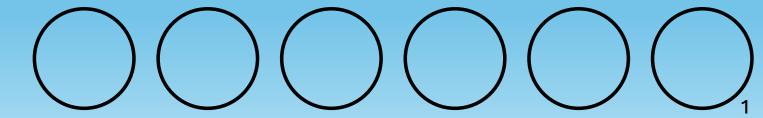
Mens Erger Je Niet with a quantum twist

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Introduction **The Game Performing** Quantum Running the the Bell test in phenomena game **Demos** game

Introduction

Goal of the project

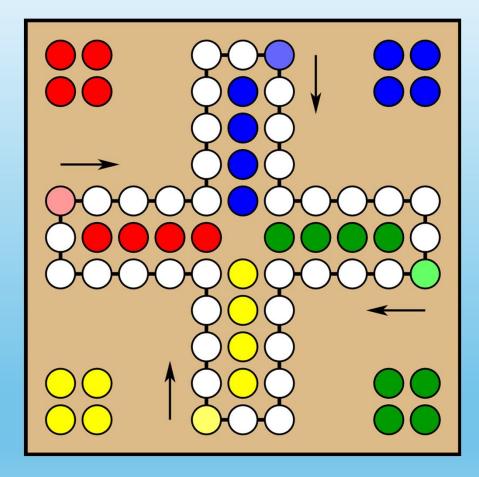
Introduction

- Quantum chess
- Quantum minesweeper
- Quantum tic-tac-toe

Christopher Cantwell. Quantum Chess: Developing a Mathematical Framework and Design Methodology for Creating Quantum Games. 2019. arXiv: 1906.05836 [quant-ph]. Url: https://arxiv.org/abs/1906.0583

Allan Goff. "Quantum tic-tac-toe: A teaching metaphor for superposition in quantum mechanics". In: American Journal of Physics 74.11 (Nov.2006), pp. 962–973. issn: 0002-9505. doi: 10.1119/1.2213635. eprint: https://pubs.aip.org/aapt/aip/article-pdf/74/11/962/13128226/962_1_online.pdf. url: https://doi.org/10.1119/1.2213635. Michal Gordon and Goren Gordon. "Quantum computer games: Quantum minesweeper". In: Physics Education 45 (June 2010), p. 372. doi:10.1088/0031-9120/45/4/008.

Introduction

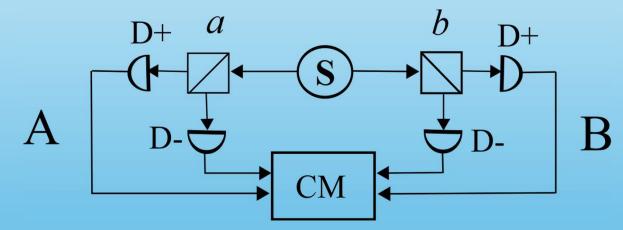


Source: Mens erger je niet! -Wikipedia

Quantum phenomena

Quantum elements

- Superposition
- Entanglement
- Measurement
- Phase
- Interference



- $|0\rangle \rightarrow -1$ $|1\rangle \rightarrow +1$

Quantum phenomena

Bell test (classical)

$$S = \langle A_1 \otimes B_1 \rangle - \langle A_1 \otimes B_2 \rangle + \langle A_2 \otimes B_1 \rangle + \langle A_2 \otimes B_2 \rangle$$

$$S = A_1(B_1 - B_2) + A_2(B_1 + B_2)$$

Local realism

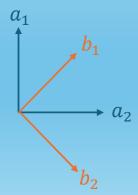
Classically: $|S| \leq 2$

Quantum phenomena

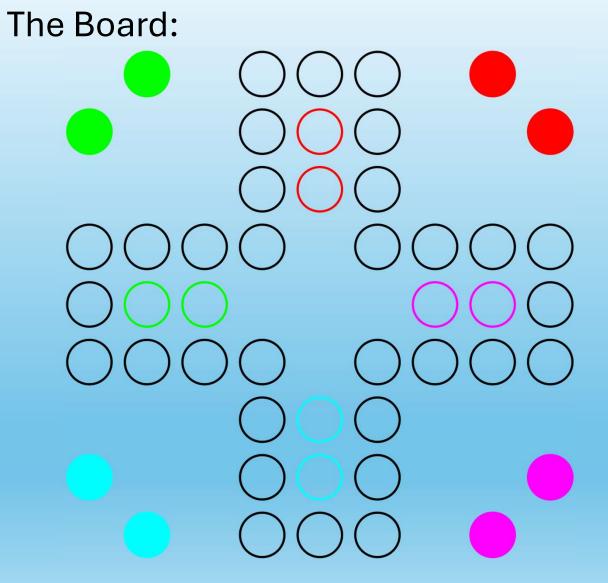
Bell test

$$S = \langle A_1 \otimes B_1 \rangle - \langle A_1 \otimes B_2 \rangle + \langle A_2 \otimes B_1 \rangle + \langle A_2 \otimes B_2 \rangle$$
$$|\Psi^-\rangle = \frac{1}{\sqrt{2}}(|10\rangle - |01\rangle$$
$$\langle A_1 \otimes B_2 \rangle = 1/\sqrt{2}$$
$$\langle A_1 \otimes B_1 \rangle = \langle A_2 \otimes B_1 \rangle = \langle A_2 \otimes B_2 \rangle = -1/\sqrt{2}$$

In quantum mechanics: $|S| \le 2\sqrt{2}$

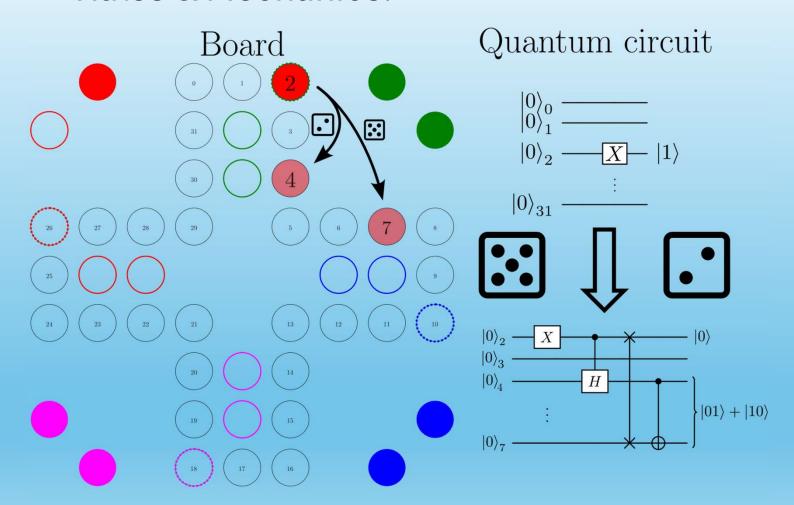


- The Game



The Game

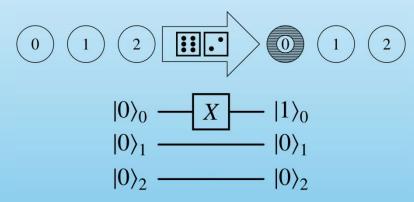
Rules & Mechanics:



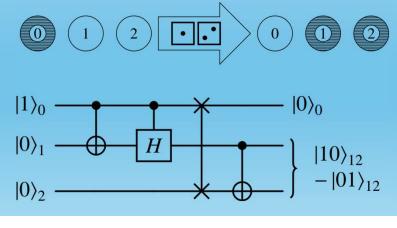
The Game

Rules & Mechanics:

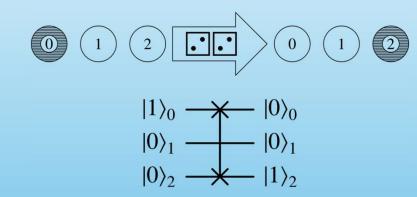
Placing a pawn:



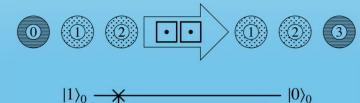
Superposition play:

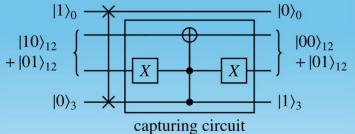


Moving a pawn



Capturing a pawn:





Rules & Mechanics:

The Game

- No double occupancy
- Capturing moves the capturer one further, also leads to entanglement
- Measurement:
 - 20 Pawns are on the board ⇒ Z basis
 - Pawn reaches winning spot ⇒ different basis

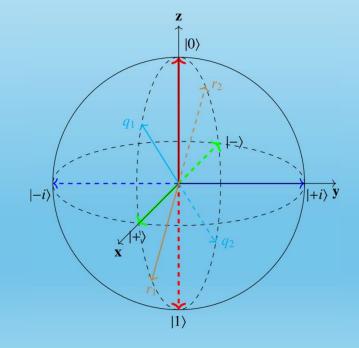
The Game

Rules & Mechanics:

Q-basis: The diagonal between the Z-basis' $|0\rangle$ state and the X-basis' $|+\rangle$ state.

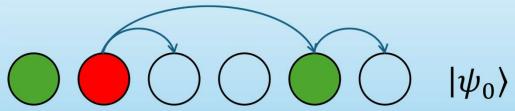
R-basis: The diagonal between the X-basis' $|-\rangle$ state and the Z-basis' $|1\rangle$ state.

Pawn\Basis	Z	Q	X	R
Red 1	R	G	В	P
Red 2	R	P	В	G
Blue 1	В	P	R	G
Blue 2	В	G	R	P
Green 1	G	R	P	В
Green 2	G	В	P	R
Purple 1	P	В	G	R
Purple 2	P	R	G	В



Performing the Bell test in game

Creating the Singlet state



$$|\psi_0\rangle = |110010\rangle$$

$$|\psi_1\rangle = |101010\rangle - |100001\rangle$$

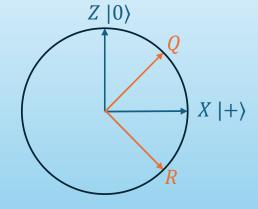
$$|\psi_2\rangle = |000110\rangle - |000101\rangle$$
$$= |0001\rangle \otimes (|10\rangle - |01\rangle)$$

Performing the Bell test in game

Mapping the axes

Trigger

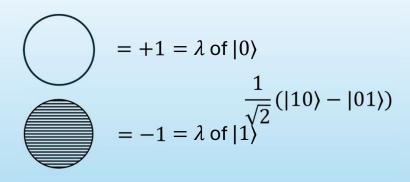
Pawn\Basis	Z	Q	X	R
Red 1	R	G	В	P
Red 2	R	P	В	G
Blue 1	В	P	R	G
Blue 2	В	G	R	P
Green 1	G	R	P	В
Green 2	G	В	P	R
Purple 1	P	В	G	R
Purple 2	P	R	G	В



Red = Alice Green = Bob

Performing the Bell test in game

Mapping the outcomes



Performing the Bell test in game

Trigger

Bringing it all together

$$S = \langle A_1 \otimes B_1 \rangle - \langle A_1 \otimes B_2 \rangle + \langle A_2 \otimes B_1 \rangle + \langle A_2 \otimes B_2 \rangle$$

$$Average \qquad Average \qquad Average \qquad Average$$

$$Outcome \qquad +1 \quad -1 \quad +1 \quad -1$$

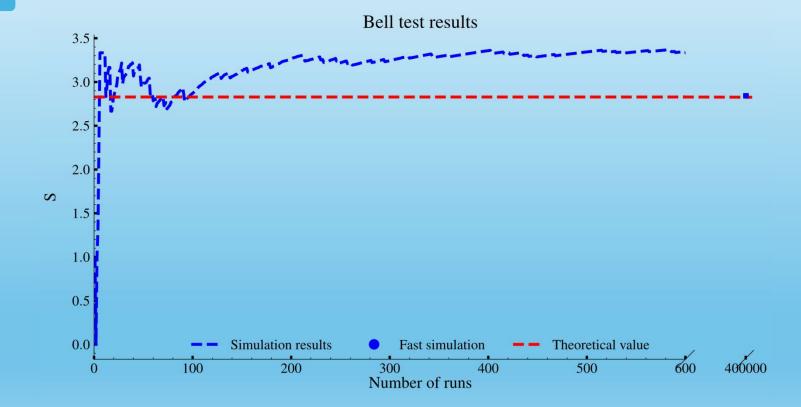
$$(random)$$

$$Trigger \qquad R1 \quad R1 \quad P1 \quad P1 \quad R2 \quad R2 \quad G2 \quad G2 \quad B1 \quad B1 \quad G1 \quad G1 \quad B2 \quad B2 \quad P2 \quad P2$$

$$(random)$$

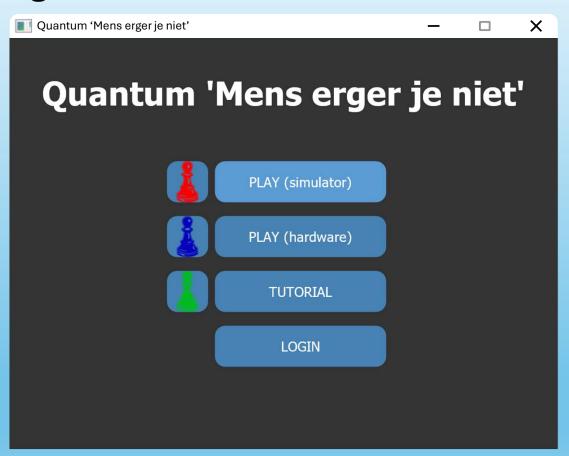
Performing the Bell test in game

Results



Running
the game
Demos

The game



Q&A