

```

In[37]:= M3 = {{-(ℓ c γ) - c Subscript[r, x], c Subscript[r, x]}, 
    {β (1 - ℓ c γ - c Subscript[r, x]), -β + β c Subscript[r, x]}};
M3 // MatrixForm
{val, vec} = Eigensystem[M3];
val[[2]] (* The eigenvalue of M1 *)
{1, vec[[2]][[2]] / vec[[2]][[1]]} (* Corresponding eigenvector *)
Out[38]//MatrixForm=

$$\begin{pmatrix} -c\ell\gamma - cr_x & cr_x \\ \beta(1 - c\ell\gamma - cr_x) & -\beta + c\beta r_x \end{pmatrix}$$

Out[40]=

$$\frac{1}{2} \left( -\beta - c\ell\gamma - cr_x + c\beta r_x + \sqrt{-4c\ell\beta\gamma + (\beta + c\ell\gamma + cr_x - c\beta r_x)^2} \right)$$

Out[41]=
{1,
 - ((2β(-1 + cℓγ + crx)) / (β - cℓγ - crx - cβrx + √(β² - 2cℓβγ + c²ℓ²γ² + 2cβrx - 2cβ²rx + 2c²ℓγrx - 2c²ℓβγrx + c²r²x - 2c²βr²x + c²β²r²x)))}
}

In[42]:= A3 := ℓ c γ + c Subscript[r, x];
B3 := 1 - c Subscript[r, x];
Simplify[val[[2]] - (-A3/2 - (B3 β)/2 + (1/2) Sqrt[(A3 + B3 β)^2 - 4 ℓ c β γ])]
(* Check the form of λ *)
Simplify[vec[[2]] - ({(1/(2(1-A3)))*
    (-A3 + B3 β + Sqrt[(A3 - B3 β)^2 + 4 c Subscript[r, x] β (1 - A3)]), 1}
    (* Check the form of corresponding eigenvector. *))
]
Out[44]=
0
Out[45]=
{0, 0}

```