

22. Oktober 2018

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In [1]: %matplotlib inline
import matplotlib.pyplot as plt
import numpy as np

#Messwerte aus Tabelle 1: U_m über f
f = np.array([2.96,6.02,9.01,11.8,14.7])
fehler_f = np.array([0.05,0.05,0.05,0.01,0.01])

U_m = np.array([0.9,1.8,2.9,3.7,4.6])
fehler_U_m = np.array([0.1,0.1,0.1,0.1,0.1])

U_pp = 2*U_m
fehler_U_pp = 2*fehler_U_m

#Fitfunktion
from scipy import odr

def fit_func(p, x):
    (a, b) = p
    return a*x+b

model = odr.Model(fit_func)

#darzustellende Daten
x = f
y = U_pp
delta_x = fehler_f
delta_y = fehler_U_pp

#Startparameter
para0 = [1.0, 1.0]

data = odr.RealData(x, y, sx=delta_x, sy=delta_y)
odr = odr.ODR(data, model, beta0=para0)
out = odr.run()

#1-Sigma
popt = out.beta
perr = out.sd_beta

#Sigma-Umgebung
nstd = 1 # um n-Sigma-Umgebung zu zeichnen
popt_top = popt+nstd * perr
popt_bot = popt - nstd * perr

#Plot-Umgebung
x_fit = np.linspace(min(x)-1, max(x)+1, 100)
fit = fit_func(popt, x_fit)
fit_top = fit_func(popt_top, x_fit)
fit_bot = fit_func(popt_bot, x_fit)

#Plot
fig, ax = plt.subplots(1)
plt.errorbar(x, y, yerr=delta_y, xerr=delta_x, lw=1, ecolor='k', fmt='none', capsize=1, label='Messdaten')
plt.title('Diagramm 1: ' + r'$U_{pp}$' + ' als Funktion von ' + r'$\omega$')
plt.grid(True)
plt.xlabel('Frequenz ' + r'$\omega$' + ' ' + r'$[Hz]$')
plt.ylabel('Induktionsspannung ' + r'$U_{pp}$' + ' ' + r'$[V]$')
plt.plot(x_fit, fit, 'r', lw=1, label='Fit')
ax.fill_between(x_fit, fit_top, fit_bot, alpha=.25, label=str(nstd)+r'$\sigma$'+'-Umgebung')
plt.legend(loc='best')

#Chi-Quadrat orthogonal
from scipy.stats import chi2

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dof = x.size-popt.size
chisquare = np.sum(((fit_func([*popt], x)-y)**2)/(delta_y**2+((fit_func([*popt], x+delta_x)-fit_func([*popt], x-delta_x))/2)**2))
chisquare_red = chisquare/dof
prob = round(1-chi2.cdf(chisquare,dof),2)*100

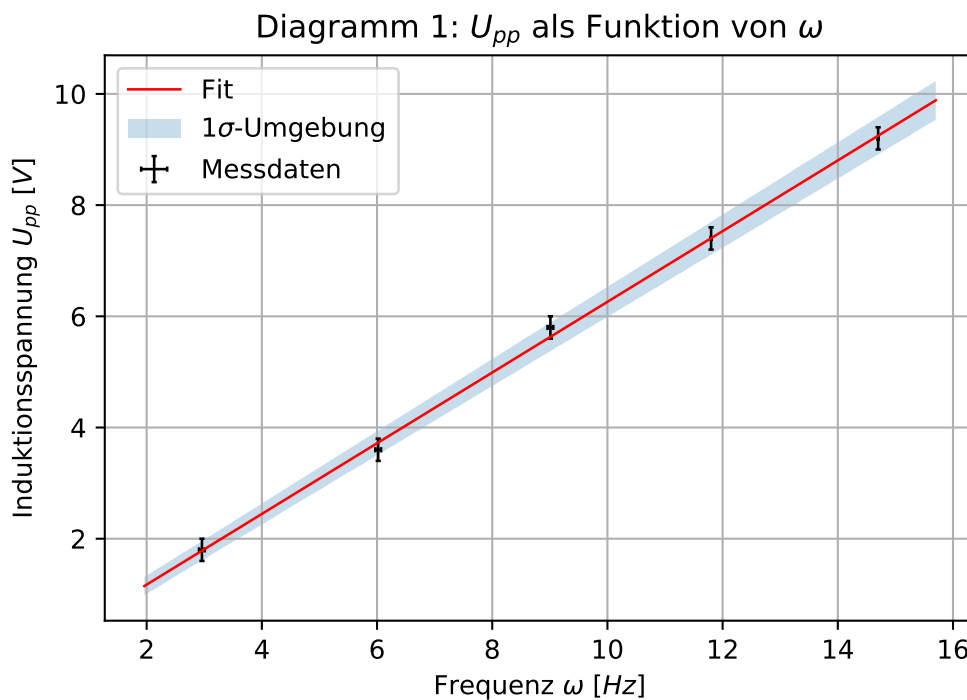
#Grenzfrequenz berechnen
f_g = 1/np.tan(45*np.pi/180)

#Output
plt.savefig('figures/245_Diagramm1.pdf', format='pdf')
print('Steigung [V/Hz] = ', popt[0], ', Standardfehler = ', perr[0])
print('Nullspannung [V] = ', popt[1], ', Standardfehler = ', perr[1])
print('\n')
print('Chi-Quadrat = ', chisquare)
print('Freiheitsgrade = ', dof)
print('Chi-Quadrat reduziert = ', chisquare_red)
print('Wahrscheinlichkeit ein größeres oder gleiches Chi-Quadrat zu erhalten = '+str(prob)+'%')

Steigung [V/Hz] = 0.6357796560256483 , Standardfehler = 0.013607457052426549
Nullspannung [V] = -0.09742579478819292 , Standardfehler = 0.1340837992595958

Chi-Quadrat = 1.1740097348326421
Freiheitsgrade = 3
Chi-Quadrat reduziert = 0.39133657827754736
Wahrscheinlichkeit ein größeres oder gleiches Chi-Quadrat zu erhalten = 76.0%

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In [2]: %matplotlib inline
import matplotlib.pyplot as plt
import numpy as np

#Messwerte aus Tabelle 2:  $U_m$  über  $I_{HH}$ 
I_HH = np.array([0.50, 1.00, 1.50, 2.00, 2.50, 3.00, 3.50, 4.00, 4.50])
fehler_I_HH = np.array([0.05, 0.05, 0.05, 0.05, 0.05, 0.05, 0.05, 0.05, 0.05])

U_m = np.array([0.46, 0.76, 1.15, 1.44, 1.75, 2.1, 2.4, 2.9, 3.36])
fehler_U_m = np.array([0.01, 0.01, 0.02, 0.04, 0.05, 0.1, 0.1, 0.1, 0.1])

U_pp = 2*U_m

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fehler_U_pp = 2*fehler_U_m

#Fitfunktion
from scipy import odr

def fit_func(p, x):
    (a, b) = p
    return a*x+b

model = odr.Model(fit_func)

#darzustellende Daten
x = I_HH
y = U_pp
delta_x = fehler_I_HH
delta_y = fehler_U_pp

#Startparameter
para0 = [1.0, 1.0]

data = odr.RealData(x, y, sx=delta_x, sy=delta_y)
odr = odr.ODR(data, model, beta0=para0)
out = odr.run()

#1-Sigma
popt = out.beta
perr = out.sd_beta

#Sigma-Umgebung
nstd = 1 # um n-Sigma-Umgebung zu zeichnen
popt_top = popt+nstd*perr
popt_bot = popt-nstd*perr

#Plot-Umgebung
x_fit = np.linspace(min(x)-1, max(x)+1, 100)
fit = fit_func(popt, x_fit)
fit_top = fit_func(popt_top, x_fit)
fit_bot = fit_func(popt_bot, x_fit)

#Plot
fig, ax = plt.subplots(1)
plt.errorbar(x, y, yerr=delta_y, xerr=delta_x, lw=1, ecolor='k', fmt='none', capsize=1, label='Messdaten')
plt.title('Diagramm 2: ' + r'$U_{pp}$' + ' als Funktion von ' + r'$I_{HH}$')
plt.grid(True)
plt.xlabel('Spulenstrom ' + r'$I_{HH}$' + ' ' + r'$[A]$')
plt.ylabel('Induktionsspannung ' + r'$U_{pp}$' + ' ' + r'$[V]$')
plt.plot(x_fit, fit, 'r', lw=1, label='Fit')
ax.fill_between(x_fit, fit_top, fit_bot, alpha=.25, label=str(nstd)+r'$\sigma$'-Umgebung')
plt.legend(loc='best')

#Chi-Quadrat orthogonal
from scipy.stats import chi2

dof = x.size-popt.size
chisquare = np.sum(((fit_func([*popt], x)-y)**2)/(delta_y**2+((fit_func([*popt], x+delta_x)-fit_func([*popt], x-delta_x))/2)**2))
chisquare_red = chisquare/dof
prob = round(1-chi2.cdf(chisquare,dof),2)*100

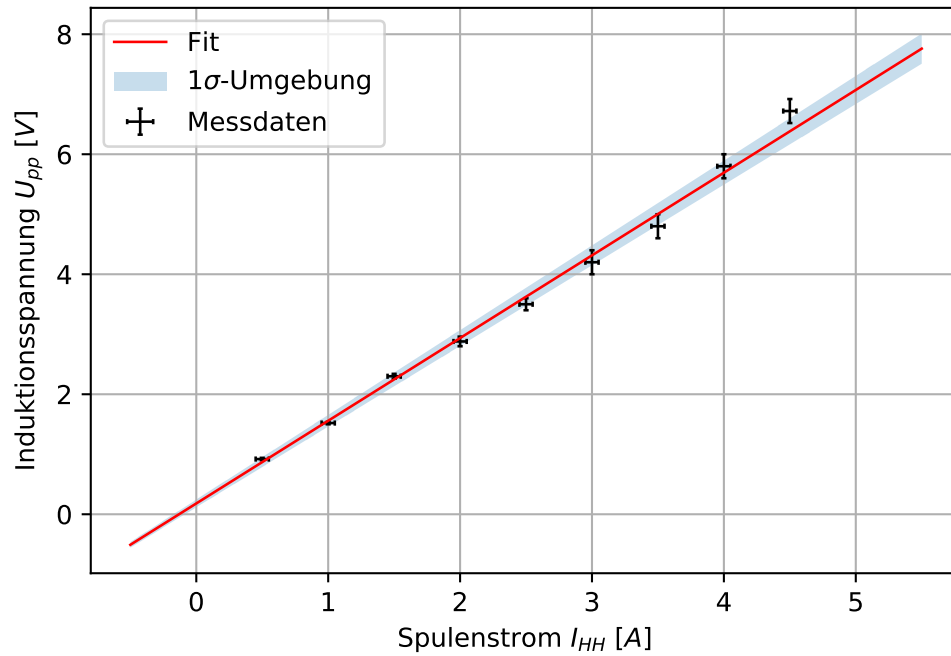
#Output
plt.savefig('figures/245_Diagramm2.pdf', format='pdf')
print('Steigung [V/A] = ', popt[0], ' ', Standardfehler = ', perr[0])
print('Nullspannung [V] = ', popt[1], ' ', Standardfehler = ', perr[1])
print('\n')
print('Chi-Quadrat = ', chisquare)
print('Freiheitsgrade = ', dof)
print('Chi-Quadrat reduziert = ', chisquare_red)
print('Wahrscheinlichkeit ein größeres oder gleiches Chi-Quadrat zu erhalten = '+str(prob)+'%')

Steigung [V/A] = 1.3780803393226733 , Standardfehler = 0.03431204247559972
Nullspannung [V] = 0.1802311865872918 , Standardfehler = 0.06287338789282541

Chi-Quadrat = 6.6094148490961215
Freiheitsgrade = 7
Chi-Quadrat reduziert = 0.9442021212994459
Wahrscheinlichkeit ein größeres oder gleiches Chi-Quadrat zu erhalten = 47.0%

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Diagramm 2: U_{pp} als Funktion von I_{HH}



```
In [3]: %matplotlib inline
import matplotlib.pyplot as plt
import numpy as np

#Messwerte aus Tabelle 3:  $U_m$  über  $\alpha$ 
alpha=np.array([0,30,60,90,120,150,180,210,240,270,300,330])
fehler_alpha=np.array([3,3,3,3,3,3,3,3,3,3,3,3])

U_m=np.array([4.64,4.16,2.48,-0.23,-2.70,-4.24,-4.88,-4.24,-2.60,-0.20,2.12,3.88])
fehler_U_m=np.array([0.05,0.05,0.05,0.05,0.05,0.05,0.05,0.05,0.05,0.05,0.05,0.05])

#Fitfunktion
from scipy import odr

def fit_func(p, x):
    (a, b, c) = p
    return a*np.cos((x+b)*np.pi/180)+c

model = odr.Model(fit_func)

#darzustellende Daten
x = alpha
y = U_m
delta_x = fehler_alpha
delta_y = fehler_U_m

#Startparameter
para0 = [1.0, 1.0, 1.0]

data = odr.RealData(x, y, sx=delta_x, sy=delta_y)
odr = odr.ODR(data, model, beta0=para0)
out = odr.run()

#1-Sigma
popt = out.beta
perr = out.sd_beta

#Sigma-Umgebung
nstd = 4 # um n-Sigma-Umgebung zu zeichnen
popt_top = popt+nstd*perr
popt_bot = popt-nstd*perr
```

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#Plot-Umgebung
x_fit = np.linspace(min(x)-10, max(x)+10, 100)
fit = fit_func(popt, x_fit)
fit_top = fit_func(popt_top, x_fit)
fit_bot = fit_func(popt_bot, x_fit)

#Plot
fig, ax = plt.subplots(1)
plt.errorbar(x, y, yerr=delta_y, xerr=delta_x, lw= 1, ecolor='k', fmt='none', capsize=1, label='Messdaten')
plt.title('Diagramm 3: ' + r'$U_m$' + ' als Funktion von ' + r'$\alpha$')
plt.grid(True)
plt.xlabel('Drehwinkel ' + r'$\alpha$' + ' ' + r'$[^\circ]$')
plt.ylabel('Induktionsspannung ' + r'$U_m$' + ' ' + r'$[V]$')
plt.plot(x_fit, fit, 'r', lw=1, label='Fit')
ax.fill_between(x_fit, fit_top, fit_bot, alpha=.25, label=str(nstd)+r'$\sigma$'+'-Umgebung')
plt.legend(loc='best')

#Chi-Quadrat orthogonal
from scipy.stats import chi2

dof = x.size-popt.size
chisquare = np.sum(((fit_func([*popt], x)-y)**2)/(delta_y**2+((fit_func([*popt], x+delta_x)-fit_func([*popt], x-delta_x))/2)**2))
chisquare_red = chisquare/dof
prob = round(1-chi2.cdf(chisquare,dof),2)*100

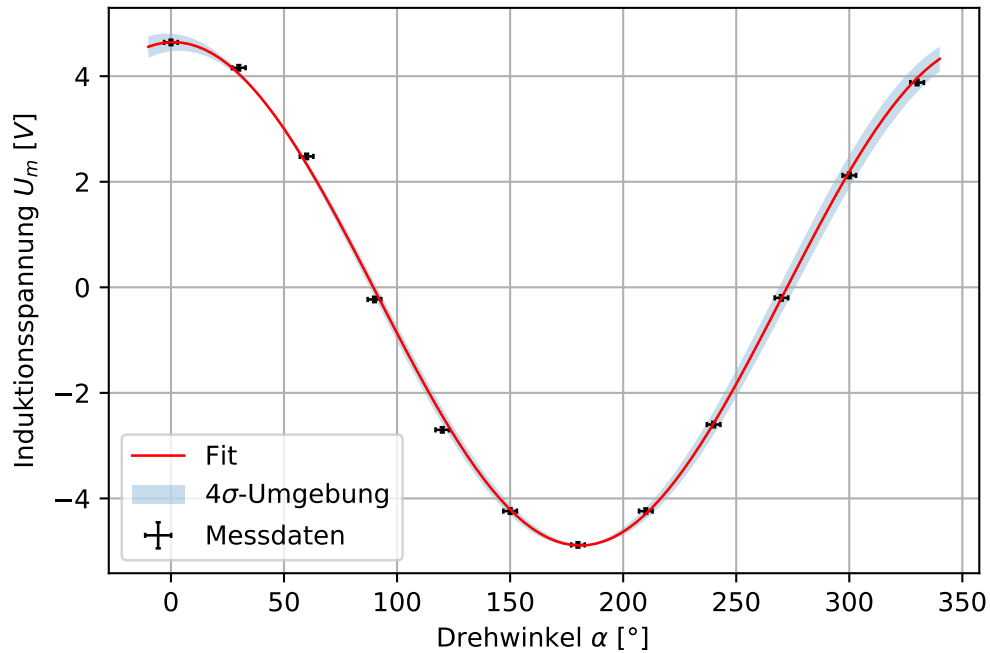
#Output
plt.savefig('figures/245_Diagramm3.pdf', format='pdf')
print('Amplitude [V] = ', popt[0], ', Standardfehler = ', perr[0])
print('Ausgangswinkel [^\circ] = ', popt[1], ', Standardfehler = ', perr[1])
print('Untergrundspannung [V] = ', popt[2], ', Standardfehler = ', perr[2])
print('\n')
print('Chi-Quadrat = ', chisquare)
print('Freiheitsgrade = ', dof)
print('Chi-Quadrat reduziert = ', chisquare_red)
print('Wahrscheinlichkeit ein grÖßeres oder gleiches Chi-Quadrat zu erhalten = '+str(prob)+'%')

Amplitude [V] = 4.768431216467123 , Standardfehler = 0.021186837768468563
Ausgangswinkel [^\circ] = -0.981911428502888 , Standardfehler = 0.6588325317219716
Untergrundspannung [V] = -0.1231631314674312 , Standardfehler = 0.01975967706206923

Chi-Quadrat = 3.892776040875202
Freiheitsgrade = 9
Chi-Quadrat reduziert = 0.43253067120835575
Wahrscheinlichkeit ein grÖßeres oder gleiches Chi-Quadrat zu erhalten = 92.0%

```

Diagramm 3: U_m als Funktion von α



```
In [4]: %matplotlib inline
import matplotlib.pyplot as plt
import numpy as np

#Messwerte aus Tabelle 4: U_HH und U_ind über f
f=np.array([20.0,40.0,60.0,80,100,120,140,160,180,200,400,600,800,1000,1200,1400,1600,1800,2000])
fehler_f=np.array([0.1,0.1,0.4,0.4,1,1,1,1,1,1,2,2,5,5,5,5,5,5,5])

U_ind=np.array([3.32,4.20,4.42,4.54,4.58,4.60,4.62,4.64,4.64,4.62,4.62,4.62,4.62,4.62,4.62,4.62,4.66,4.68,4.70])
fehler_U_ind=np.array([0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02])

U_HH=np.array([7.00,7.08,7.08,7.02,7.02,6.98,6.96,6.90,6.94,6.94,6.96,6.88,6.86,6.86,6.86,6.86,6.88,6.86,6.86])
fehler_U_HH=np.array([0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02])

r=U_ind/U_HH
fehler_r=np.sqrt((fehler_U_HH/U_HH)**2+(fehler_U_ind/U_ind)**2)*r

#Fitfunktion
from scipy import odr

def fit_func(p, x):
    (a, b, c) = p
    return (a**2+(b*x)**2)/(1+(c/x)**2)

model = odr.Model(fit_func)

#darzustellende Daten
x = f
y = r
delta_x = fehler_f
delta_y = fehler_r

#Startparameter
para0 = [1.0, 1.0, 1.0]

data = odr.RealData(x, y, sx=delta_x, sy=delta_y)
odr = odr.ODR(data, model, beta0=para0)
out = odr.run()

#1-Sigma
popt = out.beta
```

```

perr = out.sd_beta

#Sigma-Umgebung
nstd = 4 #um n-Sigma-Umgebung zu zeichnen
popt_top = popt+nstd*perr
popt_bot = popt-nstd*perr

#Plot-Umgebung
x_fit = np.linspace(min(x)/2, max(x)*2, 1000)
fit = fit_func(popt, x_fit)
fit_top = fit_func(popt_top, x_fit)
fit_bot = fit_func(popt_bot, x_fit)

#Plot
fig, ax = plt.subplots(1)
plt.errorbar(x, y, yerr=delta_y, xerr=delta_x, lw= 1, ecolor='k', fmt='none', capsize=1, label='Messdaten')
plt.title('Diagramm 4: ' + r'$U_{ind}$ / $U_{HH}$' + ' als Funktion von ' + r'$\omega$')
plt.grid(True)
plt.xscale('log')
plt.xlabel('Frequenz ' + r'$\omega$' + ' ' + r'$[Hz]$')
plt.ylabel('Verhältnis ' + r'$U_{ind}$ / $U_{HH}$' + ' ' + r'$\{ \}$')
plt.plot(x_fit, fit, 'r', lw=1, label='Fit')
ax.fill_between(x_fit, fit_top, fit_bot, alpha=.25, label=str(nstd)+r'$\sigma$'-Umgebung')
plt.legend(loc='best')

#Chi-Quadrat orthogonal
from scipy.stats import chi2

dof = x.size-popt.size
chisquare = np.sum(((fit_func([*popt], x)-y)**2)/(delta_y**2+((fit_func([*popt], x+delta_x)-fit_func([*popt], x-delta_x))/2)**2))
chisquare_red = chisquare/dof
prob = round(1-chi2.cdf(chisquare,dof),2)*100

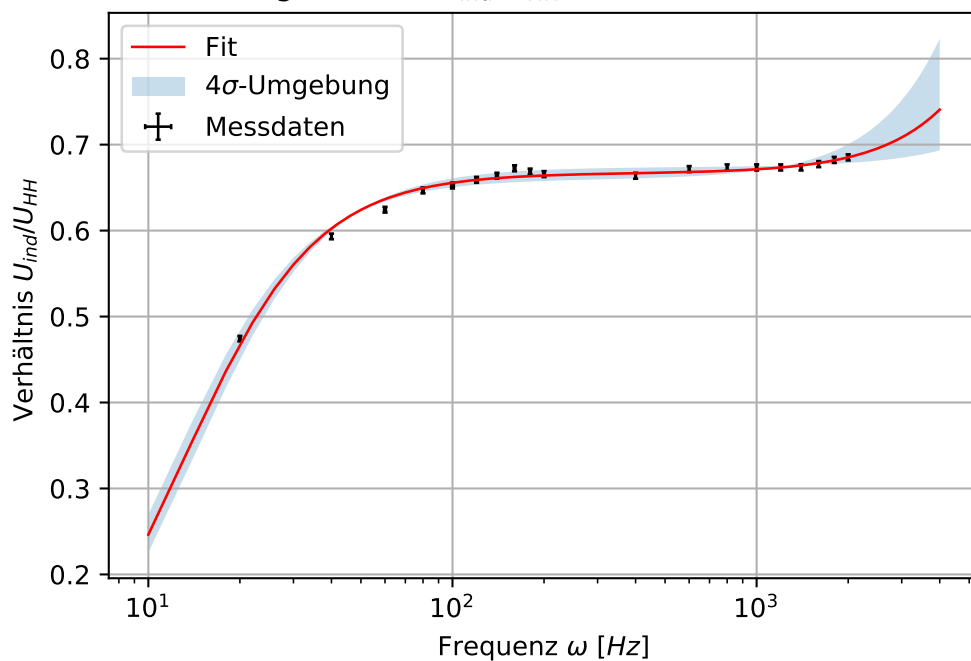
#Output
plt.savefig('figures/245_Diagramm4.pdf', format='pdf')
print('R_2/R_HH = ', abs(popt[0]), ', Standardfehler = ', perr[0])
print('L_2/R_HH [s]= ', abs(popt[1]), ', Standardfehler = ', perr[1])
print('L_HH/R_HH [s]= ', abs(popt[2]), ', Standardfehler = ', perr[2])
print('\n')
print('Chi-Quadrat = ', chisquare)
print('Freiheitsgrade = ', dof)
print('Chi-Quadrat reduziert = ', chisquare_red)
print('Wahrscheinlichkeit ein größeres oder gleiches Chi-Quadrat zu erhalten = '+str(prob)+'%')

R_2/R_HH = 0.816544318979079 , Standardfehler = 0.001089061039241941
L_2/R_HH [s]= 6.798774186287494e-05 , Standardfehler = 8.294132659518005e-06
L_HH/R_HH [s]= 13.065292675598439 , Standardfehler = 0.25914661572085657

Chi-Quadrat = 42.098540176005535
Freiheitsgrade = 16
Chi-Quadrat reduziert = 2.631158761000346
Wahrscheinlichkeit ein größeres oder gleiches Chi-Quadrat zu erhalten = 0.0%

```

Diagramm 4: U_{ind}/U_{HH} als Funktion von ω



```
In [5]: %matplotlib inline
import matplotlib.pyplot as plt
import numpy as np

#Messwerte aus Tabelle 4: U_HH über I_HH
f=np.array([20.0,40.0,60.0,80,100,120,140,160,180,200,400,600,800,1000,1200,1400,1600,1800,2000])
fehler_f=np.array([0.1,0.1,0.4,0.4,1,1,1,1,1,1,2,2,5,5,5,5,5,5,5])

U_HH=np.array([7.00,7.08,7.08,7.02,7.02,6.98,6.96,6.90,6.94,6.94,6.96,6.88,6.86,6.86,6.86,6.86,6.88,6.86,6.86])
fehler_U_HH=np.array([0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02,0.02])

I_HH=np.array([1.451,0.925,0.656,0.503,0.408,0.342,0.295,0.257,0.229,0.207,0.101,0.066,0.047,0.036,0.028,0.022,0.018,0.012,0.011])
fehler_I_HH=np.array([0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001,0.001])

Z_HH=U_HH/I_HH
fehler_Z_HH=np.sqrt((fehler_U_HH/U_HH)**2+(fehler_I_HH/I_HH)**2)*Z_HH

#Fitfunktion
from scipy import odr

def fit_func(p, x):
    (a, b) = p
    return np.sqrt(a**2+(b*x)**2)

model = odr.Model(fit_func)

#darzustellende Daten
x = f
y = Z_HH
delta_x = fehler_f
delta_y = fehler_Z_HH

#Startparameter
para0 = [1.0, 1.0]

data = odr.RealData(x, y, sx=delta_x, sy=delta_y)
odr = odr.ODR(data, model, beta0=para0)
out = odr.run()

#1-Sigma
popt = out.beta
```



```

perr = out.sd_beta

#Sigma-Umgebung
nstd = 32 #um n-Sigma-Umgebung zu zeichnen
popt_top = popt+nstd*perr
popt_bot = popt-nstd*perr

#Plot-Umgebung
x_fit = np.linspace(min(x)/2, max(x)*2, 1000)
fit = fit_func(popt, x_fit)
fit_top = fit_func(popt_top, x_fit)
fit_bot = fit_func(popt_bot, x_fit)

#Plot
fig, ax = plt.subplots(1)
plt.errorbar(x, y, yerr=delta_y, xerr=delta_x, lw=1, ecolor='k', fmt='none', capsize=1, label='Messdaten')
plt.title('Diagramm 5: ' + r'$Z_{HH}$' + ' als Funktion von ' + r'$\omega$')
plt.grid(True)
plt.xscale('log')
plt.xlabel('Frequenz ' + r'$\omega$' + ' ' + r'$[Hz]$')
plt.ylabel('Impedanz ' + r'$Z_{HH}$' + ' ' + r'$\Omega$')
plt.plot(x_fit, fit, 'r', lw=1, label='Fit')
ax.fill_between(x_fit, fit_top, fit_bot, alpha=.25, label=str(nstd)+r'$\sigma$'-Umgebung')
plt.legend(loc='best')

#Chi-Quadrat orthogonal
from scipy.stats import chi2

dof = x.size-popt.size
chisquare = np.sum(((fit_func([*popt], x)-y)**2)/(delta_y**2+((fit_func([*popt], x+delta_x)-fit_func([*popt], x-delta_x))/2)**2))
chisquare_red = chisquare/dof
prob = round(1-chi2.cdf(chisquare,dof),2)*100

#Output
plt.savefig('figures/245_Diagramm5.pdf', format='pdf')
print('R_HH [Ohm] = ', abs(popt[0]), ', Standardfehler = ', perr[0])
print('L_HH [H] = ', abs(popt[1]), ', Standardfehler = ', perr[1])
print('\n')
print('Chi-Quadrat = ', chisquare)
print('Freiheitsgrade = ', dof)
print('Chi-Quadrat reduziert = ', chisquare_red)
print('Wahrscheinlichkeit ein grÖßeres oder gleiches Chi-Quadrat zu erhalten = '+str(prob)+'%')

R_HH [Ohm] = 3.4508432508320737 , Standardfehler = 0.09159822413230949
L_HH [H] = 0.16943103440093077 , Standardfehler = 0.0014413789992948258

Chi-Quadrat = 185.91059927843514
Freiheitsgrade = 17
Chi-Quadrat reduziert = 10.935917604613833
Wahrscheinlichkeit ein grÖßeres oder gleiches Chi-Quadrat zu erhalten = 0.0%

```

Diagramm 5: Z_{HH} als Funktion von ω

