MAE 259B Group 2 Progress Report

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What we did - Starting point

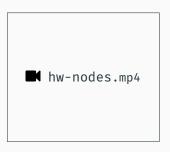
Start from the homework code

Adapted from the MATLAB sample code, translated into Python, with minor changes and optimizations.

Build utilities

Command line interface, 3D visualization tool, code snapshot tool, etc..





Not all PDF viewers can play videos. If not playable here, the videos can be found at https://github.com/kmxz/mae259b-project/tree/master/mid-presentation/video.

What we did - Performance optimization

Profiling shows 90% of time is spent on calculating F and J.

```
def gradEbAndHessEb(xkml, ykml, xk, yk, xkpl, ykpl, ok0):
       itm1 = 2 * tan(0.5 * \omega k0)
       itm2 = ((-xk + xkp1) * (xk - xkm1) + (-yk + ykp1) * (yk - ykm1))
       itm3 = ((-xk + xkp1) * (vk - vkm1) - (xk - xkm1) * (-vk + vkp1))
       itm4 = itm3 / itm2 ** 2
                                                                                                                                                                                       30.6 \, s
       itm5 = tan(0.5 * atan(itm3 / itm2))
       itm6 = (1 + itm3 ** 2 / itm2 ** 2)
       itm7 = ((ykm1 - ykp1) / itm2 + itm3 * (2 * xk - xkm1 - xkp1) / itm2 ** 2)
       itm8 = ((-xkm1 + xkp1) / itm2 + itm3 * (2 * vk - vkm1 - vkp1) / itm2 ** 2)
       itm9 = ((-xk + xkm1) / itm2 + (-yk + ykm1) * itm4)
       itm10 = ((-xk + xkm1) * itm4 + (vk - vkm1) / itm2)
       itml1 = (-itm1 + 2 * itm5) * (itm5 ** 2 + 1) * itm5 / itm6 ** 2
       itm12 = (-itm1 + 2 * itm5) * (itm5 ** 2 + 1) / itm6
                                                                                                                                                                                          7.6s
       itm13 = itm12 / itm6
       itm14 = itm3 ** 2 / itm2 ** 3
                                                                                                                                                                                4x faster
       F = np.empty(6)
       F[0] = 2 * ((-xk + xkp1) * itm4 + (-vk + vkp1) / itm2) * itm12
       F[1] = 2 * ((xk - xkp1) / itm2 + (-yk + ykp1) * itm4) * itm12
       F[2] = 2 * itm7 * itm12
       F[3] = 2 * itm8 * itm12
       F[4] = 2 * itm10 * itm12
       F[5] = 2 * itm9 * itm12
       J11 = 2 * ((-2 * xk + 2 * xkp1) * (-xk + xkp1) * itm3 / itm2 ** 3 + 2 * (-xk + xkp1) * (-yk + 
  vkp1) / itm2 ** 2) * itm12 + 2 * (-(-2 * xk + 2 * xkp1) * itm14 - (-2 * vk + 2 * vkp1) * itm4) *
   ((-xk + xkp1) * itm4 + (-vk + vkp1) / itm2) * itm13 + 2 * ((-xk + xkp1) * itm4 + (-vk + vkp1) /
  itm2) ** 2 * itm11 + 2 * ((-xk + xkp1) * itm4 + (-yk + ykp1) / itm2) ** 2 * (itm5 ** 2 + 1) ** 2
  / itm6 ** 2
       J12 = 2 * (-itm1 + 2 * itm5) * (itm5 ** 2 + 1) * ((-xk + xkp1) * (xk - xkp1) / itm2 ** 2 + 1)
   (-xk + xkpl) * (-2 * yk + 2 * ykpl) * itm3 / itm2 ** 3 + (-yk + ykpl) ** 2 / itm2 ** 2) / itm6 +
  2 * ((xk - xkpl) / itm2 + (-yk + ykpl) * itm4) * ((-xk + xkpl) * itm4 + (-yk + ykpl) / itm2) *
  itml1 + 2 * ((xk - xkpl) / itm2 + (-yk + ykpl) * itm4) * ((-xk + xkpl) * itm4 + (-yk + ykpl) /
  itm2) * (itm5 ** 2 + 1) ** 2 / itm6 ** 2 + 2 * ((-xk + xkp1) * itm4 + (-vk + ykp1) / itm2) *
  (-(2 * xk - 2 * xkp1) * itm4 - (-2 * yk + 2 * ykp1) * itm14) * itm13
       J13 = 2 * (-itm1 + 2 * itm5) * (itm5 ** 2 + 1) * ((-xk + xkp1) * (ykm1 - ykp1) / itm2 ** 2 + 1)
   (-xk + xkp1) * itm3 * (4 * xk - 2 * xkm1 - 2 * xkp1) / itm2 ** 3 + (-yk + ykp1) * (2 * xk - xkm1
```

- xkp1) / itm2 ** 2 - itm4) / itm6 + 2 * itm7 * ((-xk + xkp1) * itm4 + (-vk + vkp1) / itm2) *

What we did - Natural curvature

When calculating bending energy, replace $\frac{1}{2}EI(\phi_k)^2$ with $\frac{1}{2}EI(\phi_k-\phi_{k0})^2$.

The formulas for calculating *F* and *J* need to be changed (do differentiation again).

To verify the result:

- Expect same result as previous code when ϕ_0 = 0;
- Expect a straight beam to recover natural curvature when no external force applied.

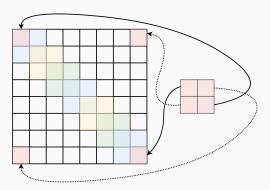
```
from sympy import symbols, diff, tan, atan
def Φκ(Xkm, Xk, Xkp, Ykm, Yk, Ykp):
     return atan(((x_{kp} - x_k) * (y_k - y_{km})
  -(x_k - x_{km}) * (y_{kp} - y_k)) / ((x_{kp} - y_k))
  (x_k) * (x_k - x_{km}) + (y_{kp} - y_k) * (y_k - y_k)
  V k m ) ) )
def Eb_k(x_{km}, x_k, x_{kp}, y_{km}, y_k, y_{kp}, \phi_{ko}):
     return (2 * tan(\phi_k(x_{km}, x_k, x_{kp})
  v_{km}, v_k, v_{kp}) / 2.0) - 2 * tan(\phi_{ko} /
  2.0)) ** 2
X_{km}, X_k, X_{kp}, Y_{km}, Y_k, Y_{kp}, \phi_{ko} =
  symbols('xkm1 xk xkp1 ykm1 yk ykp1 \ok0')
Eb = Eb_k(x_{km}, x_k, x_{kp}, y_{km}, y_k, y_{kp}, \phi_{ko})
F1 = diff(Eb, x_{km})
F2 = diff(Eb, y_{km})
F3 = diff(Eb, x_k)
F4 = diff(Eb, v_k)
F5 = diff(Eb, x_{kp})
F6 = diff(Eb, v_{kp})
J11 = diff(F1, x_{km})
J12 = diff(F1, y_{km})
J13 = diff(F1, x_k)
J14 = diff(F1. v_k)
J15 = diff(F1, x_{kn})
```

What we did - Circular structure

Instead of nv - 1 edges, we have nv edges.

For bending, instead of nv-2 components, we have nv components. For stretching, instead of nv-1 components, we have nv components.

When assembling the Jacobians, new components added to connect two ends together:



What we did - Circular structure

Verify our code by running the "hanging circle":

What we did - Inflation pressure



With \underline{x}_k and \underline{x}_{k+1} , we can easily calculate force exerted on those two points.

As force is dependent on actual positions of nodes, we need to add the variation into the Jabobian matrix. We simply take derivatives on the forces.

What we did - Surface contact

Predictor-corrector method is used.

Assume a surface at y = 0, When doing time-marching, on each time step :

- 1. Compute q(t) as before;
- 2. Check if there exists any node whose y < 0. If there is any, set it as a temporarily constrained DOF with y = 0, and recompute current frame;
- 3. Check if there exists any temporarily constrained DOF, such that the normal *force* between the surface and the node is negative. Remove such temporary constraint, and recompute current frame.

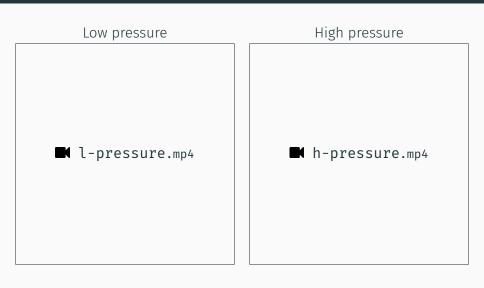
```
Fb, Jb = getFb(qCurrentIterate, EI, nv, voronoiRefLen, -2 * pi / nv, isCircular=True)
Fs, Js = getFs(qCurrentIterate, EA, nv, refLen, isCircular=True)
Fg = m * garr
Fp, Jp = getFp(qCurrentIterate, nv, refLen, InflationPressure)
Forces = Fb + Fs + Fg + Fp
# Equation of motion
f = m * (qCurrentIterate - q0) / dt ** 2 - m * u / dt - Forces
fUncons = dofHelper.unconstrained_v(f)
```

What we did - Surface contact

In each frame:

```
gNew, reactionForces = objfun(g0)
      # inspect reactionForces to see if any one is negative, which should be UNCONSTRAINED
      needToFree = [unconsInd for unconsInd in dofHelper. constrained if (reactionForces[
unconsInd1 < 0)1
      if needToFree:
          dofHelper.unconstraint(needToFree)
          print('Contact condition updated. Remove constraints and recompute')
          gNew, reactionForces = obifun(g0)
      # inspect qNew to see if any one falls below ground, which should be CONSTRAINED
      while True:
          a0Effective = None
          for c in range(nv):
              index = 2 * c + 1
              if aNew[index] < 0: # v < 0: bad!
                  if gOEffective is None:
                      q0Effective = q0.copy()
                  g0Effective[index] = 0
                  dofHelper.constraint([index])
          if q0Effective is None:
              break
          else:
              print('Contact condition violated. Add constraints and recompute')
              qNew, reactionForces = objfun(q0Effective)
```

Objective completed!



What we did - Damping

Without damping, we have oscillations.

Naïve damping $\underline{F}_{d,k} \propto -\underline{v}_k$ ruins bulk motion (as our bulk velocity is high)

So we use velocity relative to center of mass:

$$\underline{F}_{d,k} \propto -(\underline{v}_k - \underline{v}_{cm})$$



Problem: Shape Jitter



- Step size too large, everything bashed to ground before reacting
- · No self-intersection detection

Project on GitHub now!

All code, results (and these slides) uploaded to

https://github.com/kmxz/mae259b-project

