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# The Overlapping Generations Model by Auerbach and Kotlikoff: A Survey

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## Abstract

This survey paper provides a comprehensive examination of the overlapping generations model (OLG) developed by Auerbach and Kotlikoff, highlighting its pivotal role in analyzing economic interactions across generational cohorts. The model serves as a critical tool for evaluating the sustainability of public pension systems amid demographic changes such as aging populations and declining birth rates, which pose significant fiscal challenges. By integrating the life-cycle hypothesis, the OLG model facilitates the analysis of individual savings and consumption patterns, informing retirement planning and policy formulations. The survey underscores the importance of pension reforms and policy changes in maintaining economic stability and individual welfare, emphasizing the need for innovative risk-sharing mechanisms and tailored policy interventions. Key findings suggest that optimizing pension systems through increased contribution rates and benefit progressivity can enhance social welfare. Additionally, the integration of systematic longevity risk into pension models offers refined strategies for diverse investor types. The survey highlights the utility of generational accounting in addressing intergenerational justice and fiscal sustainability. Future research should focus on improving financial literacy, exploring alternative investment strategies, and assessing the long-term impact of reforms on pensioners' welfare. The survey concludes that the OLG model remains an indispensable tool for policymakers and researchers, providing valuable insights into the complex dynamics of intergenerational economic interactions and guiding the design of sustainable and equitable economic systems.

## 1 Introduction

### 1.1 Purpose and Significance

This survey aims to thoroughly examine the overlapping generations model (OGM) established by Auerbach and Kotlikoff, which is essential for understanding economic interactions among different age cohorts. The OGM serves as a crucial analytical framework for economists and policymakers, enabling the assessment of public pension system sustainability amidst demographic changes, particularly population aging, which presents significant fiscal challenges for developed nations [1]. By incorporating the life-cycle hypothesis, the model aids in analyzing individual savings and consumption patterns, thereby informing retirement planning and policy development [2].

Furthermore, the survey emphasizes the necessity of pension reforms and policy adjustments to maintain economic stability and individual welfare in light of evolving demographic conditions [3]. By addressing these themes, the survey highlights the OGM's role in elucidating intergenerational transfers and resource allocation dynamics, which are vital for promoting social equity and economic growth [4]. This work contributes to ongoing discussions regarding social security, pensions, and intergenerational relationships, laying a foundation for future research and policy initiatives.

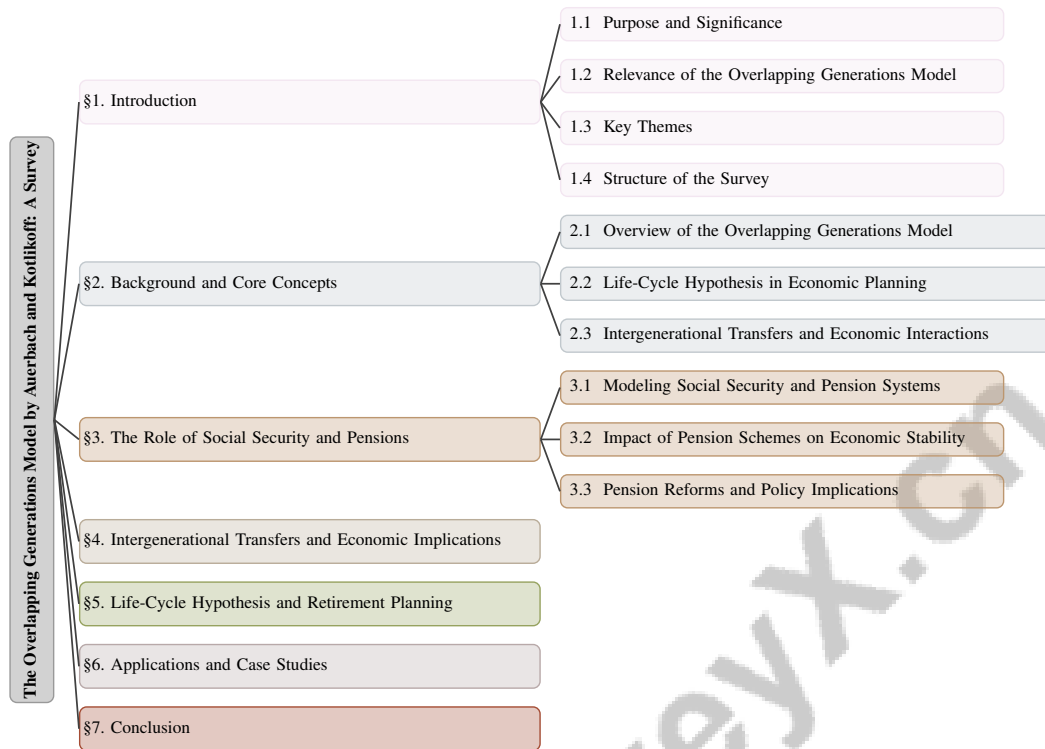


Figure 1: chapter structure

## 1.2 Relevance of the Overlapping Generations Model

The OGM is pivotal for analyzing economic interactions across generations, particularly amid demographic transitions. It provides a comprehensive framework for evaluating pension system sustainability in the face of challenges such as population aging, declining fertility rates, and increased life expectancy [5]. These demographic shifts pose substantial fiscal risks, exemplified by the unsustainable pension systems in countries like Russia, where an aging populace and a contracting workforce threaten the viability of pay-as-you-go schemes [6].

In addition to assessing pension sustainability, the model captures the complexities of pension systems, as shown in comparative analyses of the Netherlands' pension tax systems, which evaluate Exempt-Exempt-Taxed (EET) and Taxed-Exempt-Exempt (TEE) frameworks in the context of demographic changes [7]. The model also sheds light on young people's attitudes toward pensions, particularly with the implementation of auto-enrollment policies designed to encourage saving [8].

Moreover, the OGM addresses conventional metrics' limitations, such as government debt, in the context of intergenerational equity, emphasizing intergenerational fiscal justice [9]. It also illustrates how demographic transitions impact long-term economic growth, as evidenced by South Korea's experiences with an aging population [10]. Beyond pensions, the model's applicability extends to understanding the relationship between modern policies and traditional kinship practices, highlighting how pension plans can significantly alter these dynamics [11]. Its relevance is further underscored in agent-based models (ABMs), where accurately capturing age distribution is critical for predicting life cycle outcomes and economic decisions [12].

Additionally, the model incorporates insights into the social transmission of traits among agents, illustrating how behaviors, diseases, or information spread through social influence over time [13]. It also reflects the evolving principles of social security systems, transitioning from social solidarity to contribution, which is crucial for maintaining financial balance and sustainability [14]. Through these diverse applications, the OGM remains an indispensable tool for analyzing the intricate economic interactions that shape intergenerational relationships and inform policy decisions, particularly amid changing demographic and economic landscapes [4].

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### 1.3 Key Themes

The survey investigates several key themes within the OGM, focusing on their significance in elucidating economic interactions across various age cohorts. A primary theme is the influence of pension policies on cultural evolution, kinship practices, and educational investments, highlighting the transformative effects of pension systems on societal structures [11]. This theme is expanded through an examination of the challenges individuals face in managing investment risks and the potential benefits of collective risk-sharing mechanisms, which are crucial for enhancing retirement financial security [15].

Additionally, the survey explores optimal pension strategies and age-dependent risk preferences, which are vital for understanding intergenerational transfers and resource allocation. These considerations are essential for designing pension schemes that cater to the varying risk appetites of different age groups, ensuring equitable resource distribution [16]. The analysis of pension system evolution in Georgia, alongside international comparisons, underscores the importance of mandatory funded pension systems in improving pension adequacy and sustainability [3].

Furthermore, the survey addresses the optimization of neural network architectures, model efficiency, and the balance between model complexity and computational efficiency, increasingly relevant in economic modeling and forecasting contexts [17]. Collectively, these themes provide a comprehensive overview of the multifaceted dynamics within the OGM framework, offering critical insights into the interplay between social security, pensions, and intergenerational transfers.

### 1.4 Structure of the Survey

This survey is meticulously structured to provide a comprehensive exploration of the OGM, developed by Auerbach and Kotlikoff, and its implications for economic interactions across various age groups. The paper begins with an **Introduction**, outlining the study's purpose and significance, emphasizing the model's relevance in addressing demographic transitions and its critical role in understanding intergenerational economic dynamics. This section introduces key themes such as social security, pensions, and intergenerational transfers.

Following the introduction, offers an in-depth exploration of the foundational principles underlying the OGM, crucial for understanding how demographic transitions affect long-term economic growth projections, as illustrated in Kwon's analysis of Korea's economic dynamics [18, 10]. It elucidates core concepts like the life-cycle hypothesis, intergenerational transfers, and the role of social security and pensions in economic planning, establishing a framework for understanding the interconnectedness of these elements within the model.

**Section 3: The Role of Social Security and Pensions** examines how these systems are modeled within the OGM framework, highlighting the significant implications of various pension schemes and policies for retirement planning and resource allocation. It focuses on how the structure and management of pension systems—such as Georgia's mandatory funded pension system—affect economic stability and individual welfare. This section emphasizes the necessity of optimizing pension and social security costs to ensure a decent quality of life in old age while alleviating budgetary pressures. Additionally, it addresses how market risks impact pension fund sustainability, particularly within the New Pension System (NPS), and the importance of effective investment strategies and government responsibilities in safeguarding against potential shortfalls in pension corpus [3, 19].

In **Section 4: Intergenerational Transfers and Economic Implications**, the focus shifts to the significance of intergenerational transfers within the model, analyzing their effects on wealth distribution, economic growth, and social equity, while exploring policy implications in the context of aging populations and changing demographics.

investigates how the life-cycle hypothesis can be integrated into retirement planning models, providing valuable insights for developing strategies that address challenges posed by an aging population, particularly in the Malaysian energy sector. This section underscores the importance of understanding psychological, social, and environmental influences on retirement preparedness, emphasizing proactive financial planning for a sustainable quality of life in retirement [20, 21, 22]. It explores the effects of demographic changes and economic policies on individual savings and consumption patterns over a lifetime.

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The survey then presents **Section 6: Applications and Case Studies**, showcasing real-world applications of the OGM through case studies and empirical research that illustrate the model's utility in analyzing issues related to social security, pensions, and intergenerational resource allocation.

Finally, **Section 7: Conclusion** synthesizes the key findings and insights from the survey, reflecting on the model's importance in understanding economic dynamics across generations and suggesting areas for future research and potential policy implications. Through a systematic methodology, this survey conducts a comprehensive analysis of the OGM, highlighting its significance in addressing current economic issues such as demographic transitions, fiscal burdens, and intergenerational justice, as explored in recent studies, including Kwon's examination of Korea's long-term growth projections [18, 10, 9]. The following sections are organized as shown in Figure 1.

## 2 Background and Core Concepts

### 2.1 Overview of the Overlapping Generations Model

The overlapping generations (OLG) model, introduced by Auerbach and Kotlikoff, is a critical framework in economic theory for understanding interactions among generational cohorts. Based on the life-cycle hypothesis, it examines how individuals' consumption and savings decisions impact successive generations' economic conditions, facilitating a thorough analysis of intergenerational transfers and resource allocation [2]. The OLG model categorizes public pension systems into pay-as-you-go (PAYG) and fully funded schemes, crucial for evaluating fiscal sustainability amid demographic trends like aging populations and declining birth rates [6]. Its flexibility in incorporating diverse demographic and economic variables enhances its utility in assessing pension systems' long-term viability and fiscal policy implications [14]. This framework also classifies pension systems based on funding principles, contrasting distribution-based and accumulation-based systems [3].

The model adeptly incorporates complex economic behaviors, analyzing parental transfers' impact on children's wealth and education [23]. It explores optimal consumption and investment decisions through the Dynamic Life-Cycle Model with Age-Dependent Preferences, optimizing decisions for pension fund investors [16]. Additionally, the OLG model addresses local determinacy of steady states, differentiating between monetary and non-monetary steady states, essential for understanding economic equilibria stability [24]. Insights into hybrid pension plans that merge defined benefit and defined contribution plans are also provided, addressing limitations in light of increasing life expectancy and demographic shifts [25].

Social networks and agents' heterogeneity, particularly sociability attributes, play a significant role in shaping economic interactions and outcomes within the model [13]. Its adaptability is further evidenced in agent-based modeling, which critiques traditional models for unrealistic assumptions and proposes new approaches to better capture intergenerational preferences in pension policy [5]. The OLG model evaluates various economic models, including cash-in-advance and cobweb models, utilizing datasets derived from chaotic behaviors, underscoring its capacity to address complex economic phenomena [26]. Its comprehensive structure and assumptions make it an indispensable tool for analyzing intergenerational economic dynamics, providing valuable insights for policymakers and researchers.

### 2.2 Life-Cycle Hypothesis in Economic Planning

The life-cycle hypothesis is central to economic planning within the overlapping generations model, offering a framework for understanding how individuals allocate consumption and savings over their lifetime. It posits that individuals smooth consumption in response to income fluctuations, optimizing financial well-being. This hypothesis informs retirement planning strategies, structuring pension benefits and optimal retirement ages, vital for pension system sustainability [27]. Incorporating the life-cycle hypothesis into economic planning requires understanding demographic changes that influence labor supply and consumption-saving decisions, affecting the capital-labor ratio and necessitating policy adjustments to maintain economic equilibrium [10]. The hypothesis is enriched by considering rational inattention, emphasizing informational frictions in retirement decisions and the need for models accounting for cognitive limitations and information acquisition costs [28].

The hypothesis examines risk aversion and mortality's roles in shaping investment decisions, with models incorporating age-dependent risk preferences revealing a tendency to minimize investment

risk as retirement approaches [16]. Advanced algorithms, such as deep reinforced learning, enhance analysis of optimal agent behavior in life-cycle models and social security reforms [29]. Economic planning under the life-cycle hypothesis must consider chaotic behavior observed in economic models, understood through dynamical systems and ergodic theory, highlighting the importance of recognizing such behavior in developing robust economic policies [26]. The hypothesis underscores the significance of diverse pension systems—public, private, and mixed—in providing retirement income, stressing the need for structures supporting individuals throughout their life cycle [4].

The integration of the life-cycle hypothesis into economic planning is further complicated by involuntary unemployment, which can persist even with divisible labor supply due to economic instability, emphasizing adaptive expectations and policy interventions to stabilize outcomes [30]. The hypothesis’s relevance extends to tax system design, influencing savings and consumption across demographic scenarios [7]. It provides a comprehensive framework for understanding individual financial behavior and integration into broader economic planning, offering critical insights for policymakers aiming to design sustainable and equitable economic systems, particularly in production economies where local determinacy varies based on utility and production functions [24].

### 2.3 Intergenerational Transfers and Economic Interactions

Intergenerational transfers are vital to economic interactions and stability within the overlapping generations framework, facilitating resource allocation across age cohorts. These transfers, including public pension benefits and private household contributions, significantly impact wealth distribution, economic growth, and social equity. The OLG model, through generational accounting, offers a method for assessing fiscal burdens on future generations and the sustainability of these transfers [9]. Heterogeneity in initial savings and investment strategies critically influences income stability and fluctuations, particularly in pooled annuity funds, where wealth disparities can affect overall economic equilibrium [31]. The model highlights challenges posed by dynamic inefficiency, akin to capital overaccumulation, arising from suboptimal resource allocation across generations [18].

The transition from PAYG to fully funded pension systems exemplifies intergenerational transfers’ complexity, imposing economic burdens on all generations that can reduce consumption and increase work efforts, necessitating careful policy design [6]. The imbalance between active contributors and retiring beneficiaries, exacerbated by rising life expectancy and declining birth rates, poses challenges to pension system sustainability [14]. Intergenerational preferences significantly shape pension policy, with conflicting preferences among age groups often obstructing effective reform [5]. Understanding these preferences is essential for designing policies that equitably allocate resources and ensure economic stability for current and future generations.

The transmission of traits—such as behaviors or awareness—among agents over time is critical in influencing the persistence or extinction of economic practices and policies within the OLG model [13]. These social transmission dynamics underscore the need to consider behavioral and informational factors in analyzing intergenerational transfers.

## 3 The Role of Social Security and Pensions

Category	Feature	Method
<b>Modeling Social Security and Pension Systems</b>	Risk Management Strategies	DLM-ADP[16]
<b>Impact of Pension Schemes on Economic Stability</b>	Stochastic Simulation Techniques	SDM-DL[32], MCS-PR[19], SDP-PF[33]
	Optimization and Control Strategies	RZCLB[34], NAOICS[35], ROCA-HP[25]

Table 1: This table provides a comprehensive summary of the methodologies employed in modeling social security and pension systems, as well as their impact on economic stability. It categorizes the methods into risk management strategies and optimization techniques, highlighting the diverse approaches used in assessing and enhancing pension scheme sustainability.

Social security and pension systems are crucial for economic stability and individual welfare. This section delves into these systems’ complexities using the overlapping generations framework, focusing on contributory versus non-contributory schemes and their implications for economic and personal stability. Table 1 presents a detailed summary of the methodologies used in modeling social security and pension systems and their implications for economic stability. Additionally, Table 3 presents a comprehensive comparison of various methodologies used in modeling social security and pension

systems, focusing on their implications for economic stability and policy reforms. ?? illustrates the hierarchical structure of social security and pension systems, emphasizing modeling methodologies, economic impacts, and reform implications. The figure categorizes key concepts into frameworks, challenges, strategies, risks, and policy tools, highlighting their roles in ensuring sustainability and economic stability. The subsequent subsection explores methodologies for modeling these systems, emphasizing the integration of diverse economic, demographic, and policy variables to evaluate their sustainability and effectiveness.

### 3.1 Modeling Social Security and Pension Systems

The overlapping generations model is essential for analyzing social security and pension systems, integrating various economic, demographic, and policy variables. Distinguishing between contributory and non-contributory pension schemes is crucial, as it significantly impacts economic stability and individual welfare. The shift from defined benefit to defined contribution plans transfers risk from governments to employees, highlighting the need for innovative risk-sharing mechanisms to ensure intergenerational equity [25].

Demographic transitions, such as increased life expectancy and declining birth rates, challenge Pay-as-you-go (PAYG) pension schemes, necessitating policy adjustments for fiscal sustainability. Comparing pension models like Bismarckian and Beveridgean reveals significant differences in resource allocation and long-term viability, with Bismarckian systems typically allocating more resources to pensions [4]. Incorporating stochastic elements, such as stochastic diffusion processes, enhances pension sustainability assessments by integrating demographic data with economic forecasts [33], capturing uncertainties in demographic and economic variables.

Figure 2 illustrates the hierarchical structure of social security and pension systems, focusing on pension scheme types, demographic challenges, and policy sustainability. This figure highlights the complexity of contributory and non-contributory schemes, demographic transitions affecting pension models, and the importance of policy adjustments for sustainability. Aligning social welfare with economic efficiency is paramount, underscoring the importance of designing pension annuities that mitigate idiosyncratic longevity risk while pooling systematic risk to enhance retirees' financial security [16]. Insights from Japan on social security reforms illustrate diverse impacts on household welfare across generations, genders, and employment types [36]. Furthermore, applying chaotic dynamical systems to economic models offers a novel perspective on pension systems' complex behaviors, enriching sustainability analyses [26].

The effectiveness of mandatory funded pension systems in enhancing individual welfare, as seen in Georgia, underscores the critical role of policy design in promoting pension adequacy and sustainability [3]. Through these theoretical and empirical perspectives, the overlapping generations model provides a comprehensive framework for analyzing and optimizing social security and pension systems, offering insights into their sustainability and effectiveness in fostering intergenerational economic stability.

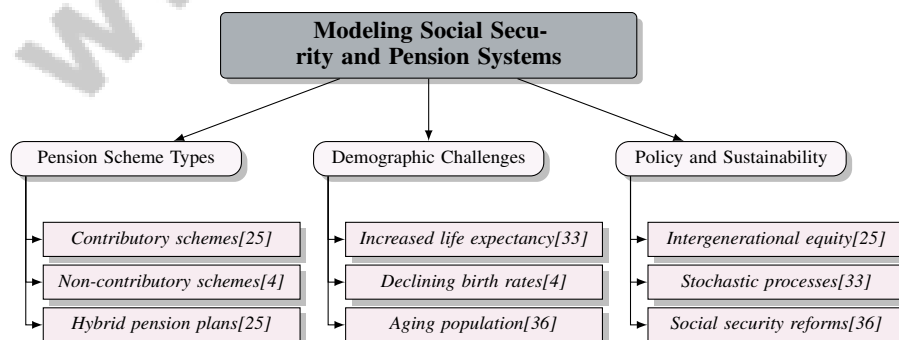


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### 3.2 Impact of Pension Schemes on Economic Stability

Method Name	Economic Stability	Risk Management	Demographic Adaptation
SDM-DL[32]	Pension System Affordability	Financial Risks Management	Ageing Population Adaptation
MCS-PR[19]	Fiscal Responsibilities	Market Risks	-
RZCLB[34]	Longevity Market Development	Rolling Zero-coupon	Dynamic Hedging Longevity
NAOICS[35]	Resource Allocation	Financial Risks Management	Increasing Life Expectancies
SDP-PF[33]	Resource Allocation	Stochastic Processes	Demographic Changes
ROCA-HP[25]	Resource Allocation	Financial Risks	Longevity Trends

Table 2: Comparison of Various Pension Scheme Methods in Terms of Economic Stability, Risk Management, and Demographic Adaptation.

Pension schemes significantly influence economic stability and individual welfare, involving demographic trends, financial risks, and policy frameworks. Within the overlapping generations model, pension systems are pivotal in resource allocation and risk management across age cohorts. Recent reforms have shown promise in alleviating the pension crisis, enabling extended retirement periods without overburdening healthcare systems, thus contributing to economic stability [32]. Table 2 provides a comprehensive comparison of different pension scheme methods, highlighting their contributions to economic stability, risk management, and demographic adaptation.

Optimizing financial strategies, such as bequest proportions and fractional consumption rates, enhances pension schemes' adaptability to individual needs, supporting economic stability and welfare [37]. Market risks, particularly fluctuations in returns and annuity rates, significantly affect the pension corpus's ability to sustain retirees' livelihoods, underscoring the necessity for robust risk management strategies [19]. Developing a longevity market is critical for managing longevity basis risk, ensuring pension schemes remain viable amid increasing life expectancies [34].

Innovative investment strategies, including collectivized pension investment approaches, demonstrate efficiency in computing optimal strategies, offering rapid convergence and stability compared to traditional methods [35]. These strategies, alongside models that maximize capital accumulation at retirement while minimizing volatility, present viable alternatives to conventional pension schemes, enhancing economic stability [38].

Systematic predictions of financial needs, supported by advanced modeling techniques, are essential for maintaining pension fund sustainability [33]. However, the unpredictable nature of financial markets and demographic trends poses challenges, potentially leading to negative cash flows in pension funds [39]. Deferring Social Security benefits based on wealth-to-primary insurance amount ratios can significantly enhance individual welfare and economic stability by optimizing retirement income [27].

A robust optimal control approach addresses investment challenges in hybrid pension plans, emphasizing the need to adjust retirement ages in response to demographic trends [25]. However, social security reforms may adversely affect current low-income groups, especially women and contingent workers [36]. The pension gap can be partially covered for late retirees, highlighting greater challenges for those with dynamic careers [40].

The design and implementation of pension schemes, coupled with strategic investment and informed policy decisions, are crucial for ensuring economic stability and improving individual welfare. These elements must adapt to changing demographic trends and address longevity disparities to optimize resource allocation and enhance retirement system sustainability. Effective pension reforms, as observed in Georgia and other countries, underscore the importance of balancing contributions and benefits to meet diverse worker needs while maintaining fiscal responsibility and promoting equitable outcomes across socioeconomic groups [41, 21, 42, 3, 1].

### 3.3 Pension Reforms and Policy Implications

Pension reforms are vital for ensuring the sustainability and effectiveness of pension systems, particularly within the overlapping generations (OLG) model framework, where demographic and economic factors are intricately intertwined. A primary challenge addressed by reforms is the growing disparity in life expectancy across socioeconomic groups, which can exacerbate inequalities in pension outcomes. Reforms must consider these disparities to promote equitable pension distributions [21]. Increasing the retirement age is a common reform proposal to counteract the adverse effects of

demographic aging, potentially mitigating welfare losses and enhancing pension system viability [43].

Accurate information dissemination and correction of misconceptions about pension eligibility are crucial for effective participation in pension schemes. Enhancing financial literacy and transparency can significantly improve participation rates and decision-making among beneficiaries [44]. Organizational initiatives aimed at improving retirement planning and financial literacy are essential for informed decision-making and optimal engagement with pension schemes [22].

Incorporating stochastic elements and health status proxies into pension models provides a realistic framework for evaluating reform outcomes, allowing for accurate predictions and adjustments to changing economic conditions [45]. The IRS-DC model, which enables automatic adjustments to individual accounts based on funding ratios, exemplifies how pension schemes can become more adaptable and welfare-enhancing [15].

Generational Accounting serves as a valuable tool for analyzing and comparing the impacts of pension reforms across countries, highlighting implications for intergenerational balance and fiscal sustainability. This approach is crucial for understanding long-term policy effects and ensuring equitable and sustainable pension systems across generations [46]. Additionally, distinguishing between savings and pension contributions can enhance families' financial freedom, allowing for flexible resource allocation and improved financial security [47].

Utilizing random walks in modeling pension funds provides insights into sustainability and management, offering a novel perspective on pension fund reserve dynamics [39]. Time inconsistency, which can lead to multiple steady states in the economy, underscores the importance of establishing a renegotiation-proof equilibrium for achieving intergenerational equity [48]. The study by Ana (2019) reinforces the importance of OLG models in analyzing social security systems, particularly in predicting financial equilibrium amidst demographic changes [14]. Pension reforms and policy changes profoundly influence the predictions of the OLG model, shaping its capacity to address the complex dynamics of intergenerational economic interactions and ensuring pension system sustainability.

Feature	Modeling Social Security and Pension Systems	Impact of Pension Schemes on Economic Stability	Pension Reforms and Policy Implications
Economic Impact	Intergenerational Equity	Resource Allocation	Fiscal Sustainability
Risk Management	Innovative Mechanisms	Longevity Market	Automatic Adjustments
Demographic Adaptation	Stochastic Elements	Policy Adjustments	Retirement Age Increase

Table 3: This table provides a comparative analysis of the methodologies employed in modeling social security and pension systems, emphasizing their economic impacts, risk management strategies, and demographic adaptations. It highlights the key features of different approaches, including intergenerational equity, resource allocation, fiscal sustainability, and policy adjustments, thereby offering insights into the implications of pension reforms on economic stability.

## 4 Intergenerational Transfers and Economic Implications

Examining the economic implications of intergenerational transfers requires understanding the principles governing interactions among age cohorts. These transfers reflect financial arrangements and interdependencies, encapsulating equity and risk management concepts, especially in education, pensions, and health. They mirror societal values of social solidarity and sustainability, increasingly challenged by demographic shifts, economic pressures, and evolving family structures [47, 19, 14, 4, 1]. The overlapping generations model (OLG) provides insights into intergenerational equity and risk sharing, highlighting the impact of policy decisions on various cohorts and enhancing our understanding of economic stability and generational welfare.

### 4.1 Intergenerational Equity and Risk Sharing

Intergenerational equity and risk sharing are central to the OLG model, emphasizing the balance of current and future generations' needs for sustainable economic outcomes. Moiseev underscores the importance of recognizing distinct cohort responses to pension reforms, advocating for tailored policy interventions [6]. The life-cycle model's intergenerational altruism concept aids in addressing generational welfare and equity, guiding policymakers in ensuring fair resource distribution [14]. Golub's work on contagion elucidates behaviors affecting economic transmission across generations [13].



Risk-sharing mechanisms are vital for sustaining pension benefits. Milazzo highlights the retirement age's role in pension adequacy, suggesting that adjustments significantly impact system sustainability and equity [40]. Stochastic processes, such as random walks and Brownian motion, offer robust models for pension fund reserve evolution, guiding equitable resource allocation [26].

Age-dependent risk aversion significantly influences wealth distribution and investment strategies, particularly in pension fund management. This relationship underscores the need for policies promoting intergenerational equity as aging populations increasingly rely on pension funds, major stock market players. Optimal consumption and investment decisions must consider risk preferences' time-varying nature across cohorts, necessitating adaptive financial market strategies to ensure sustainable retirement savings and equitable wealth distribution [49, 16].

To illustrate these concepts, Figure 3 presents a figure that illustrates the hierarchical structure of intergenerational equity and risk sharing in the context of pension reforms, risk-sharing mechanisms, and investment strategies, highlighting the key concepts and their interrelations. The OLG model integrates diverse insights, offering guidance for designing equitable and sustainable economic systems addressing both current and future generations' needs.

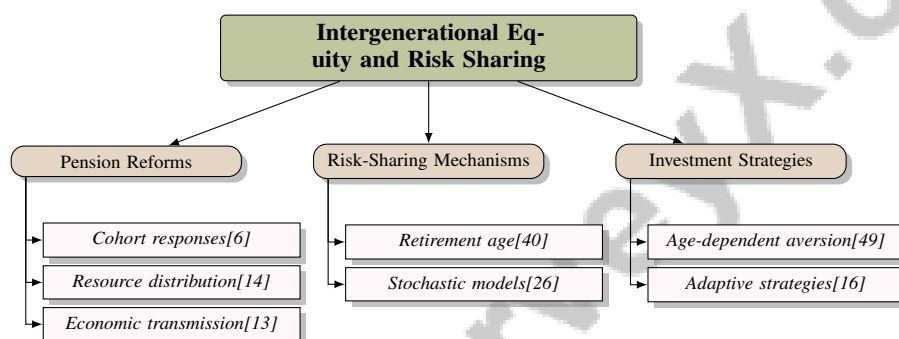


Figure 3: This figure illustrates the hierarchical structure of intergenerational equity and risk sharing in the context of pension reforms, risk-sharing mechanisms, and investment strategies, highlighting the key concepts and their interrelations.

## 4.2 Impact of Demographic Changes on Wealth Distribution

Demographic changes, notably aging populations and declining fertility rates, significantly impact wealth distribution and economic growth, altering resource allocation dynamics across generations. Kwon's study illustrates how these trends in Korea reduce the labor force and increase the dependency ratio, necessitating policy adjustments for economic stability and equitable resource distribution [10].

Increasing life expectancy and demographic shifts challenge pension planning, as Fu advocates for flexible systems adapting to an aging population's needs [25]. Pension fund sustainability is further complicated by the gambler's ruin probability, deemed crucial for long-term viability by Ferreira [39]. This underscores the need for careful management and policy planning to mitigate demographic change risks.

In Japan, the rise of contingent workers and the persistent gender income gap significantly influence wealth distribution, as noted by Iiboshi [36]. These socioeconomic factors necessitate targeted policies addressing the unique challenges faced by various demographic groups to ensure equitable wealth distribution. Furthermore, as Khozrevidze discusses, inadequate pension support often fails to meet retirees' basic needs, exacerbating wealth disparities and undermining public trust in the system [3].

Demographic changes play a crucial role in shaping wealth distribution and economic growth. Addressing these impacts requires comprehensive policy frameworks promoting intergenerational equity and economic stability. By analyzing the complex relationship between demographic trends and their economic implications, policymakers can develop targeted strategies fostering sustainable and equitable economic growth, ensuring social security systems remain viable and responsive to diverse populations in an evolving demographic landscape [21, 50, 10].

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### 4.3 Heterogeneity and Intergenerational Transfers

Heterogeneity significantly influences intergenerational transfers and resource allocation within the OLG model. Variations in individual productivity, retirement preparedness, and risk preferences affect pension transfers' effectiveness. Armstrong highlights managing diverse investor needs within a collectivized framework, necessitating tailored strategies to accommodate varying preferences [41]. His work on collectivized pension investment demonstrates optimal strategies' robustness in heterogeneous settings as investor numbers increase [51].

Market risks critically impact pension fund sustainability. Das employs Monte Carlo simulations to quantify risks associated with market returns and annuity rates, providing insights for enhancing retirees' financial security amidst varying market conditions [19]. Agarwal suggests exploring multiple longevity bonds and refining risk-sharing mechanisms to strengthen pension schemes against longevity risk, emphasizing the accommodation of diverse demographic and economic variables [34].

Shared-indexation collective defined contribution (CDC) schemes offer a nuanced understanding of intergenerational transfers' financial characteristics and risks, promoting equitable resource allocation across cohorts [35]. These schemes' flexibility allows investment strategies to adapt to individual investors, accommodating inherent heterogeneity in intergenerational transfers.

Ferreira underscores the need for innovative pension fund management approaches, identifying existing methods' limitations in predicting financial requirements due to demographic changes [33]. Developing strategies that address different age groups' diverse needs and characteristics is essential for effective pension management.

## 5 Life-Cycle Hypothesis and Retirement Planning

The Life-Cycle Hypothesis emphasizes the strategic allocation of resources over an individual's lifetime to optimize utility, underscoring the critical interplay between consumption patterns and retirement planning. It highlights the necessity for effective financial management as individuals transition into retirement. The subsequent subsection delves into optimal consumption strategies for retirees, taking into account factors such as wealth heterogeneity and market risks that influence financial decision-making during retirement. A comprehensive understanding of these strategies is essential for retirees aiming to maintain financial stability and achieve their desired standard of living.

### 5.1 Optimal Consumption Strategies for Retirees

Optimizing consumption strategies for retirees involves an integrated approach that combines advanced modeling techniques, financial literacy, and individual preferences. Time preferences are pivotal in retirement planning, significantly influencing consumption and savings behaviors. A nuanced understanding of financial literacy, trust in financial institutions, and personal time preferences is vital for crafting effective retirement policies that enhance long-term savings behaviors and mitigate old-age poverty risks in an era of increasing life expectancy [44, 52, 53].

Wealth heterogeneity among retirees poses challenges in securing stable income during retirement, which can be mitigated through innovative financial strategies like pooled annuity funds. These funds enable individuals to share longevity risks and income fluctuations, thereby enhancing income stability by pooling resources from individuals with diverse initial savings. This method promotes equitable distribution of retirement income and can be supplemented by collectivized investment strategies that redistribute assets among surviving members, reducing the capital required for desired income levels [21, 54, 41, 31]. Furthermore, the impact of market risks on pension adequacy against inflation-adjusted living costs is crucial for optimizing consumption strategies, necessitating robust risk management.

Incorporating time-inconsistent preferences into economic models provides a deeper analysis of retirement planning, illustrating how variations in time preferences and financial literacy influence consumption decisions and retirement preparedness. This framework sheds light on the interplay between individual characteristics, planning behaviors, and misconceptions about retirement policies [44, 52, 16, 28]. Moreover, optimizing asset allocation in defined contribution plans enhances expected returns and manages risks, informing consumption strategies aligned with retirees' risk tolerance.

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Stochastic optimal control applications, particularly in wealth accumulation dynamics within pension funds, offer valuable insights into retirement resource management. This theoretical framework assists in formulating strategies for optimizing capital accumulation during retirement, leveraging lifecycle models to determine the optimal timing for claiming Social Security benefits based on wealth-to-primary insurance amount ratios. Emphasizing the role of financial literacy in retirement planning addresses systemic resource mobilization challenges, highlighting the importance of informed decision-making and proactive saving behaviors to mitigate old-age poverty [44, 27, 43]. Exploring default savings systems could further enhance retirement preparedness, ensuring financial stability in later life.

Evaluating perpetual and finite time maintenance costs in pension funds provides insights into optimal consumption strategies for effective pension fund management. This approach underscores the importance of strategic planning in ensuring financial stability for retirees, particularly in the context of insufficiently financed pension schemes requiring external financing. Utilizing stochastic modeling techniques, such as diffusion processes and renewal-reward frameworks, addresses demographic risks and evolving financial conditions, guiding policymakers in balancing sustainability, adequacy, and fairness in pension distributions [33, 55]. By leveraging these advanced modeling techniques and understanding individual preferences, retirees can achieve greater financial security and stability, maintaining their desired standard of living throughout retirement.

## **5.2 Life Expectancy and Retirement Planning**

Life expectancy plays a crucial role in shaping retirement planning and savings strategies, directly impacting retirement timing and the adequacy of accumulated resources. The complexity of modeling stochastic volatility and random contributions, as explored by Bosserhoff, underscores the challenges in predicting retirement outcomes and the necessity for sophisticated modeling techniques to address these uncertainties [56]. Furthermore, incorporating pension income into optimization frameworks complicates traditional retirement planning strategies, as varying pension incomes can affect overall planning [57].

The reliance on Employees Provident Fund (EPF) savings, often insufficient for a comfortable retirement, presents a significant challenge, highlighting the need for comprehensive retirement planning that considers diverse income streams and potential financial shortfalls [22]. Additionally, Dagpunar's evaluation of different scenarios using UK Office of National Statistics life tables illustrates how bequest motives and risk aversion levels influence retirement planning decisions [37].

Retirees face complexities such as mortality, longevity, and investment risks, further complicated by means-tested Age Pension policies [45]. These factors necessitate a nuanced approach to retirement planning that accounts for individual risk profiles and potential policy changes. Werpachowska's analysis of historical demographic data and various scenarios for state pension ages demonstrates the impact of demographic changes on retirement planning, particularly in the context of post-Brexit migration patterns [32].

Moreover, individual patience plays a crucial role in retirement planning, as those with higher patience levels are more likely to engage in proactive planning activities, enhancing financial security in later life [52]. Kwon's study on Korea further emphasizes the importance of understanding demographic trends, particularly the projected decline in economic growth due to demographic changes, necessitating adaptive retirement planning strategies [10].

## **5.3 Behavioral Economics and Retirement Planning**

Behavioral economics provides valuable insights into the psychological factors influencing financial decision-making among retirees, significantly impacting retirement planning. By integrating psychological insights into economic models, behavioral economics enhances the understanding of financial decision-making, particularly in retirement planning. Incorporating behavioral factors, such as costly attention, into life-cycle models offers a nuanced perspective on resource allocation, considering cognitive costs associated with processing information and making financial decisions [28]. This approach underscores the importance of recognizing cognitive limitations and information acquisition costs in retirement planning, as they significantly affect consumption and savings behaviors.

As illustrated in Figure 4, the integration of behavioral economics into retirement planning encompasses key psychological factors, technological advancements, and policy impacts. This figure demonstrates how cognitive costs, behavioral patterns, and risk preferences influence retirement decisions, while advances such as deep neural networks and the uniformly self-justified equilibria (USJE) framework optimize planning. The application of deep neural networks to optimize consumption strategies, as demonstrated by Chen, illustrates the potential of leveraging real-time data to dynamically adjust retirement plans, thereby enhancing financial security [58]. This technological advancement facilitates personalized and adaptive retirement strategies that accommodate retirees' diverse needs and preferences.

Empirical studies, such as those by Jais and Clark, provide valuable insights into the psychological and behavioral factors influencing retirement planning. Jais utilizes Partial Least Square Structural Equation Modelling (PLS-SEM) to support the relationships between psychological factors and retirement planning behaviors [22]. Similarly, Clark's study of public sector workers in North Carolina combines administrative records with survey data to evaluate how behavioral factors impact retirement planning decisions [52]. These studies underscore the importance of understanding individual behavioral patterns and their implications for effective retirement planning.

The concept of uniformly self-justified equilibria (USJE) offers a robust framework for analyzing retirement planning decisions, ensuring guaranteed existence, computational tractability, and rigorous error analysis [59]. This framework facilitates the development of accurate models that incorporate behavioral insights, enhancing the predictive power of retirement planning models.

The impact of social security reforms on retirement planning is significant, as discussed by Iiboshi, who highlights potential improvements in future generations' welfare while posing challenges for current generations, particularly vulnerable groups [36]. Understanding policy expectations, as explored by Zhang, is crucial for designing retirement policies that align with household financial needs and promote long-term financial security [60].

Furthermore, Golub's findings indicate that different types of contagion exhibit distinct dynamics, with complex contagions requiring critical mass for persistence, while simple contagions can thrive in smaller populations [13]. This underscores the importance of understanding social influence and behavioral transmission in shaping retirement planning decisions.

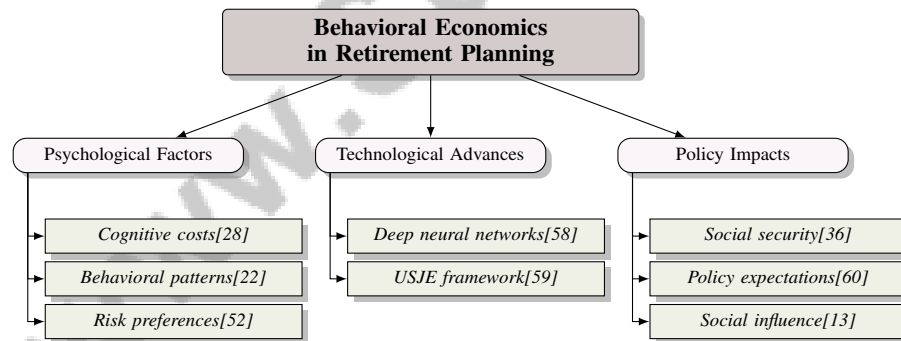


Figure 4: This figure illustrates the integration of behavioral economics into retirement planning, highlighting key psychological factors, technological advancements, and policy impacts. It demonstrates how cognitive costs, behavioral patterns, and risk preferences influence retirement decisions, while advances like deep neural networks and the USJE framework optimize planning. Additionally, it explores the effects of social security reforms, policy expectations, and social influences on retirement strategies.

## 6 Applications and Case Studies

Exploring applications and case studies in pension systems reveals the complex dynamics of their design and management. A comparative analysis of these systems provides a foundational understanding, enabling a systematic evaluation of different frameworks under various demographic and economic conditions. By examining structural characteristics and funding methodologies across countries, this analysis underscores the diversity of pension systems and facilitates insights into their

effectiveness and sustainability. The subsequent subsection will delve into a comparative analysis of pension systems, focusing on critical differences that affect their performance and viability amidst societal changes.

## 6.1 Comparative Analysis of Pension Systems

Benchmark	Size	Domain	Task Format		Metric
DRA[60]	13,939	Economics	Savings Behavior Analysis		Savings Rate 1, Savings Rate 2
CDC[61]	1,000,000	Pension Economics	Performance Evaluation		Intergenerational Cross-Subsidy Ratio, Replacement Ratio
NRPS[62]	12,000	Economics	Intergenerational Analysis	Transfers	Probability of receiving transfers, Average transfer amount

Table 4: Summary of benchmark datasets employed in the analysis of pension systems, detailing their size, domain, task format, and evaluation metrics. The table includes datasets focused on savings behavior, pension economics, and intergenerational transfers, providing a foundation for comparative analysis within the overlapping generations model.

Comparative analysis within the overlapping generations model offers nuanced insights into how diverse structural characteristics, funding methods, and demographic contexts influence pension systems’ sustainability and effectiveness. This comprehensive examination highlights critical differences stemming from unique configurations and economic environments [63]. Janssen’s research [7] employs a general equilibrium framework to analyze interactions among households, firms, and government, emphasizing the importance of understanding complex economic interdependencies for effective pension policy design.

As illustrated in Figure 5, the key aspects of pension systems are depicted, highlighting structural characteristics, investment strategies, and the challenges associated with potential reforms, all of which are grounded in various academic studies. Furthermore, Table 4 presents an overview of the benchmark datasets utilized for evaluating pension systems, highlighting their relevance in understanding the economic and demographic factors influencing pension sustainability. Chen’s study [15] utilizes a stylized model adaptable for real-world applications, demonstrating innovative risk-sharing mechanisms that enhance retirees’ financial security. This analysis underscores the necessity for pension systems to incorporate adaptive strategies addressing demographic changes and economic uncertainties. Armstrong’s method [35] employs a dimension-reduced Hamilton-Jacobi-Bellman equation for efficient computation of optimal strategies, illustrating the potential of collectivized investment strategies to improve pension systems’ robustness and efficiency.

Khozrevanidze’s analysis [3] of Georgia’s pension system highlights challenges faced by countries with lower replacement rates and insufficient funding, emphasizing the importance of adequate funding and effective policy design for sustainability. Milazzo’s work [40] contributes to the literature on optimal investment strategies in defined contribution schemes, underscoring strategic financial planning’s significance in addressing pension gaps and enhancing retirement security.

Mihailescu [26] proposes using inverse limits to analyze stability and ergodic properties of economic models, providing insights into the long-term stability of pension systems amid demographic shifts and economic fluctuations. By examining various configurations and socio-economic implications, policymakers can formulate comprehensive strategies that foster intergenerational equity and enhance economic stability, addressing longevity heterogeneity, reforming pay-as-you-go systems, and considering labor market transformations [4, 21, 46, 43].

## 6.2 Case Studies on Pension Fund Management

The overlapping generations model’s application in pension fund management is illustrated through case studies demonstrating its utility in addressing complex financial and demographic challenges. These studies offer insights into pension fund management strategies’ effectiveness, emphasizing sustainability implications. Research on the New Pension System (NPS) reveals how market risks affect pension corpus growth, influencing retirees’ financial security. Analyzing the relationship between pension fund investments and stock market dynamics in Europe underscores pension funds’

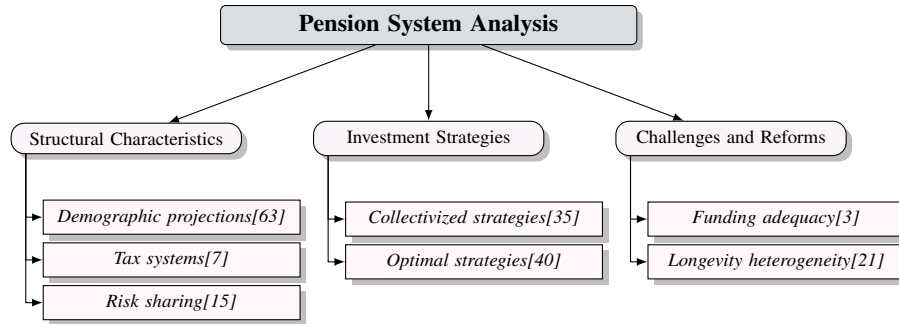


Figure 5: This figure illustrates the key aspects of pension systems, highlighting structural characteristics, investment strategies, and challenges with potential reforms, based on various academic studies.

evolving role as major market players amid an aging population. The impact of financial literacy and trust on retirement planning highlights informed decision-making's importance in enhancing pension fund sustainability [49, 19, 1, 53].

Notable case studies include Ferreira's exploration [39] of using random walks to model pension fund sustainability, emphasizing strategic risk management amid unpredictable market conditions. Das [19] employs Monte Carlo simulations to quantify market risks associated with pension fund sustainability, underscoring the need for robust risk management approaches.

Armstrong's research [35] presents a case study on collectivized pension investment strategies, demonstrating their efficiency and stability compared to traditional methods. Milazzo [40] examines challenges faced by Italian pension funds, contributing to strategic financial planning literature for pension fund sustainability.

These case studies collectively illustrate the overlapping generations model's application in pension fund management, providing valuable insights into effective strategies for addressing financial and demographic challenges. By employing sophisticated modeling techniques and strategic planning, pension fund managers can enhance resilience and sustainability, addressing market risks and ensuring retirees' financial security amid economic and demographic shifts [49, 19, 64].

### 6.3 Impact of Economic Policies and Fiscal Stability

Economic policies significantly influence fiscal stability, particularly when analyzed through the overlapping generations model. Integrating demographic and economic variables is crucial for understanding these policies' effects on fiscal stability and pension systems' sustainability. Inaccurate life expectancy estimates can lead to financial imbalances in pension schemes, necessitating policy adjustments to maintain economic equilibrium [43]. This emphasizes precise demographic forecasting in policy design for long-term pension system viability.

The overlapping generations model highlights the complex relationship between growth and environmental quality, necessitating careful consideration of capital accumulation and environmental policies for sustainable growth [18]. Agent-based modeling provides insights into population dynamics, demonstrating its utility in analyzing aging's implications on public policy and fiscal sustainability [12].

Market risks' impact on fiscal stability is a critical concern. Findings from Das [19] inform policy debates regarding pension guarantees and fiscal responsibilities, emphasizing robust economic policies' necessity to mitigate these risks. Ekeland's study [48] suggests capital taxation as a tool for addressing time inconsistency in overlapping generations, highlighting fiscal policy's importance in maintaining economic stability.

The political dynamics of pension systems, as explored by Bacelar [5], illustrate political factors' importance in economic policy design. Agent-based modeling offers valuable insights into these dynamics, suggesting future research could explore its applicability across countries with varying pension systems, emphasizing adaptable policies for diverse contexts.

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Furthermore, aging's implications on public policy, particularly concerning pensions and fiscal sustainability, are critical research areas [10]. Understanding these dynamics is essential for developing policies that promote fiscal stability and sustainable economic growth. Exploring complex network structures and varying degrees of immunity and influence among agents, as suggested by Golub [13], could enhance the analysis of economic policies and their impact on fiscal stability.

## 7 Conclusion

The overlapping generations model is a critical framework for understanding the complex economic dynamics that occur across different generational cohorts. It effectively addresses key interactions involving social security systems, pension structures, intergenerational transfers, and the life-cycle hypothesis, providing valuable insights into the challenges posed by aging populations and declining birth rates. These demographic shifts present significant risks to fiscal sustainability and intergenerational equity, necessitating strategic policy interventions.

The survey underscores the importance of optimizing pension systems to enhance social welfare. By adjusting contribution rates and increasing the progressivity of benefits, substantial social gains can be achieved, potentially outweighing any behavioral distortions. Additionally, the integration of systematic longevity risk into pension models offers refined strategies tailored to diverse investor profiles and market conditions, paving the way for future research that could deepen our understanding of intergenerational economic dynamics.

Generational accounting is highlighted as a fundamental tool for achieving intergenerational justice, providing a more equitable framework for fiscal sustainability. The survey also points to the economic benefits of tax reforms, such as projected increases in GDP and wages, suggesting further exploration of these policy implications. Investigating the influence of initial conditions on long-term growth outcomes offers additional insights into the economic interactions shaping generational relationships.

This model remains an indispensable resource for policymakers and researchers committed to fostering sustainable and equitable economic systems. By addressing the intricate interplay between demographic trends, economic policies, and social factors, it offers essential guidance for enhancing fiscal stability and intergenerational equity. Future research should focus on incorporating environmental and health dynamics into the model and developing more effective pension fund investment strategies, thereby extending its relevance and utility. Enhancing financial literacy, exploring alternative investment options, and assessing the long-term effects of reforms on pensioners' welfare are also crucial areas for further investigation. These efforts will ensure that the model continues to provide critical insights into the economic challenges and opportunities of the future.

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