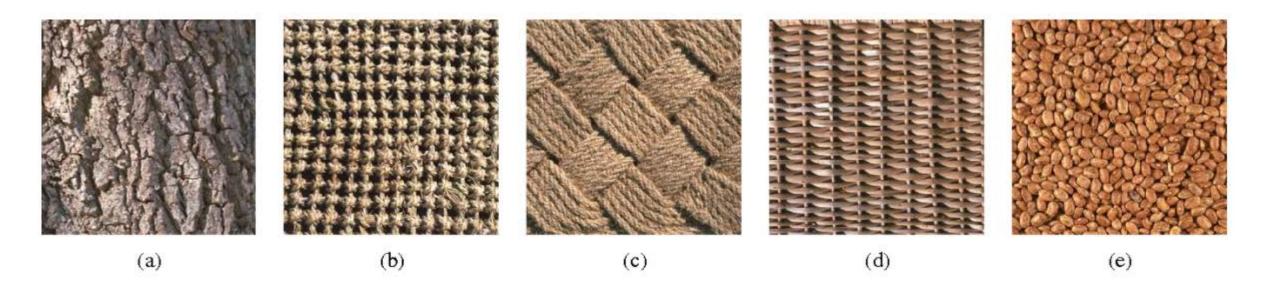
C.-C. Jay Kuo University of Southern California

#### Introduction

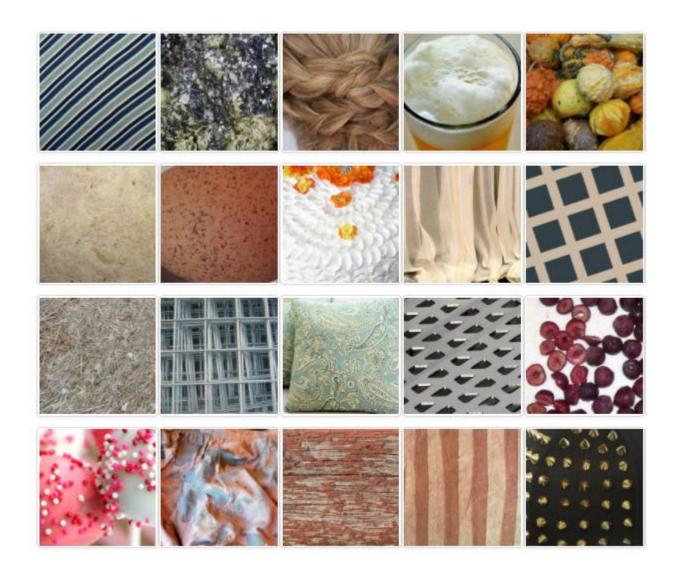
#### USC Brodatz Texture dataset



#### MIT Vision Texture Dataset



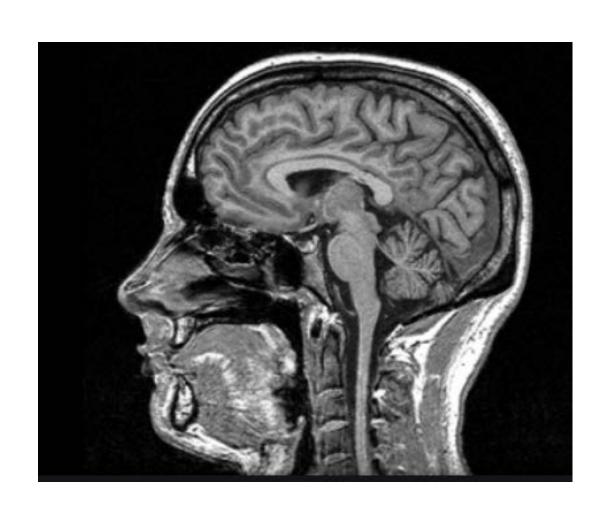
## Describable Textures Dataset (DTD)



#### Remote Sensing Images



# MRI Scanned Images





# Real World Images (1)



# Real World Images (2)



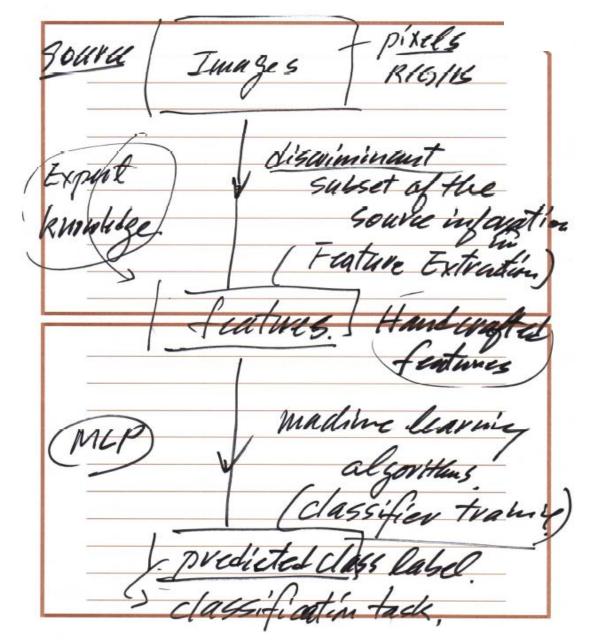
Texture Analysis

#### Texture Definition and Applications

#### Texture

- No formal mathematical definition
- Defined by examples
  - Regions or surfaces exhibit certain patterns, e.g., water, grass, wood, cloud, etc.
  - Most natural images consist of smooth regions, textured regions and edge regions
- Applications of Texture Analysis
  - Remote sensing image analysis (segmentation, classification, etc.)
  - Medical image analysis

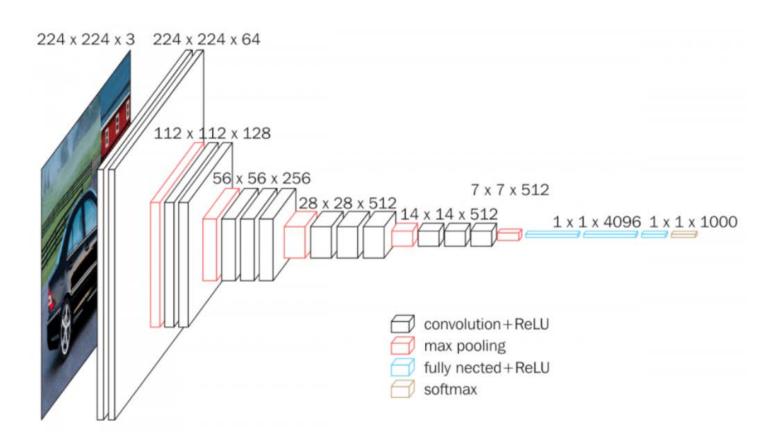
#### Image Analysis (a.k.a. Low-Level Computer Vision)



#### "End-to-End" or "Modularized" Design

- Recent Trend
  - The end-to-end optimized network design becomes popular since 2012
  - Deep learning

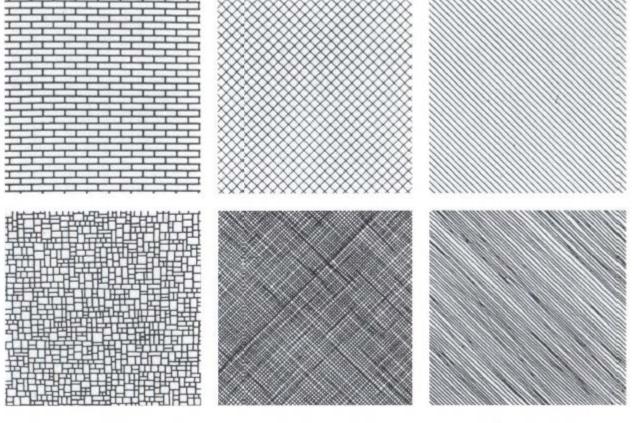
**VGG-16 Network** 



#### Challenges of Texture Analysis

 Quasi-periodic, 2D random field, dominated by high frequency components

Pratt's Book Page 546

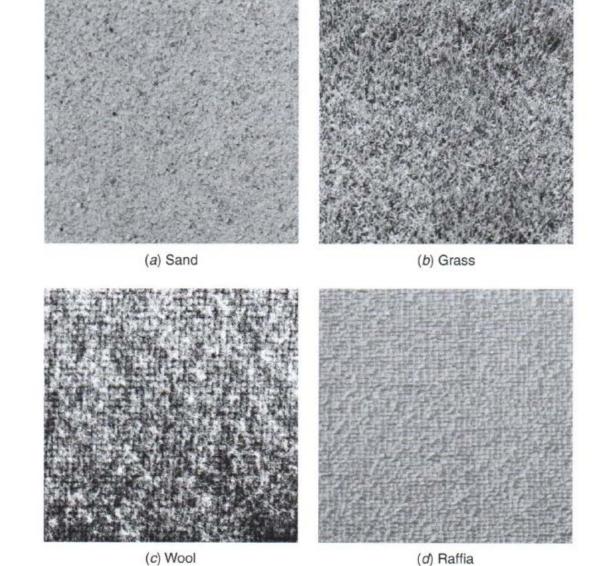


**Artificial Textures** 

## Brodatz Texture Examples

Pratt's Book

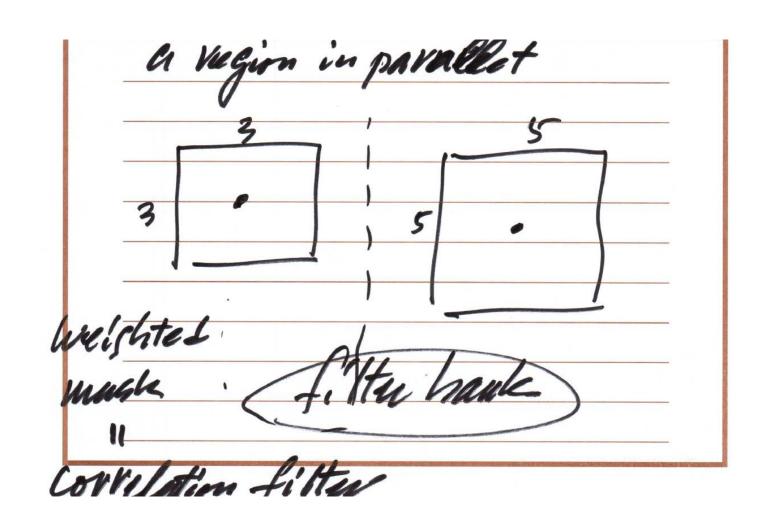
Page 547



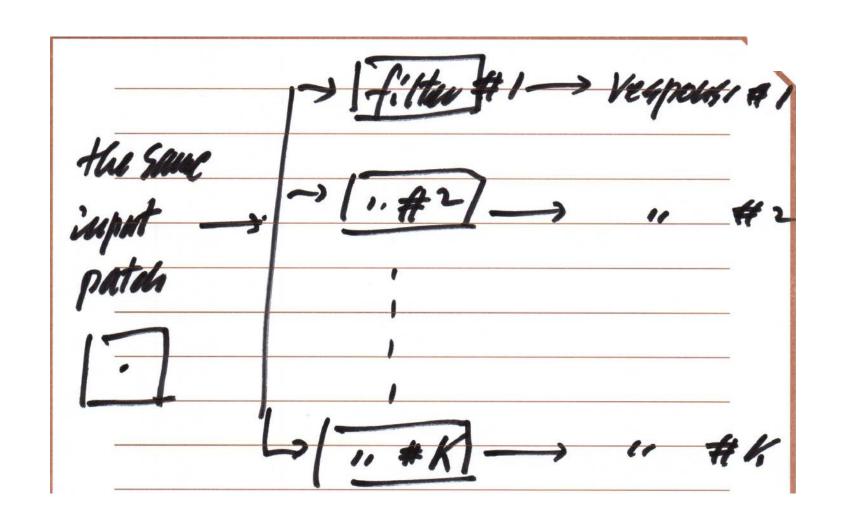
#### Texture Feature Extraction

Long history of texture feature extraction. - ad hoc. (in the textbook) Kennoth Laws. a set of fittens, applied to

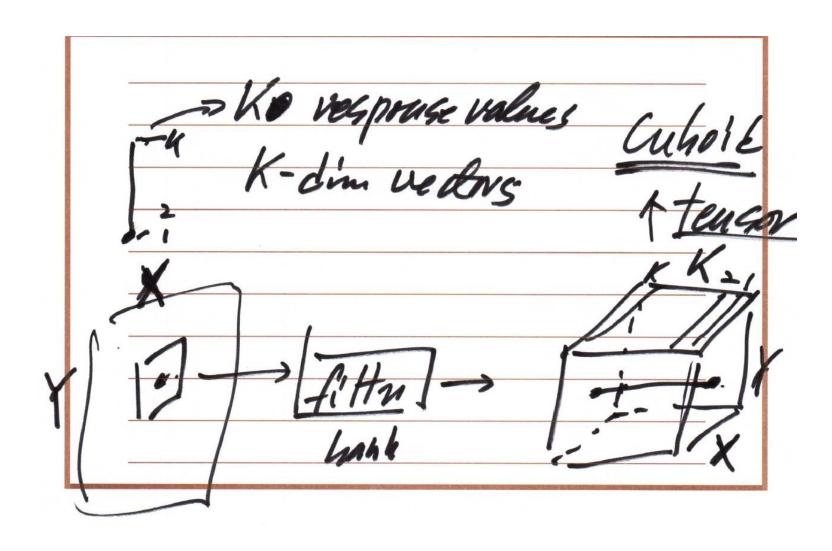
#### 3x3 and 5x5 Laws' Filters



#### Filter Banks



#### Filter Response Vector



## Laws' 3x3 Filters along x-Axis

**Horizontal Filters** 

Laws' filtus. 1980.	
3×3	
Three 1D flters	<del></del>
L3: Total averaging	10
E3: 1(-1,0,1)	tensor
53: \frac{1}{2} (-1, 2, -1)	

## Laws' Filters along y-Axis

**Vertical Filters** 

#### 2D Laws' Filters (3x3 Filter Masks)

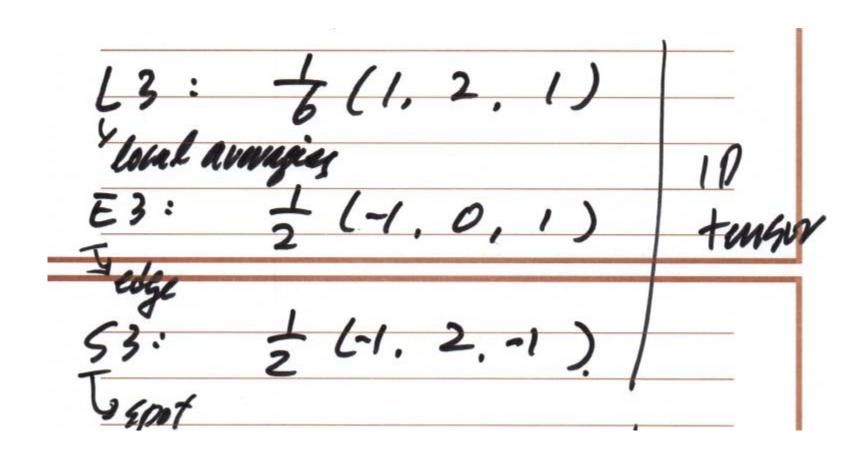
2D tensor tensor product

$$\frac{1}{2}(-1, 0, 1) \otimes \frac{1}{2} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$= \frac{1}{2} \begin{pmatrix} -1 \\ -2 \\ 0 \end{pmatrix}, \frac{2}{1} \end{pmatrix}$$

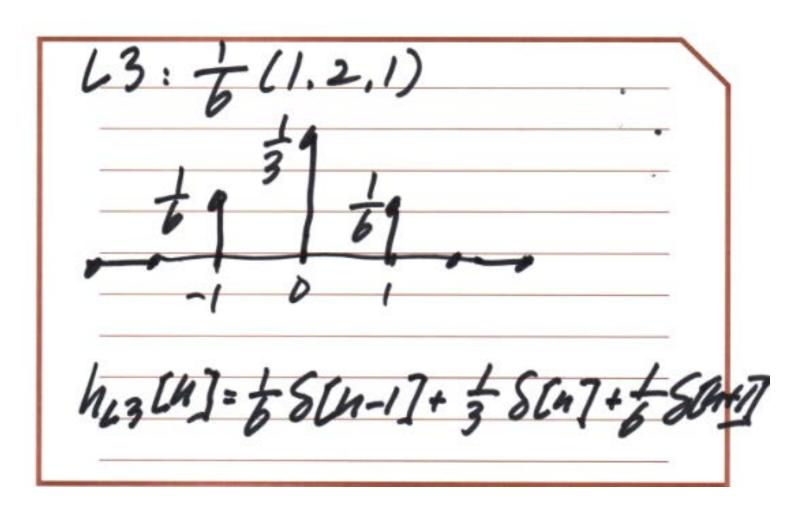
$$= \frac{1}{2} \begin{pmatrix} -2 \\ 7 \end{pmatrix}, \frac{2}{1} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

## Understanding Laws' Filters (A DSP Approach)

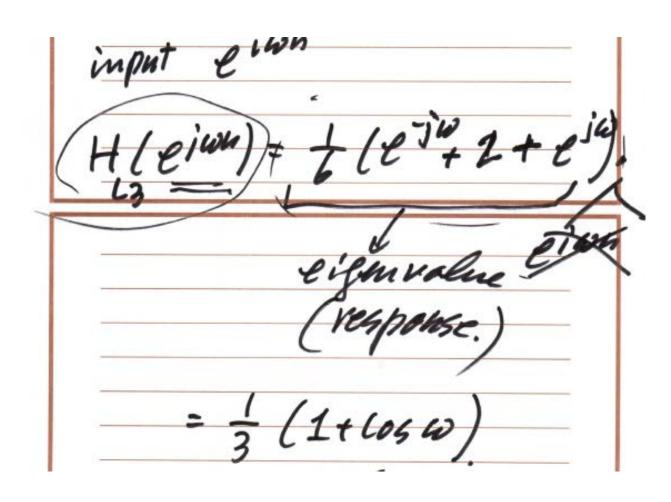


## Analysis of Filter L3

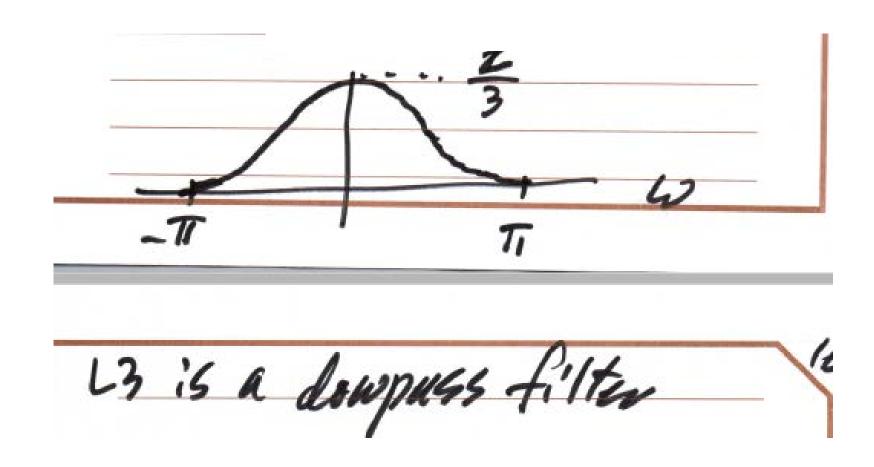
• Impulse response



## Frequency Response of Filter L3 (1)

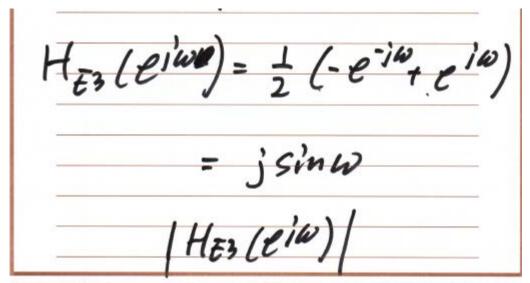


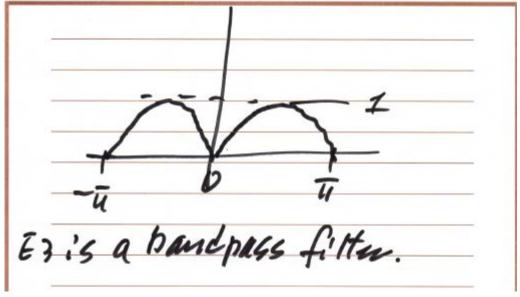
#### Frequency Response of Filter L3 (2)



## Analysis of Filter E3

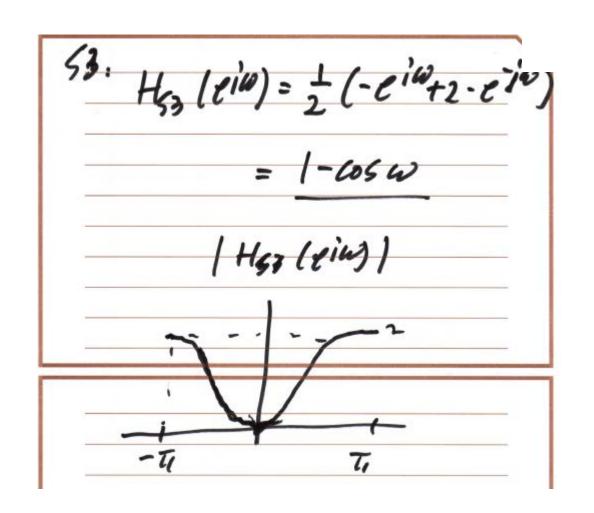
- E3: 0.5 x ( -1, 0, 1)
- Frequency Response
  - E3 is a bandpass filter



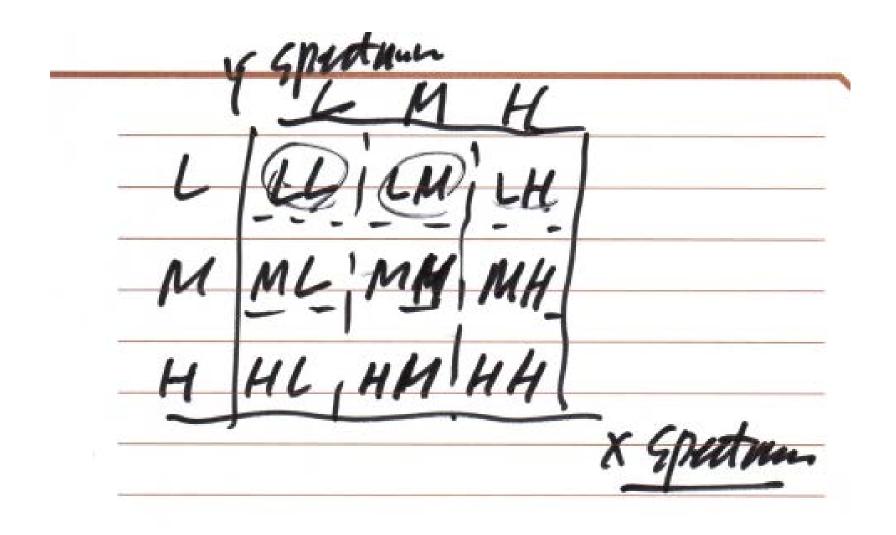


## Analysis of Filter S3

- S3: 0.5 x (-1, 2, -1)
- Frequency Response
  - S3 is a highpass filter



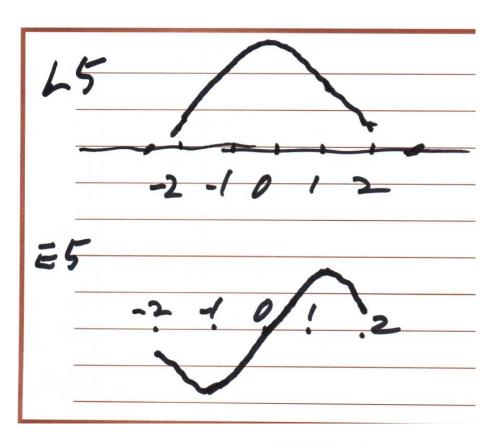
#### Responses of 2D Filters in A 3x3 Patch

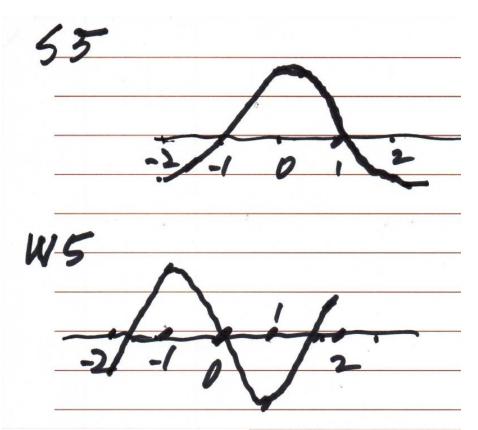


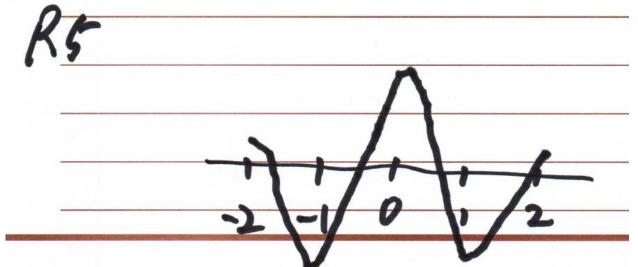
#### Laws' 5x5 Filters

**Table 1:** 1D Kernel for 5x5 Laws Filters

Name	Kernel
L5 (Level)	[1 4 6 4 1]
E5 (Edge)	[-1 -2 0 2 1]
S5 (Spot)	[-1 0 2 0 -1]
W5 (Wave)	[-1 2 0 -2 1]
R5 (Ripple)	[1 -4 6 -4 1]



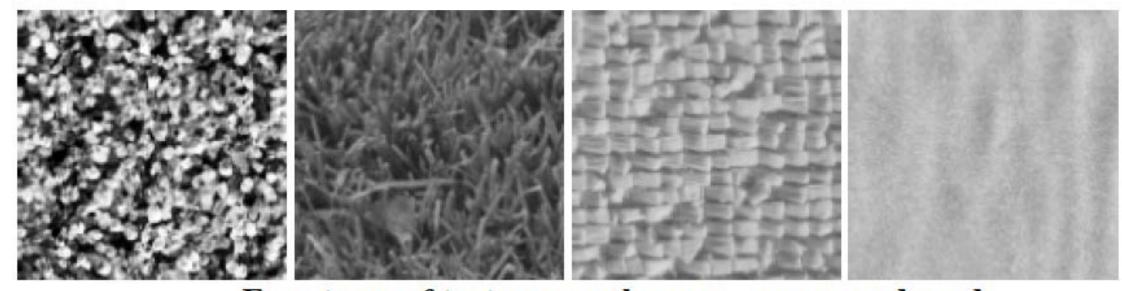




#### Exercise:

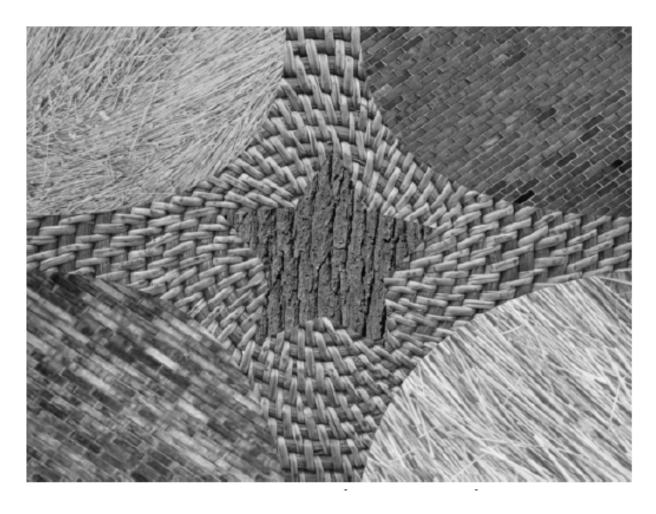
# Conduct Frequency Responses on These Five Filters

#### Texture Classification Problem



Four types of textures: rock, grass, weave, and sand

## Texture Segmentation Problem



**Texture Mosaic** 

#### Pixelwise Response and Its 2<sup>nd</sup> Order Statistics

- Scan the entire texture image pixel by pixel (stride = 1) using a bank of filters (e.g. 3x3 Laws' filters)
  - 9 filters -> 9 responses -> a random vector of 9 dimensions -> response vector
- Find the second-order statistics of the response vector
  - Mean vector
    - The LL response has a non-zero mean
    - The remaining 8 responses have the same mean (zero mean)
  - Covariance matrix
    - Symmetric matrix
    - Diagonally dominant matrix
      - Weak correlation between different elements of the feature vector

#### Ordering of Laws' Filters

$$\frac{1}{36} \begin{bmatrix}
1 & 2 & 1 \\
2 & 4 & 2 \\
1 & 2 & 1
\end{bmatrix} \quad \frac{1}{12} \begin{bmatrix}
1 & 0 & -1 \\
2 & 0 & -2 \\
1 & 0 & -1
\end{bmatrix} \quad \frac{1}{12} \begin{bmatrix}
-1 & 2 & -1 \\
-2 & 4 & -2 \\
-1 & 2 & -1
\end{bmatrix}$$

$$Laws 1 \qquad Laws 2 \qquad Laws 3$$

$$\frac{1}{12} \begin{bmatrix}
-1 & -2 & -1 \\
0 & 0 & 0 \\
1 & 2 & 1
\end{bmatrix} \quad \frac{1}{4} \begin{bmatrix}
1 & 0 & -1 \\
0 & 0 & 0 \\
-1 & 0 & 1
\end{bmatrix} \quad \frac{1}{4} \begin{bmatrix}
-1 & 2 & -1 \\
0 & 0 & 0 \\
1 & -2 & 1
\end{bmatrix}$$

$$Laws 4 \qquad Laws 5 \qquad Laws 6$$

$$\frac{1}{12} \begin{bmatrix}
-1 & -2 & -1 \\
2 & 4 & 2 \\
-1 & -2 & -1
\end{bmatrix} \quad \frac{1}{4} \begin{bmatrix}
-1 & 0 & 1 \\
2 & 0 & -2 \\
-1 & 0 & 1
\end{bmatrix} \quad \frac{1}{4} \begin{bmatrix}
1 & -2 & 1 \\
-2 & 4 & -2 \\
1 & -2 & 1
\end{bmatrix}$$

$$\frac{1}{4} \begin{bmatrix}
-1 & -2 & 1 \\
-2 & 4 & -2 \\
1 & -2 & 1
\end{bmatrix}$$

$$\frac{1}{4} \begin{bmatrix}
-1 & -2 & 1 \\
-2 & 4 & -2 \\
1 & -2 & 1
\end{bmatrix}$$

$$\frac{1}{4} \begin{bmatrix}
-1 & -2 & 1 \\
-2 & 4 & -2 \\
1 & -2 & 1
\end{bmatrix}$$

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-1 & -2 & 1 \\
-2 & 4 & -2 \\
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-1 & -2 & 1
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-1 & -2 & 1 \\
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-1 & -2 & 1 \\
-1 & -2 & 1
\end{bmatrix}$$

$$\frac{1}{4} \begin{bmatrix}
-1 & -2 & 1 \\
-1 & -2 & 1
\end{bmatrix}$$

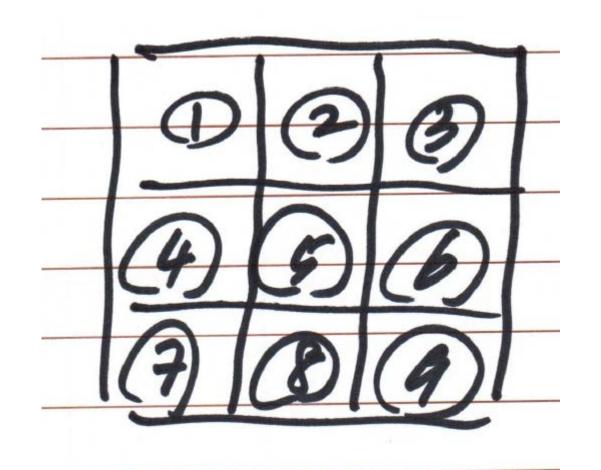
$$\frac{1}{4} \begin{bmatrix}
-1 & -2 & 1 \\
-1 & -2 & 1
\end{bmatrix}$$

$$\frac{1}{4} \begin{bmatrix}
-1 & -2 & 1 \\
-1 & -2 & 1
\end{bmatrix}$$

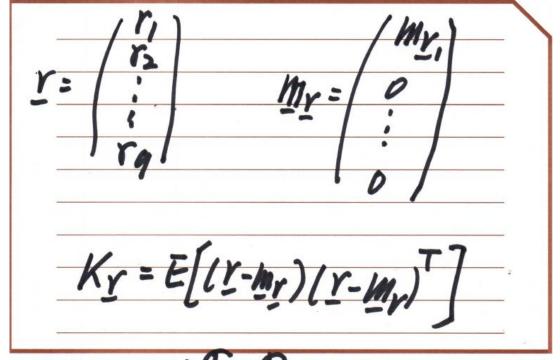
$$\frac{1}{4} \begin{bmatrix}
-1 & -2 & 1 \\
-1 & -2 & 1
\end{bmatrix}$$

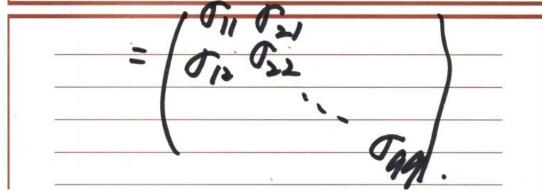
Laws 8

Laws 7



### 2<sup>nd</sup> Order Statistics of Response Vector

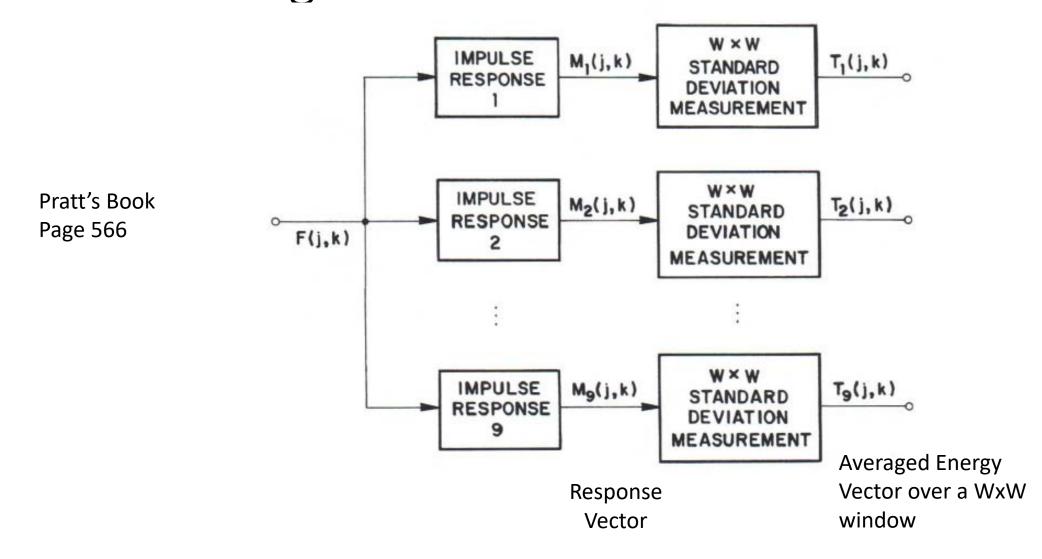




#### **Diagonal elements:**

- Intra-channel (self) correlationOff-diagonal elements
- Inter-channel correlation

## Laws' Filter Energy Feature Extraction Block-diagram

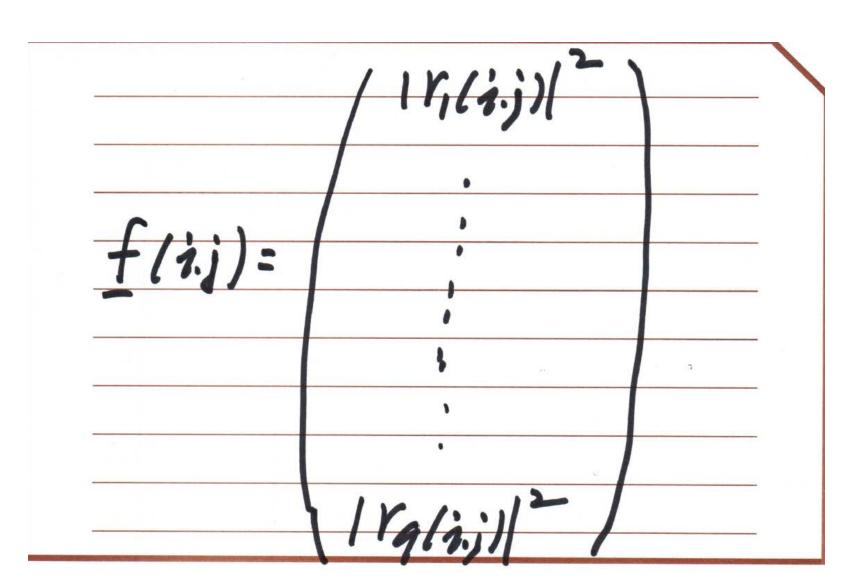


#### **Energy Feature Vector**

#### Why Averaging over WxW Window?

9-dimensional feature vector at pixel location (i,j)

Statistical Fluctuation



Digression: Basic Machine Learning

# Supervised versus Un-supervised Machine Learning

- Supervised ML
  - Training data with labels provided by humans
  - Heavily supervised ML
    - The # of training samples is much larger than the # of test samples
  - Weakly supervised ML
    - The # of training samples is much smaller than the # of test samples
- Un-supervised ML
  - No training data with human labels
- Examples
  - Sobel and Canny edge detectors are un-supervised methods
  - Structured edge detector is a supervised method

# Commonly Used Supervised Classifiers in Machine Learning

- Nearest Neighbor (NN) classifier
- k Nearest Neighbor (kNN) classifier
- Support vector machine (SVM)
- Random forest (RF)
- Multi-layer Perceptron (MLP)
- Adaptive Boosting (Adaboost)
- Gradient Boosting and Extremely Gradient Boosting (XGBoost)

#### Distance-Based Classifiers

- General principle
  - Compute the distance of the feature vector of a test image from each class' centroid and select the class that gives the minimum distance
- What kind of distance
  - Euclidean distance?
    - This is fine if the variance of each dimension is normalized to unity
    - Otherwise, we should consider Mahalanobis distance

Mahalanobis distance (or "generalized squared interpoint distance" for its squared value<sup>[3]</sup>) can also be defined as a dissimilarity measure between two random vectors  $\vec{x}$  and  $\vec{y}$  of the same distribution with the covariance matrix S:

$$d(ec x,ec y) = \sqrt{(ec x - ec y)^T S^{-1} (ec x - ec y)}.$$

#### Mahalanobis Distance

If the covariance matrix is the identity matrix, the Mahalanobis distance reduces to the Euclidean distance. If the covariance matrix is diagonal, then the resulting distance measure is called a *standardized Euclidean distance*:

$$d(ec{x},ec{y}) = \sqrt{\sum_{i=1}^N rac{(x_i-y_i)^2}{s_i^2}},$$

where  $s_i$  is the standard deviation of the  $x_i$  and  $y_i$  over the sample set.

## Unsupervised Classifier – K-means Clustering (1)

#### • Objective:

- Cluster N feature vectors of dimension D, denoted by R<sup>D</sup>, into K clusters to minimize the total distortion between each feature vector and its associated cluster centroid
- Initialization (m=0)
  - Select K feature vectors as the initial set of cluster centroids, called a codebook
- Generalized Lloyd Iteration (m=0,1,...)
  - Given codebook  $C_m = \{ y_i, i = 1, ..., K \}$  obtained from the  $m^{th}$  iteration, find a new optimal partitioning of space  $R^D$  using the nearest-neighbor condition to form the nearest-neighbor cells  $R_i = \{ x: d(x,y_i) < d(x,y_i), j \neq i \}$

## Unsupervised Classifier – K-means Clustering (1)

- Centroid update
  - Compute new centroids from new partition cells

$$Cm+1 = \{ centroid(R_i), i = 1, ..., K \}$$

$$centroid(\mathbf{R}_i) = \frac{1}{n_i} \sum_{j=1}^{n_i} \mathbf{x}_j$$

 $n_i$ : No. of vectors in  $R_i$ 

Continue this iterative optimization procedure until obtain an optimum codebook

#### Complexity Analysis of GLA

For one step of GLA, computational complexity is O(K\*D\*L)

K: codebook size

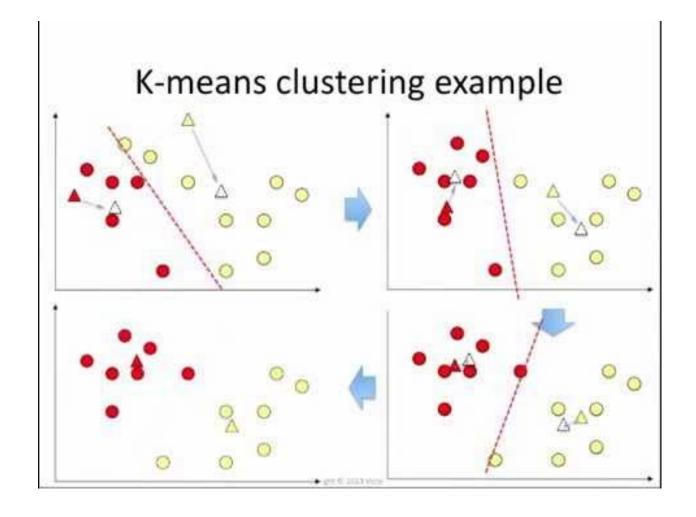
D: vector dimension

L: size of training vectors

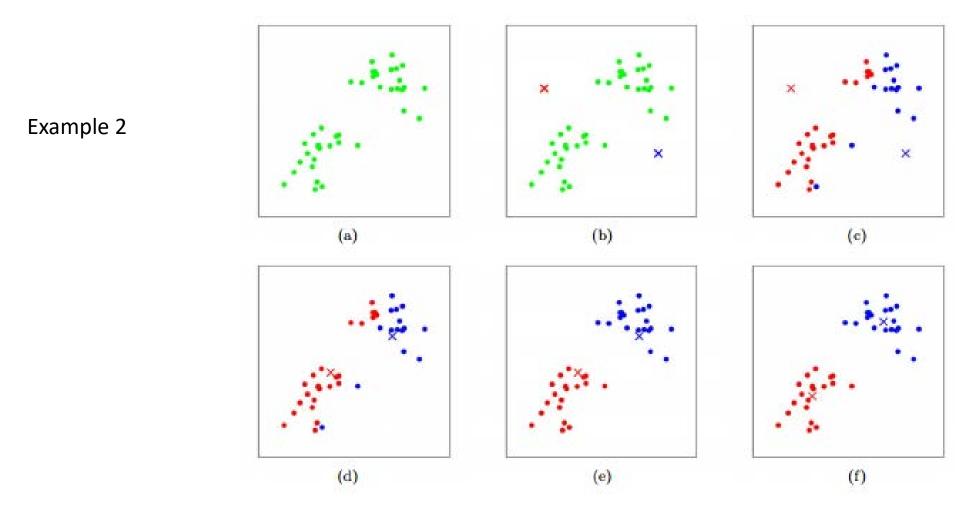
48

#### Graphic Illustration of K-means Clustering

Example 1

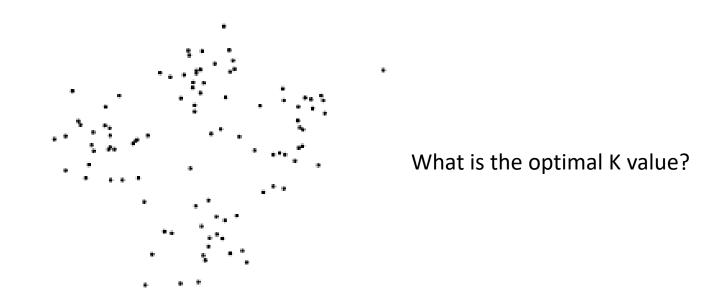


#### Graphic Illustration of K-means Clustering



#### Comments on K-means Clustering

- Non-convex optimization
  - There are multiple local minima
  - The converged solution is dependent on the initial centroid choice
- The choice of the optimal K value is a problem



### Application of K-means Clustering

General image segmentation is challenging!



#### Application of K-means Clustering

Application-specific image segmentation is more manageable



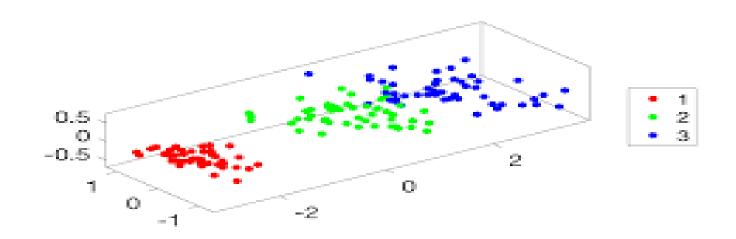
Semantic Segmentation



**Instance Segmentation** 

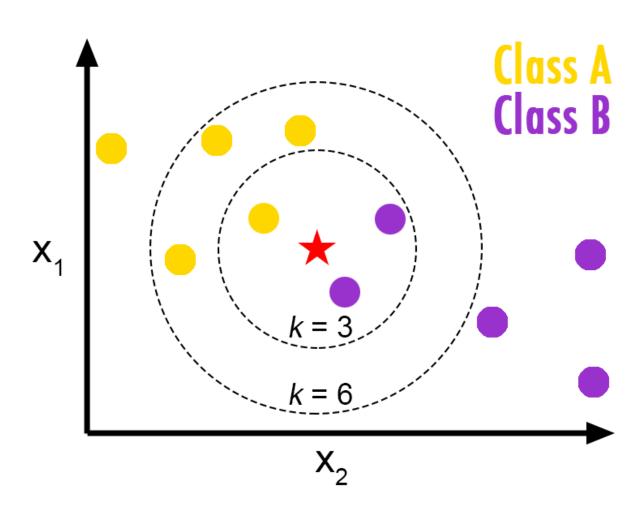
#### Supervised Distance-based Classifier (1)

- Nearest Neighbor Classifier
  - Intra-cluster variation is smaller than inter-cluster variation
  - Compute the centroid of each cluster
  - Choose the class that has the smallest test sample-to-centroid distance



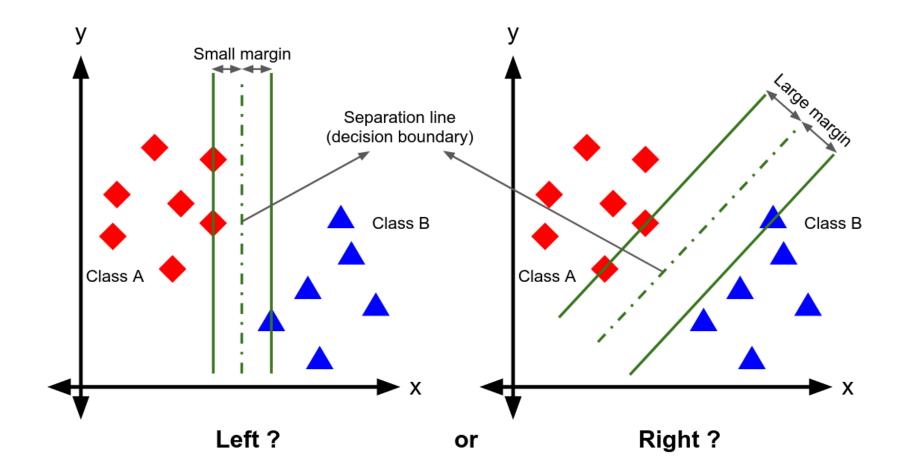
#### Supervised Distance-based Classifier (2)

KNN Classifier

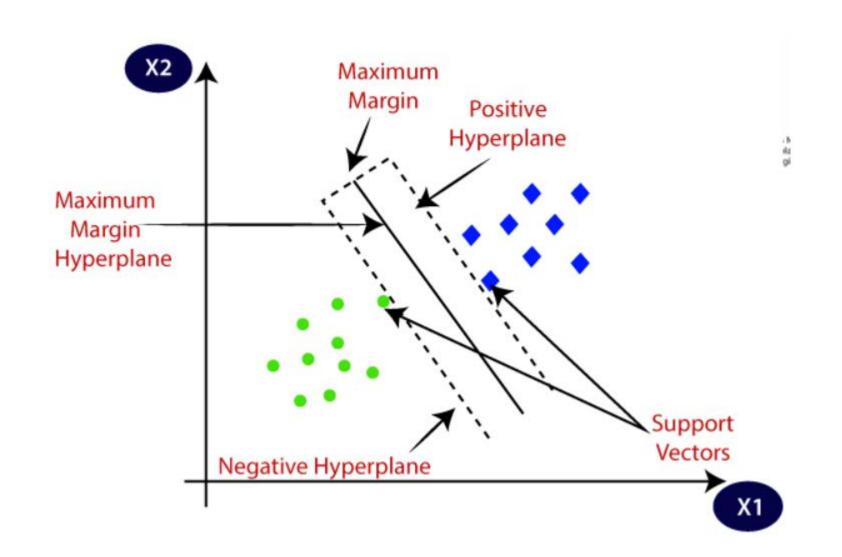


#### Other Supervised Classifiers: SVM (1)

Support Vector Machine (SVM) classifier

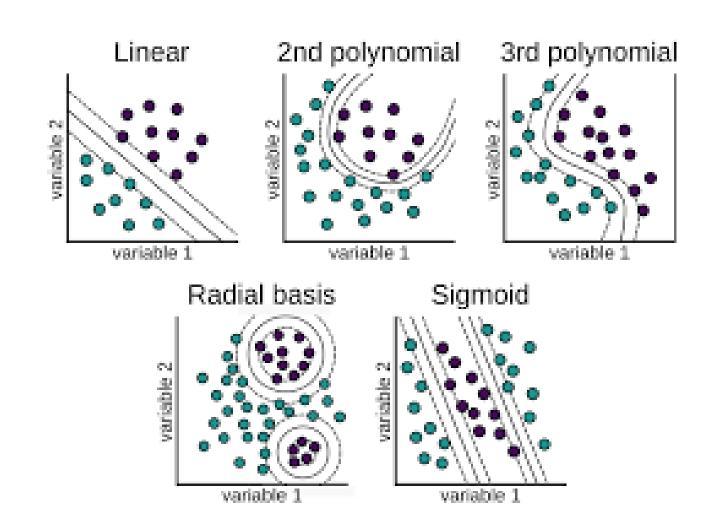


#### Other Supervised Classifiers: SVM (2)



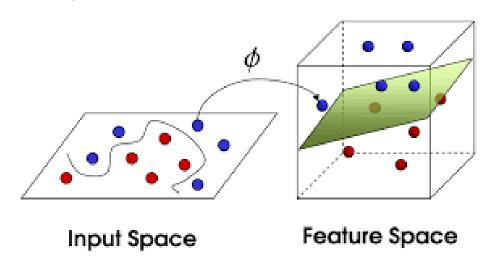
### Other Supervised Classifiers: SVM (3)

Nonlinear SVM

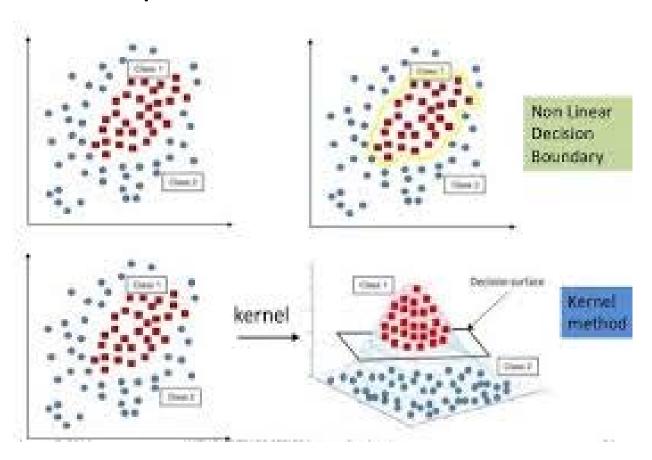


## Other Supervised Classifiers: SVM (4)

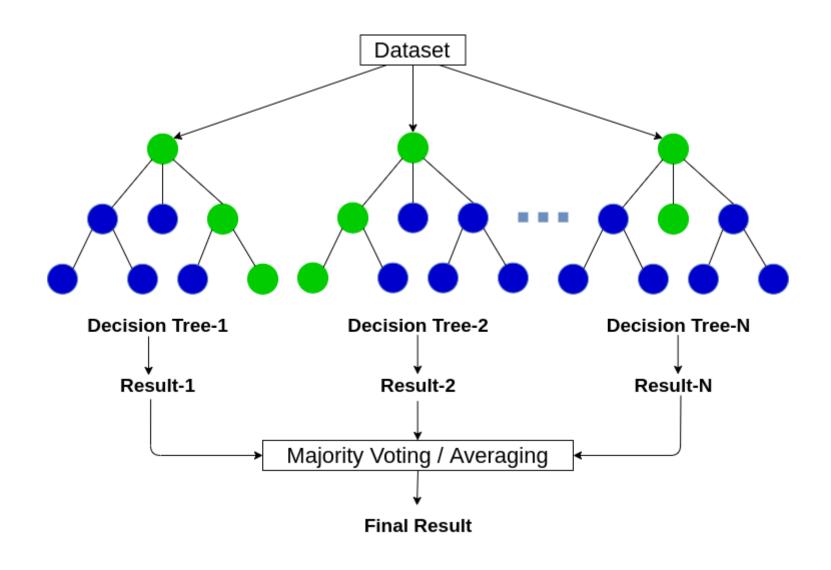
#### Example 1



#### Example 2



#### Other Supervised Classifier: Random Forest



# Back to Texture Classification and Segmentation

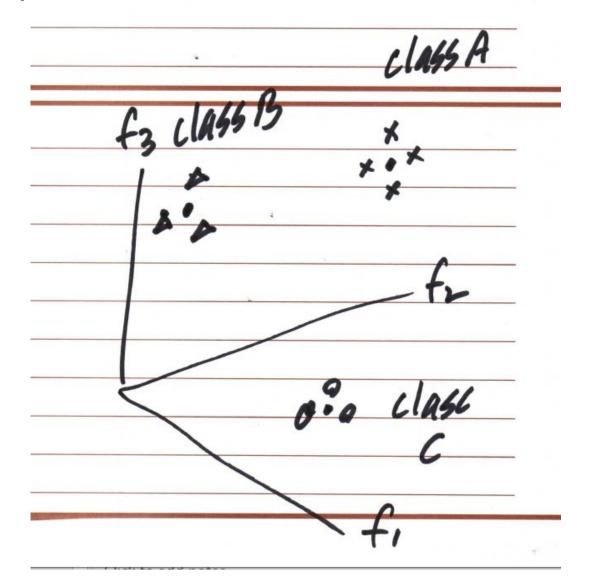
#### Differences

- Texture classification is usually treated as a supervised learning problem
  - Offer exemplar texture images from several texture types (e.g. texture type A, texture type B, texture type C, etc.)
  - Given test image X, please find its texture type
- Texture segmentation is typically treated as an unsupervised learning problem
  - One texture mosaic image that contains multiple texture types

#### Texture Classification

- Choose the window size to be the same as the image size
  - Namely, take the average of feature vectors at all pixel locations
- Suppose that there are C texture classes, where each class has Nc training images
  - Find the feature vector of each training image
  - Average the feature vectors of training images
    - Centroid of each class

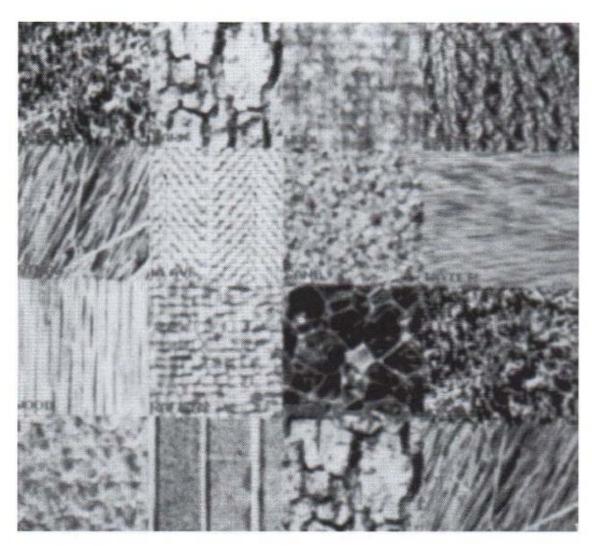
### Feature Space



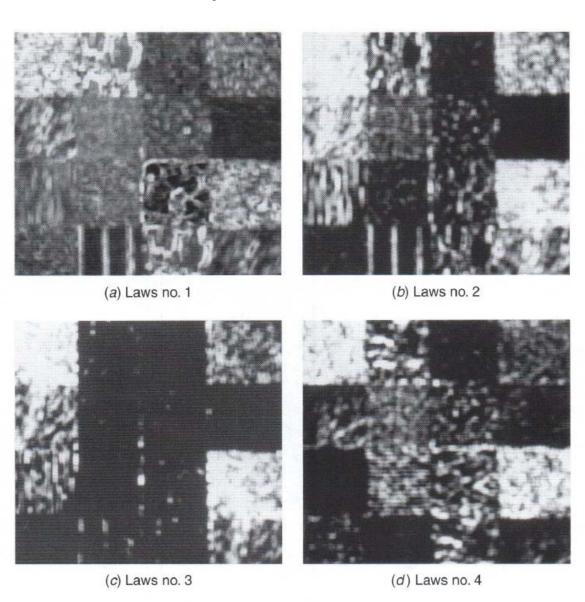
#### Texture Segmentation

- Set window size to W=13, 15 or 17
- Tradeoff:
  - For a larger window size
    - The averaged feature vector is more stable for pixels in the interior region
    - The averaged feature vector can cover multiple texture types more easily for pixels close to boundaries
  - For a smaller window size
    - The averaged feature vector could fluctuate more for pixels in the interior region
    - The average feature vector tends to cover fewer texture types for pixels close to boundaries
  - Consider a hybrid solution
    - Two-pass algorithm
    - 1<sup>st</sup> pass larger window size
    - 2<sup>nd</sup> smaller window size

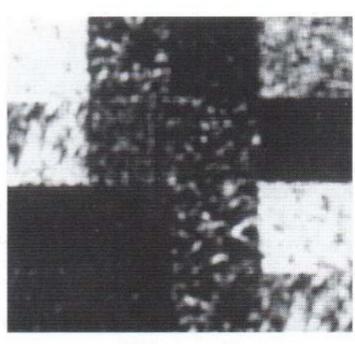
## Example of Texture Mosaic



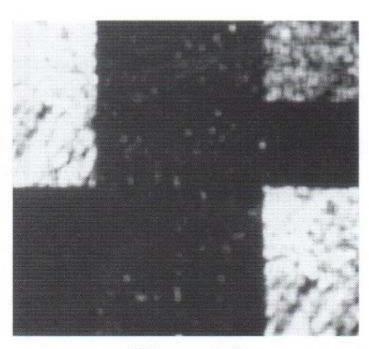
#### Energy Feature Maps of Different Channels (1)



### Energy Feature Maps of Different Channels (2)

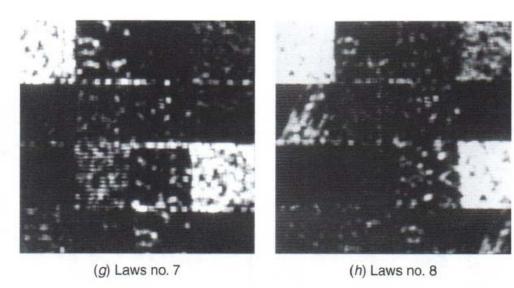


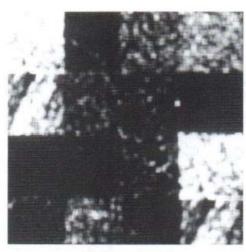
(e) Laws no. 5



(f) Laws no. 6

### Energy Feature Maps of Different Channels (3)





(i) Laws no. 9

# Window Size Selection for Energy Feature Averaging

- Set window size to W=13, 15 or 17
- Tradeoff:
  - For a larger window size
    - The averaged feature vector is more stable for pixels in the interior region
    - The averaged feature vector can cover multiple texture types more easily for pixels close to boundaries
  - For a smaller window size
    - The averaged feature vector could fluctuate more for pixels in the interior region
    - The average feature vector tends to cover fewer texture types for pixels close to boundaries
  - Consider a hybrid solution
    - Two-pass algorithm
    - 1<sup>st</sup> pass larger window size
    - 2<sup>nd</sup> smaller window size

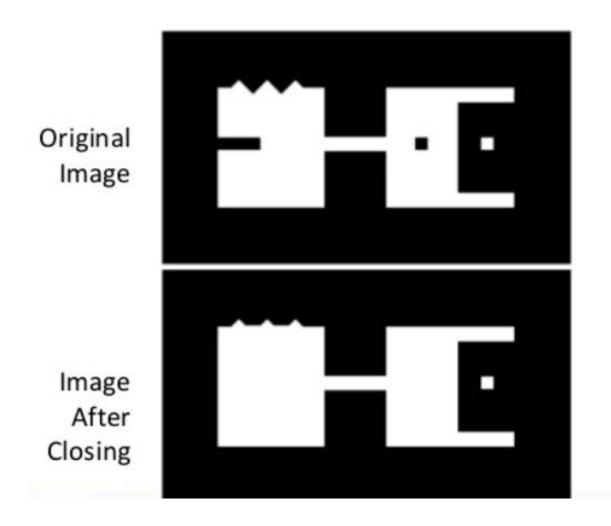
#### Criteria for Good Segmentation Results

- Qualitative Measure (rather than Quantitative)
  - Regions of a segmented image should be uniform and homogeneous w.r.t. some characteristics such as gray levels or texture
  - Region interiors should be simple and without small holes
  - Boundaries of each segment should be smooth, not ragged

#### Post-Processing of Segmentation Results

- Morphological processing to remove small holes
  - Identify small holes
  - Eliminate small holes with the close operation (structuring elements)
- Morphological processing to smooth boundaries

#### Recall: Closing Operation



You need to define the object and background properly

- Object (majority)
- Holes/background (minority)

Credit: <a href="https://www.slideshare.net/shkulathilake/morphological-image-processing-43465879">https://www.slideshare.net/shkulathilake/morphological-image-processing-43465879</a>