General Chemistry I Tutorial 07

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Outline



2 Molecular Orbital Theory



Quiz 7.1

For each of the following valence electron configurations of a homonuclear diatomic molecule or molecular ion, identify the element X or Q, and determine the total bond order.

(a)
$$X_2:(\sigma_{2s})^2,(\sigma_{2s}^*)^2,(\sigma_{2pz})^2,(\pi_{2p})^4,(\pi_{2p}^*)^2$$

(b) $Q_2^-:(\sigma_{2s})^2,(\sigma_{2s}^*)^2,(\pi_{2p})^3$

Quiz 7.2

Compare NO with NO+:

- (a) What are their bond orders?
- (b) Which one has shorter bond length?
- (c) Why do higher bond orders correspond to shorter bond lengths in general?

LCAO

LCAO

If ψ_1 , ψ_2 , ψ_3 ,... are probable states of a microscopic system, linear combination of atomic orbitals(LCAO) is also a probable configuration:

$$\Psi = c_1 \psi_1 + c_2 \psi_2 + c_3 \psi_3 + \dots$$

where c_1 , c_2 , c_3 ... are adjustable coefficients that quantify the contribution of each atomic orbital to the molecular orbital.

Wavefunctions v.s. vectors:

Three-dimensional space: 3 bases span overall space / Every vector can be expressed as a linear combination of 3 bases, e.g.

$$[1,2,3]^{\mathsf{T}} = 1[1,0,0]^{\mathsf{T}} + 2[0,1,0]^{\mathsf{T}} + 3[0,0,1]^{\mathsf{T}}$$

Molecular Orbital Theory

Remark 2.1

Three requirements for effective bonding:

- Compatible orbital symmetries(The most important)
- Approximate atomic orbital energies(Lower energy AOs contributes more to lower energy MOs)
- Maximum orbital overlap(AOs of adjacent atoms contribute to MOs)

Types of bonds:

In this course, we mainly consider two types of bonds: σ bond and π bond.

- σ bond: orbitals that are symmetric to rotation about the line connecting the nuclei(bond axis, we often define z axis to be bond axis).
- π bond: There's a nodal plane containing bond axis. (Whether or not there are nodal planes perpendicular to bond axis doesn't determine if bond is π bond)

Molecular Orbital Theory

Notation of orbitals: $(\sigma_g, \sigma_u^*, \pi_u, \pi_g^*)$

- Bonding, nonbonding, antibonding(,*)
- Centrosymmetric, antisymmetric (g, u)

Remark 2.2

Bond order (B.O.) =
$$\frac{1}{2}$$
 (# bonding electrons – # antibonding electrons)

- Bond length decreases with increasing B.O.
- Bond energy increases with increasing B.O.
- Force constant increases with increasing B.O.(Harmonic oscillator)

Correlation diagram of homonuclear diatomic molecules

- Valence orbitals(Energy, symmetry)
- Linear combination of AOs to make MOs (Energy, symmetry, bonding/antibonding)
- Fill in electrons
- (Calculate bond order)

Correlation Diagram of Homonuclear Diatomic Molecules

Without considering s-p mixing: $\sigma_{2s} < \sigma_{2s}^* < \sigma_{2pz} < \pi_{2px} = \pi_{2py} < \pi_{2px}^* = \pi_{2py}^* < \sigma_{2pz}^*$

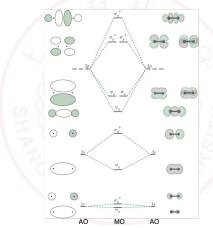


Figure 1: Molecular Orbitals for the First 10 Elements, Assuming Significant Interactions Only between the Valence Atomic Orbitals of Identical Energy.

S-p Mixing

Rev.: AOs have large contribution to MOs only when their energy are fairly close. For the main group elements within the same period, $\Delta E = E_{np} - E_{ns}$ increases with increasing atomic numbers.[Can be estimated through Slater rules]

$$\Psi = c_1 \psi(2s_a) \pm c_2 \psi(2s_b) \pm c_3 \psi(2p_a) \pm c_4 \psi(2p_b)$$

Another way to consider: When two molecular orbitals of the same symmetry mix, the one with higher energy moves still higher in energy, and the one with lower energy moves lower.

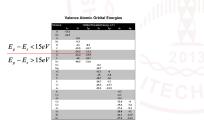


Figure 2: Energy of valence orbitals

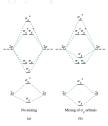


Figure 3: S-p mixing

S-p mixing

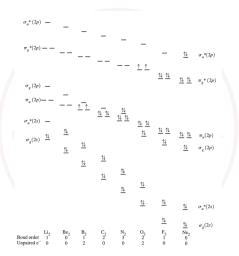


Figure 4: Energy diagram for 2nd period diatomic molecules