

## I. FORMALISM OF NON-STANDARD INTERACTIONS

Non-standard interactions are sub-leading contributions to neutrino flavor transitions arising from neutrino interactions not considered in the Standard Model. We consider matter NSIs arising from the neutral current NSIs, which exclude production and detection effects. An effective four-fermion Lagrangian for this type of interaction can be written as

$$\mathcal{L}_{\text{NC}} = -2\sqrt{2}G_F\epsilon_{\alpha\beta}^{fX} (\bar{\nu}_\alpha\gamma^\mu P_L\nu_\beta) (\bar{f}\gamma_\mu P_X f), \quad (1)$$

where NC denotes the neutral current interaction with  $f \in \{e, u, d\}$ , and  $P_X$  is the chirality projection operators with  $X \in \{L, R\}$ .

For chirality  $X$ , the NSI Hamiltonian takes the form

$$H = \frac{1}{2E}UM^2U^\dagger + \sqrt{2}G_F n_e \text{diag}(1, 0, 0) + \sqrt{2}G_F \sum_f n_f \epsilon^{fX} \quad (2)$$

We have no independent sensitivity for the chirality of  $\epsilon^{fX}$ , so we sum over these to obtain the vectorial parameter as  $\epsilon_{\alpha\beta}^{fV} = \epsilon_{\alpha\beta}^{fL} + \epsilon_{\alpha\beta}^{fR}$ . Moreover, we normalize the fermion number density  $n_f$  by the electron number density  $n_e$ . Our matter study will be wholly confined to the interior of the Earth, where we assume electrical neutrality and equal distribution of neutrons and protons, so we use the relations  $n_u/n_e \simeq n_d/n_e \simeq 3$ . The effective NSI parameters in matter now take the form

$$\begin{aligned} \epsilon_{\alpha\beta} &= \sum_{f,X} \frac{n_f}{n_e} \epsilon_{\alpha\beta}^{fX} \\ &= \epsilon_{\alpha\beta}^{eV} + 3\epsilon_{\alpha\beta}^{uV} + 3\epsilon_{\alpha\beta}^{dV} \end{aligned} \quad (3)$$

We note that our definition of  $\epsilon_{\alpha\beta}$  differs from some texts, where the quark number density is used to normalize the parameters[? ].

With the matter potential  $V = \sqrt{2}G_F n_e$ , we write

$$H = \frac{1}{2E}UM^2U^\dagger + V \begin{bmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{e\mu} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{e\tau} & \epsilon_{\mu\tau} & \epsilon_{\tau\tau} \end{bmatrix}, \quad (4)$$

where we have assumed the components of the NSI matrix to be real.

### A. Probability effects in the GeV range

In the  $\mu\tau$  sector, we have a resonance in the 20 GeV region. Any NSI parameter involving the  $\mu$  or  $\tau$  channel will dampen this resonance, with some also shifting the probability in the stationary region above 100 GeV. This ‘double effect’ of both resonance dampening and shifting happens in two cases: either when the NSI parameter shares one channel with a survival probability (e.g.  $\epsilon_{e\mu}$  and  $P_{\mu\mu}$ ), or when the sectors align (e.g.  $\epsilon_{\mu\tau}$  and  $P_{\mu\tau}$ ). The only exception to this is for  $P_{\tau\tau}$ , which due to the near-maximal mixing in the  $\mu\tau$  sector displays dampening for  $\epsilon_{e\mu}$  even though they share no channel directly. We illustrate the three different effects in Fig. 1.

Due to the lightness of  $\Delta m_{21}^2$ , the  $e$  channel has no resonance in the GeV range. Thus, the only impact that the NSI parameters considered here can have on any  $\nu_e$  probability is shifting, and this only occurs when the requirements for the ‘double effect’ are met. So except for the survival probability  $P_{ee}$ , any NSI parameter whose sector does not match the probability sector will not drastically affect it. Thus, the only off-diagonal NSI parameters that strongly affect the transition probabilities  $P_{\alpha\beta}$  are  $\epsilon_{\gamma\beta}$ , while the survival probabilities  $P_{\alpha\alpha}$  are only strongly affected by  $\epsilon_{\alpha\beta}$ .

## II. DETECTOR FORMALISM

The neutrino flux at the detector is calculated by propagating the atmospheric neutrino flux from Honda et al [1] through the Earth by solving the Schrödinger equation with the Hamiltonian from Eq. 4. The Earth density profile is taken from the PREM [2]. The baseline for a given trajectory is determined using an average neutrino production height of 15 km and an Earth radius of 6371 km. The propagation does not include neutrino absorption.

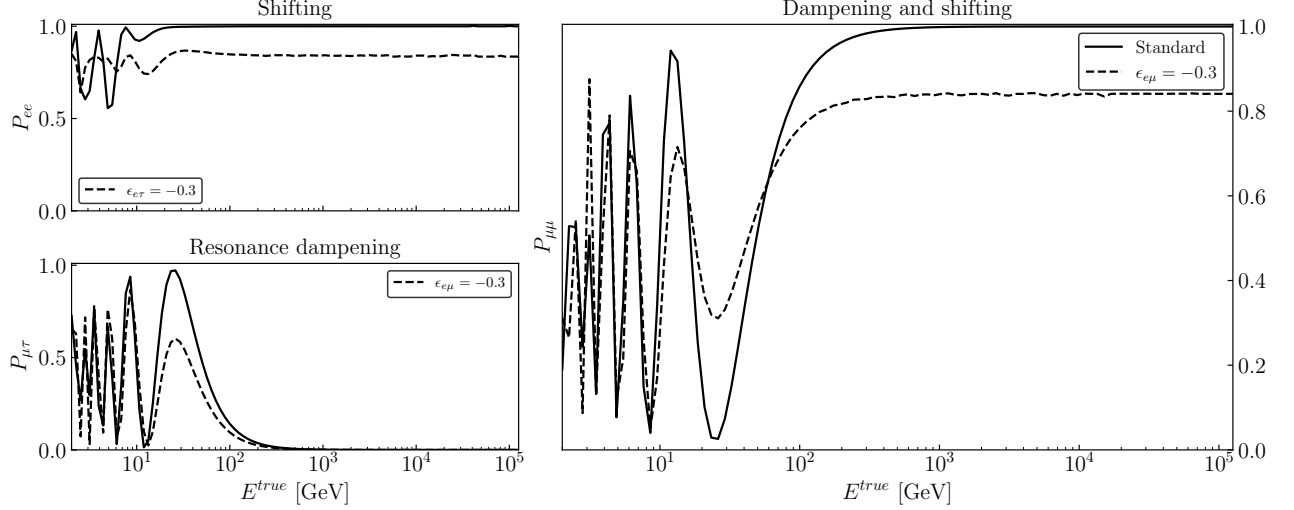


FIG. 1: The three different effects that the off-diagonal NSI parameters have in the GeV range.

The oscillation probability  $P_{\alpha\beta}$  acts as a weight to the atmospheric flux, yielding the propagated flux for flavor  $\beta$  at detector level as

$$\phi_{\beta}^{\text{det}} = \sum_{\alpha} P_{\alpha\beta} \phi_{\alpha}^{\text{atm}}, \quad (5)$$

where we sum over the initial lepton flavors  $\alpha \in \{e, \mu, \bar{e}, \bar{\mu}\}$ . To illustrate the impact of  $\epsilon_{\mu\tau}$  on both probability and flux level, we plot the flux ratios resulting from Eq. 5 in Fig. 2. In the left panel, we have marked the region in which 99% of the DeepCore cascade events originating from  $\nu_e$  and  $\nu_{\tau}$  fluxes are contained. In the right panel, we show the two regions in which 99% of the IceCube and DeepCore track events originating from  $\nu_{\mu}$  fluxes are contained. Starting with the  $\nu_{\mu}$  flux ratio, we see that the only clear signal discernible to the IceCube detector is a energy-independent flux deficiency with a factor in the order of  $\sim 10^{0.5}$  from core-crossing neutrinos within a zenith range of  $\cos(\theta_z^{\text{true}}) < -0.87$ . DeepCore on the other hand, is exposed to multiple fringes of flux surpluses with a factor in the order of  $\sim 10$ . The strongest surplus at 20 GeV is very weakly zenith dependent, a stark contrast to the energy-independent but zenith-sensitive IceCube deficiency. In IceCube, we will only consider muon track events. Thus, we have to resort to the DeepCore/PINGU detector alone for the  $\nu_e$  and  $\nu_{\tau}$  fluxes. Here we see a somewhat weaker signal, this time a zenith-independent deficiency. Where we earlier had surpluses with a factor in the order of  $\sim 10$ , we now have deficiencies in the order of  $\sim 10^{0.5}$ .

The muonic flux not only carries the largest  $\epsilon_{\mu\tau}$  effect, but it is also more abundant than the  $\nu_e$  flux. Thus, we expect to receive the highest statistics from  $\mu$ -related NSI parameters, thus constraining them the strongest.  $\epsilon_{\alpha\beta}$  which are only indirectly weakly dependent on the  $\mu$  channel will have the weakest bounds. This could be improved by considering cascade events in IceCube, thus opening up the  $e$  and  $\tau$  channels there.

### A. IceCube

We obtain the data from the IC-86 sterile data release [3], which was collected over 8 years. The event rate for each bin reads

$$N_{ij} = T \sum_{\beta} \int_{(\cos \theta_z^r)_i}^{(\cos \theta_z^r)_{i+1}} d \cos \theta_z^r \int_{E_j^r}^{E_{j+1}^r} dE^r \int_0^{\pi} R(\theta^r, \theta^t) d \cos \theta^t \int_0^{\infty} \phi_{\beta}^{\text{det}}(E^t, \theta^t) A^{\text{eff}}(E^t) R(E^r, E^t) dE^t, \quad (6)$$

where  $T$  is the live time of the detector, and  $A^{\text{eff}}$  its effective area averaged over the flavors  $\beta$  from [4].  $R(x^r, x^t)$  is a resolution function, which is responsible for the smearing between the reconstructed and true parameters  $x^r$  and  $x^t$ , respectively. We assume a log-normal distribution, giving it the form

$$R(x^r, x^t) = \frac{1}{\sqrt{2\pi} \sigma_{x^r} x^r} \exp \left[ -\frac{(\log x^r - \mu(x^t))^2}{2\sigma_{x^r}^2} \right]. \quad (7)$$

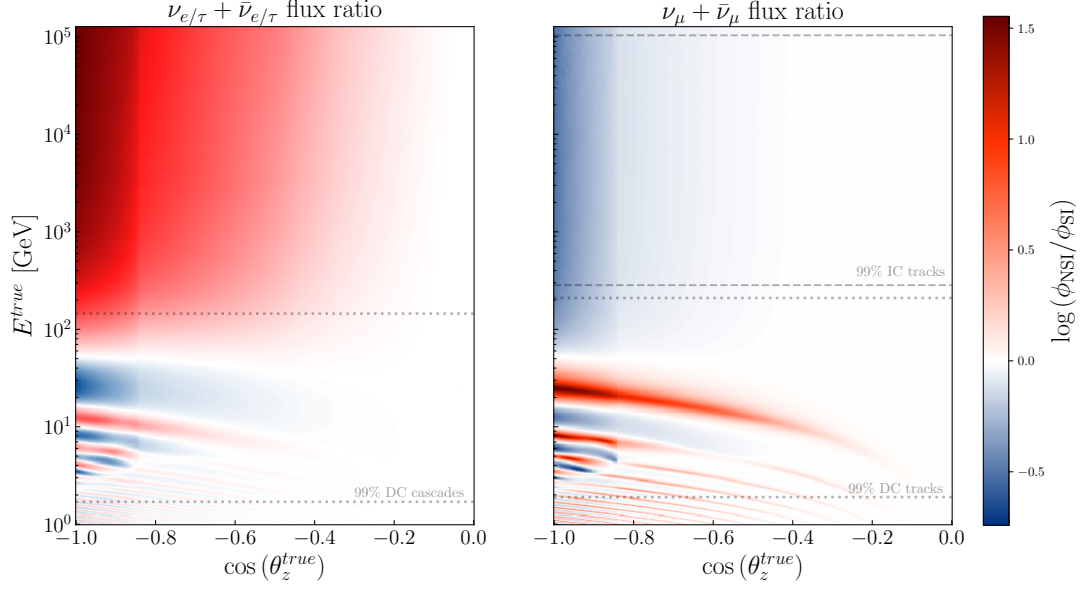


FIG. 2: Ratio of detector NSI to SI atmospheric fluxes. We set  $\epsilon_{\mu\tau} = -0.05$ , and all other  $\epsilon_{\alpha\beta} = 0$ . Within the dotted (dashed) boundaries, 99% of the DeepCore (IceCube) MC events are contained. Since we limit our IceCube study to muon tracks, a dashed region is omitted in the left panel.

However, the energy reconstruction is biased, which means that we don't assume that  $\mu(E^t) = E^r$  [5]. To model this relationship between  $E^{true}$  and  $E^{reco}$ , we train a Gaussian process regressor on the IC-86 Monte Carlo dataset from [6], from which we can extract a predicted mean and standard deviation for a given  $E^{reco}$ . We then take the  $E^{true}$  points of the 99th percentile of each distribution to obtain the limits over which to integrate. We take the angular resolution function to be identically unity since the angle resolution in IceCube for track-like events is less than  $2^\circ$ , making  $\cos(\theta_z^{true})$  practically coincide with  $\cos(\theta_z^{reco})$  for our study [3].

## B. DeepCore

We use the publically available DeepCore data sample [7] which is an updated version of what was used by the IceCube collaboration in a  $\nu_\mu$  disappearance analysis [8].

The detector systematics include ice absorption and scattering, as well as overall, lateral, and head-on optical efficiencies of the DOMs. They are applied as correction factors using the best-fit points from the DeepCore 2019  $\nu_\tau$  appearance analysis [9].

The data include 14901 track-like events and 26001 cascade-like events, both divided into eight  $\log_{10} E^{reco} \in [0.75, 1.75]$  bins, and eight  $\cos(\theta_z^{reco}) \in [-1, 1]$  bins. Each event has a Monte Carlo weight  $w_{ijk,\beta}$  from which we can construct the event count as

$$N_{ijk} = C_{ijk} \sum_{\beta} w_{ijk,\beta} \phi_{\beta}^{\det}, \quad (8)$$

where  $C_{k\beta}$  is the correction factor from the detector systematic uncertainty and  $\phi_{\beta}^{\det}$  is defined as Eq. 5. We have now substituted the effect of the Gaussian smearing by treating the reconstructed and true quantities as a migration matrix.

The oscillation parameters used on our DeepCore simulations are from the best-fit in the global analysis in [10]:  $\theta_{12} = 33.44^\circ$ ,  $\theta_{13} = 8.57^\circ$ ,  $\Delta m_{21}^2 = 7.42 \text{ eV}^2$ , and we marginalize over  $\Delta m_{31}^2$  and  $\theta_{23}$  between their  $3\sigma$  limits  $2.435 \times 10^{-3} \text{ eV}^2$  to  $2.598 \times 10^{-3} \text{ eV}^2$  and  $40.1^\circ$  to  $51.7^\circ$ , respectively.

### C. PINGU

The methodology behind the PINGU simulations is the same as with our DeepCore study IIB. We use the public Monte Carlo [11], which allows us to construct the event count as in Eq. 8. However, since no detector systematics is yet modeled for PINGU, the correction factors  $C_{ijk}$  are all unity. We will remedy this by including an uncorrelated systematic error. As with the DeepCore Monte Carlo, the PINGU Monte Carlo is divided into eight  $\log_{10} E^{reco} \in [0.75, 1.75]$  bins, and eight  $\cos(\theta_z^{reco}) \in [-1, 1]$  bins for both track- and cascade-like events. We plot the normalized event differences  $(N_{NSI} - N_{SI})/\sqrt{N_{SI}}$  for cascades and tracks in Fig. 6. We generate ‘data’ by predicting the event rates at PINGU with the following best-fit parameters from [10], except for the CP-violating phase which is set to zero for simplicity.

$$\begin{aligned} \Delta m_{21}^2 &= 7.42 \times 10^{-5} \text{ eV}^2, \quad \Delta m_{31}^2 = 2.517 \times 10^{-3} \text{ eV}^2, \\ \theta_{12} &= 33.44^\circ, \quad \theta_{13} = 8.57^\circ, \quad \theta_{23} = 49.2^\circ, \quad \delta_{CP} = 0. \end{aligned} \quad (9)$$

## III. RESULTS

In this section, we present the results from the experiments alone, as well as jointly.

### A. Methodology

For our analyses, we define our  $\chi^2$  as

$$\chi^2(\hat{\theta}, \alpha, \beta, \kappa) = \sum_{ijk} \frac{(N^{\text{th}} - N^{\text{data}})_{ijk}^2}{(\sigma_{ijk}^{\text{data}})^2 + (\sigma_{ijk}^{\text{syst}})^2} + \frac{(1 - \alpha)^2}{\sigma_\alpha^2} + \frac{\beta^2}{\sigma_\beta^2} \quad (10)$$

where we minimize over the model parameters  $\hat{\theta} \in \{\Delta m_{31}^2, \theta_{23}, \epsilon\}$ , the penalty terms  $\alpha$  and  $\beta$ , and the free parameter  $\kappa$ .  $N_{ijk}^{\text{th}}$  is the expected number of events from theory, and  $N_{ijk}^{\text{data}}$  is the observed number of events in that bin. We set  $\sigma_\alpha = 0.25$  as the atmospheric flux normalization error, and  $\sigma_\beta = 0.04$  as the zenith angle slope error [1]. The observed event number has an associated Poissonian uncertainty  $\sigma_{ijk}^{\text{data}} = \sqrt{N_{ijk}^{\text{data}}}$ . For IceCube, the event count takes the form

$$N_{ijk}^{\text{th}} = \alpha [1 + \beta(0.5 + \cos(\theta_z^{reco})_i)] N_{ijk}(\hat{\theta}), \quad (11)$$

with  $N_{ijk}(\hat{\theta})$  from Eq. 6. Here, we allow the event distribution to rotate around the median zenith angle of  $\cos(\theta_z^{reco}) = -0.5$ .

For DeepCore and PINGU, and the event count takes the form

$$N_{ijk}^{\text{th}} = \alpha [1 + \beta \cos(\theta_z^{reco})_i] N_{ijk}(\hat{\theta}) + \kappa N_{ijk}^{\mu atm}, \quad (12)$$

with  $N_{ijk}(\hat{\theta})$  from Eq. 8.  $N_{ijk}^{\mu atm}$  is the muon background, which is left to float freely in the DeepCore analysis. The background at PINGU can be considered negligible to first order [11], and we thus put  $\kappa = 0$  when calculating the PINGU  $\chi^2$ . For DeepCore and PINGU, the median zenith angle is  $\cos(\theta_z^{reco}) = 0$ , we allow the event count to rotate around this point.

We treat the uncorrelated systematic uncertainties differently for each detector. For IceCube, we set  $\sigma_{ijk}^{\text{syst}} = f \sqrt{N_{ijk}^{\text{data}}}$ . We consider best, normal, and worst-case scenarios in IceCube using  $f = 5\%$ ,  $7.5\%$ , and  $f = 15\%$  respectively. For PINGU, we use the same form but instead use  $f = 0\%$ ,  $3\%$ , and  $f = 5\%$ . For DeepCore, we use the provided systematic error distribution which accounts for uncertainties in the finite MC statistics and the data-driven muon background estimate [7]. This is summarized in Table I.

Experiment	Best case	Baseline	Worst case
IceCube	5%	10%	15%
PINGU	0%	3%	5%

TABLE I: Definition of the best, baseline, and worst case scenarios considered in each experiment, modelled by  $\sigma_{ijk}^{\text{sys}} = f\sqrt{N_{ijk}^{\text{data}}}$  with  $f$  from the table. We do not consider different DeepCore scenarios because her systematic error distribution is already provided in the data release [7].

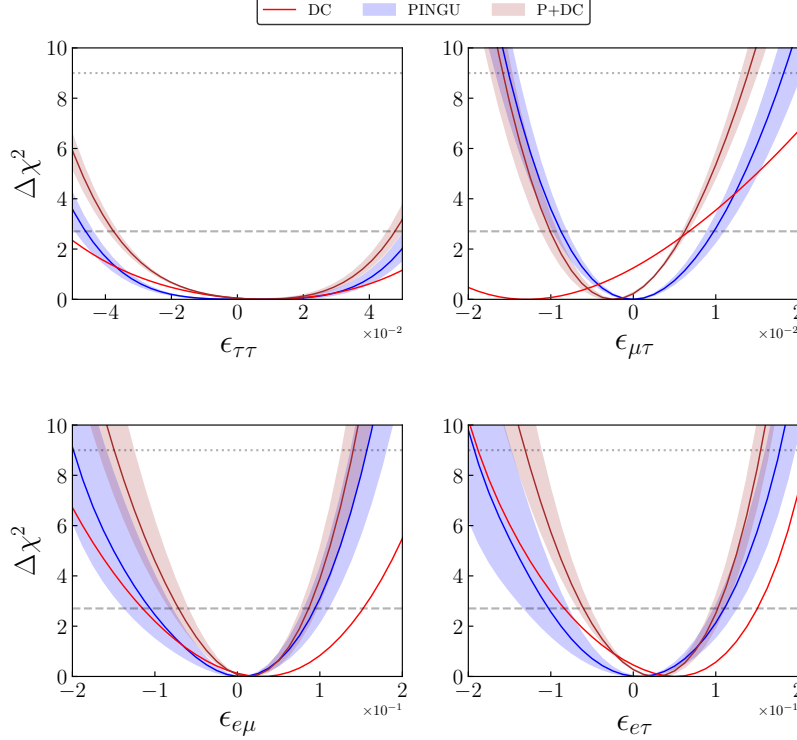


FIG. 3: PINGU and DeepCore best-case scenario, with their joint  $\Delta\chi^2$  in black.  $\Delta m_{31}^2$  and  $\theta_{23}$  and have been marginalized out, and all other NSI parameters not shown in each panel are fixed to zero. IceCube tracks only reveal  $\epsilon_{\mu\tau}$ , and are displayed separately in Fig. 4.

## B. Constraining the NSI parameters

First, we set all standard oscillation parameters to their current best-fit values of Eq. 9, except for  $\Delta m_{31}^2$  and  $\theta_{23}$ , which we marginalize over their  $3\sigma$  ranges of  $2.435 \times 10^{-3}$  to  $2.598 \times 10^{-3}$  eV<sup>2</sup> and  $40.1$  to  $51.7^\circ$  respectively. After the oscillation parameters have been marginalized out, we plot  $\Delta\chi^2$  for each of the four NSI parameters in Fig. ???. We record the confidence levels in Table II and Table III, and best-fit points in Table IV.

We see asymmetrical shapes in the  $\Delta\chi^2$  plots in Fig. 3, especially in  $\epsilon_{\mu\tau}$  and  $\epsilon_{e\tau}$ . We investigate this for  $\epsilon_{\mu\tau}$  by plotting the muon survival probability difference  $P_{\mu\mu}(\epsilon_{\mu\tau}^+) - P_{\mu\mu}(\epsilon_{\mu\tau}^-)$ , where  $\epsilon_{\mu\tau}^\pm = \pm 0.05$  in Fig. 5a. Muon events are the most abundant, and it suffices to study  $P_{\mu\mu}$  to explain the  $\epsilon_{\mu\tau}$  asymmetry. We see that positive  $\epsilon_{\mu\tau}$  generates a slightly higher  $P_{\mu\mu}$  for energies around 20 GeV (blue area), while negative  $\epsilon_{\mu\tau}$  produces higher  $P_{\mu\mu}$  for almost all other combinations of  $E_z^{\text{true}}, \cos(\theta_z^{\text{true}})$ . As we see in Fig. 2, this muon survival abundance is indeed preserved at flux level. So the flux for  $\epsilon_{\mu\tau} > 0$  is higher than the flux for  $\epsilon_{\mu\tau} < 0$ . Is this still true at event level, i.e. after reconstruction? As we see in Fig. 5b, the binned PINGU event counts display strong differences for many bins, giving a high  $\Delta\chi^2$  on both sides of  $\epsilon_{\mu\tau} = 0$  and slightly higher for  $\epsilon_{\mu\tau} = -0.01$ . DeepCore on the other hand, has fewer bins where the event count for  $\epsilon_{\mu\tau} = -0.01$  surpasses the event count for  $\epsilon_{\mu\tau} = +0.01$ , giving weaker statistics for the negative side. Thus, we conclude that the DeepCore  $\epsilon_{\mu\tau}$  asymmetry stems from the lower statistics for  $\epsilon_{\mu\tau} < 0$  at probability level, which is then preserved through the flux and finally the reconstruction.

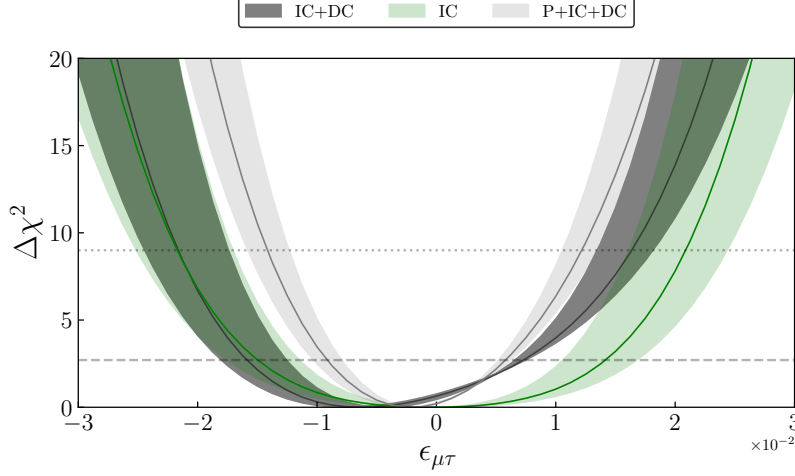


FIG. 4:  $\epsilon_{\mu\tau}$   $\Delta\chi^2$  regions for scenarios as defined in Table I.  $\Delta m_{31}^2$  and  $\theta_{23}$  and have been marginalized out, and all other NSI parameters other than  $\epsilon_{\mu\tau}$  are fixed to zero.

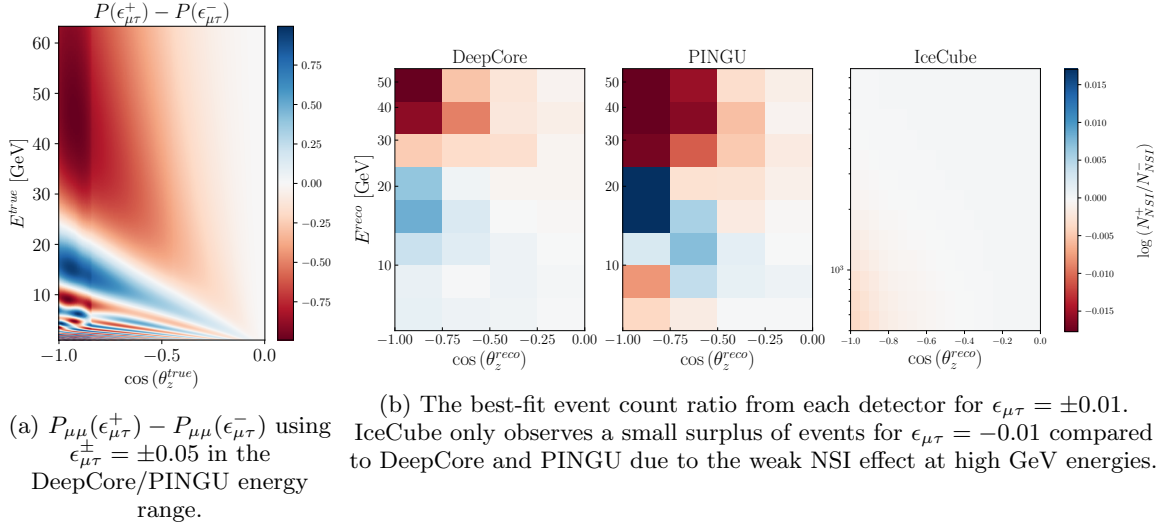


FIG. 5: Probability difference and best-fit event count. Negative  $\epsilon_{\mu\tau}$  has the strongest signal, as the thin blue region stemming from  $\epsilon_{\mu\tau} = 0.05$  is less prominent than the red regions from  $\epsilon_{\mu\tau} = -0.05$ .

Comparing Fig. 5b with the flux ratios in Fig. 2, we see that the reconstruction of PINGU is superior to DeepCore, since the event ratio  $\log(N_{NSI}^+/N_{NSI}^-)$  (which is in reconstructed quantities) more closely matches the flux ratio  $\log(\phi_{NSI}/\phi_{SI})$  (which is in true quantities). This is most evident below 20 GeV, where the DeepCore reconstruction has washed out the fringes while PINGU still has the  $N_{NSI}^-$  surplus below 10 GeV.

For the joint analysis, we follow the parameter goodness-of-fit prescription [12] and construct the joint  $\chi^2$  as

$$\chi_{\text{joint}}^2 = \sum_{\text{exp}} \chi_{\text{exp}}^2 - \chi_{\text{exp,min}}^2 \quad (13)$$

with test statistic  $\chi_{\text{joint,min}}^2$ . The  $\Delta\chi_{\text{joint}}^2$  is then  $\Delta\chi_{\text{joint}}^2 = \chi_{\text{joint}}^2 - \chi_{\text{joint,min}}^2$ . The results are shown in Fig. ?? and summarized in Tables II and III. Comparing the PINGU and the DeepCore results in Fig. 3, we note that the best-fit for each NSI parameter for the PINGU experiment is expected to be zero. This is because the ‘data’ we generated during the PINGU simulations assume no NSI since they have yet to be observed in nature. This introduces a non-NSI bias in all joint analyses which include PINGU, since PINGU has stronger statistics than DeepCore and will thus pull the joint  $\chi^2$  towards  $\epsilon = 0$ .

Parameter	Best 90% CL	Best $3\sigma$	Baseline 90% CL	Baseline $3\sigma$	Worst 90% CL	Worst $3\sigma$
IceCube						
$\epsilon_{\mu\tau}$	[-0.008, 0.009]	[-0.014, 0.017]	[-0.009, 0.01]	[-0.015, 0.018]	[-0.01, 0.011]	[-0.017, 0.02]
DeepCore						
$\epsilon_{\tau\tau}$	[-0.044, 0.051]	[-0.062, 0.069]	[-0.046, 0.054]	[-0.065]	[-0.049, 0.057]	[-0.07]
$\epsilon_{\mu\tau}$	[-0.008, 0.009]	[-0.014, 0.017]	[-0.009, 0.01]	[-0.015, 0.018]	[-0.01, 0.011]	[-0.017, 0.02]
$\epsilon_{e\mu}$	[-0.079, 0.081]	[-0.16, 0.14]	[-0.11, 0.094]	[-0.20, 0.16]	[-0.14, 0.11]	[-0.23, 0.18]
$\epsilon_{e\tau}$	[-0.079, 0.098]	[-0.15, 0.16]	[-0.10, 0.11]	[-0.19, 0.18]	[-0.13, 0.13]	[-0.23, 0.12]
IceCube + DeepCore						
$\epsilon_{\mu\tau}$	[-0.029, 0.007]	[0.026]	[-0.029, 0.007]	[0.026]	[-0.029, 0.007]	[0.026]

TABLE II: IceCube and DeepCore results from the  $\Delta\chi^2$  in Fig. 4. Best, baseline, and worst refer to the systematic uncertainty scenarios considered as in Table I.

Parameter	Best 90% CL	Best $3\sigma$	Baseline 90% CL	Baseline $3\sigma$	Worst 90% CL	Worst $3\sigma$
PINGU						
$\epsilon_{\tau\tau}$	[-0.054, 0.067]	[]	[-0.054, 0.067]	[]	[-0.054, 0.067]	[]
$\epsilon_{\mu\tau}$	[-0.029, 0.007]	[0.026]	[-0.029, 0.007]	[0.026]	[-0.029, 0.007]	[0.026]
$\epsilon_{e\mu}$	[-0.12, 0.15]	[-0.23, 0.24]	[-0.12, 0.15]	[-0.23, 0.24]	[-0.12, 0.15]	[-0.23, 0.24]
$\epsilon_{e\tau}$	[-0.084, 0.15]	[-0.19, 0.21]	[-0.084, 0.15]	[-0.19, 0.21]	[-0.084, 0.15]	[-0.19, 0.21]
DeepCore + PINGU						
$\epsilon_{\tau\tau}$	[-0.036, 0.046]	[-0.056, 0.064]	[-0.038, 0.048]	[-0.058, 0.067]	[-0.039, 0.05]	[-0.06]
$\epsilon_{\mu\tau}$	[-0.009, 0.006]	[-0.015, 0.013]	[-0.01, 0.006]	[-0.016, 0.014]	[-0.011, 0.007]	[-0.017, 0.015]
$\epsilon_{e\mu}$	[-0.06, 0.077]	[-0.126, 0.127]	[-0.071, 0.086]	[-0.149, 0.141]	[-0.082, 0.097]	[-0.17, 0.16]
$\epsilon_{e\tau}$	[-0.052, 0.095]	[-0.112, 0.144]	[-0.061, 0.103]	[-0.131, 0.155]	[-0.067, 0.11]	[-0.15, 0.17]
IceCube + DeepCore + PINGU						
$\epsilon_{\mu\tau}$	[-0.009, 0.006]	[-0.015, 0.013]	[-0.01, 0.006]	[-0.016, 0.014]	[-0.011, 0.007]	[-0.017, 0.015]

TABLE III: PINGU and joint results from the  $\Delta\chi^2$  in Fig. 3. Best, baseline, and worst refer to the systematic uncertainty scenarios considered as in Table I.

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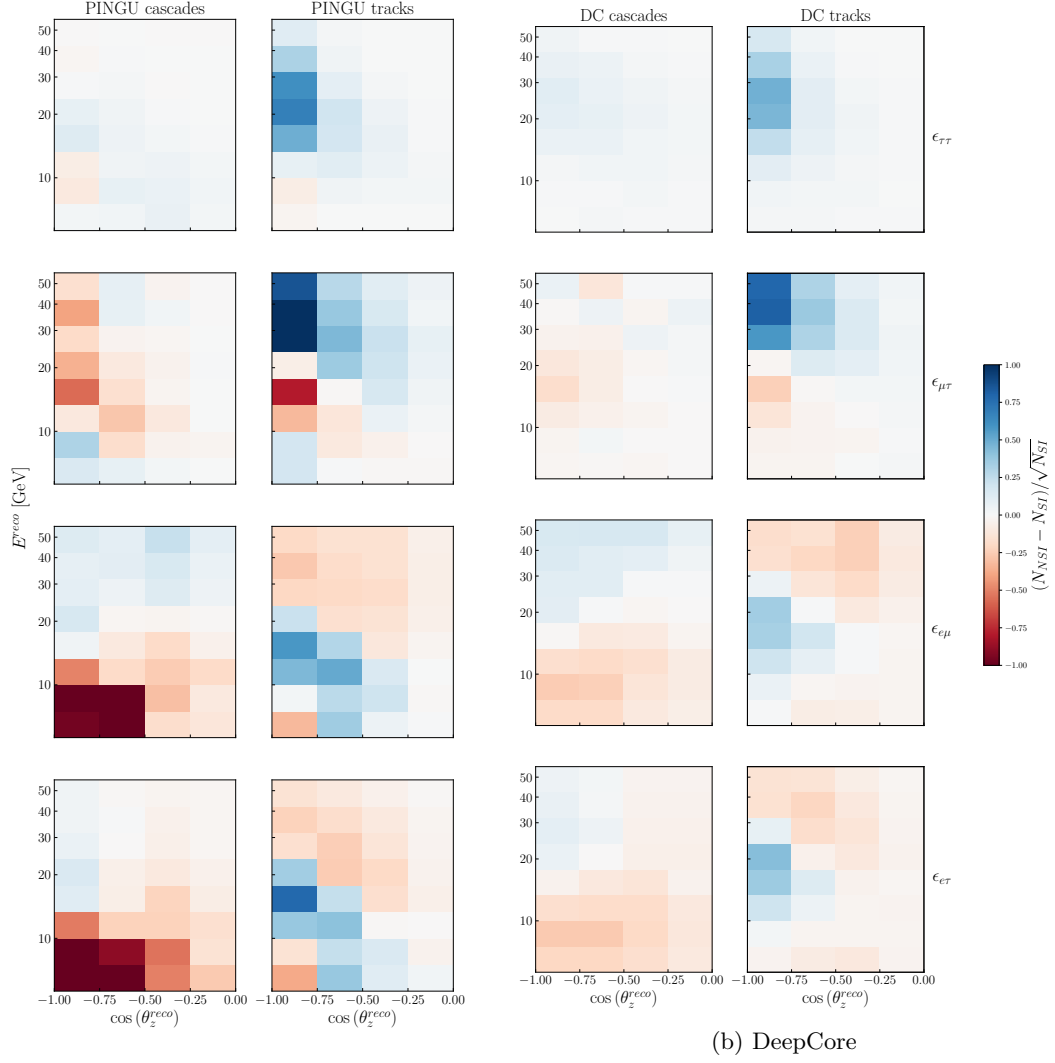
Parameter	Best fit		
	$\Delta m_{31}^2$	$\theta_{23}$	$\epsilon$
DeepCore			
$\epsilon_{\tau\tau}$	2.435	47.84	0.0125
$\epsilon_{\mu\tau}$	2.435	43.97	-0.005
$\epsilon_{e\mu}$	2.435	43.97	0
$\epsilon_{e\tau}$	2.435	43.97	0.05
IceCube			
$\epsilon_{\mu\tau}$	2.435	51.70	0
IceCube + DeepCore			
$\epsilon_{\mu\tau}$	2.517	43.97	-0.01

TABLE IV: Best fit points for  $\Delta m_{31}^2$  and  $\theta_{23}$  are given in units of  $10^{-3}\text{eV}^2$  and degrees, respectively.

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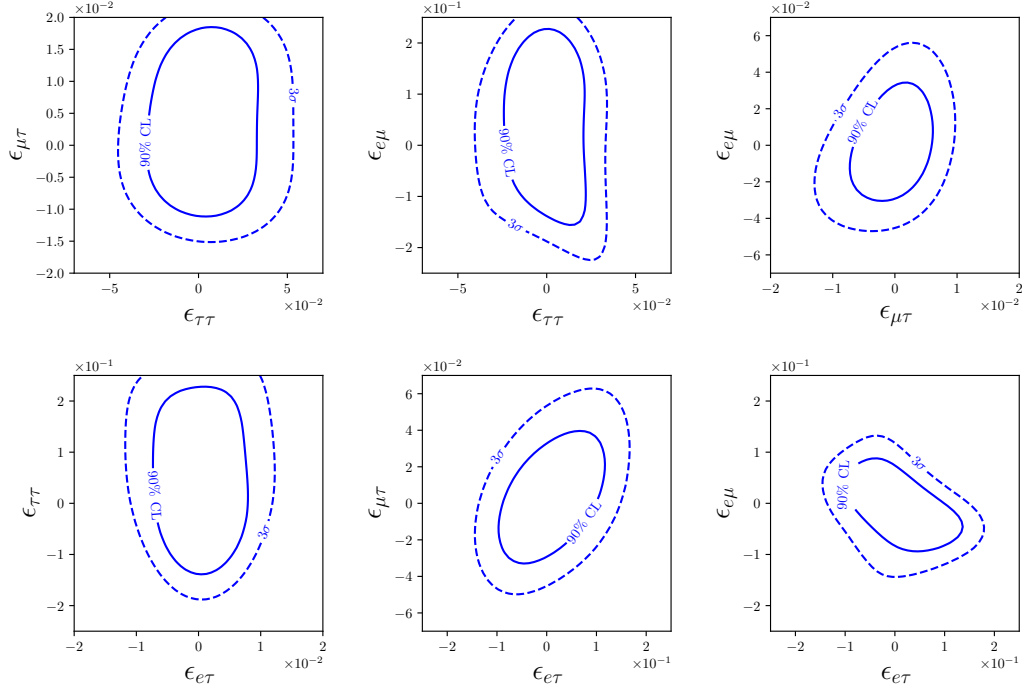
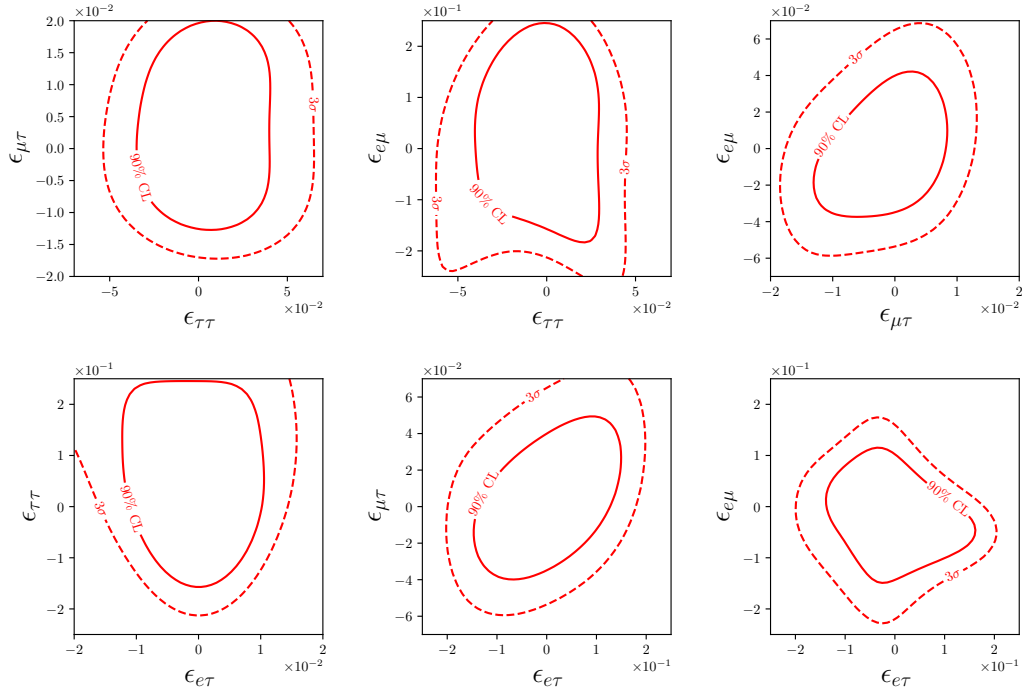




(a) PINGU

(b) DeepCore

FIG. 6: Expected pulls of the form  $(N_{NSI} - N_{SI})/\sqrt{N_{SI}}$  for PINGU and DeepCore after 3 years. We compare the NSI event count with  $\epsilon_{\mu\tau} = -0.01$  to the standard interaction count

$f = 0\%$ 

 $f = 5\%$ 


DeepCore (2017)	Demidov (2020) DC analysis	This DC+PINGU analysis
✓ Honda atmospheric fluxes	✓ Honda atmospheric fluxes	✓ Honda atmospheric fluxes
× Only look at tracks and $\epsilon_{\mu\tau}$	✓ Looks at tracks + cascades for $\epsilon_{\mu\tau}$ and $\epsilon_{\tau\tau}$	✓ Tracks and cascades for all flavors
× DC Monte Carlo from an older dataset	✓ Data and Monte Carlo from DC 2018	✓ Reco $\rightarrow$ true mapping from Monte Carlo migration matrix
× 8 E bins from 6.3 eV <sup>2</sup> to 56 eV <sup>2</sup>	✓ 8 E bins from 5.6 eV <sup>2</sup> to 56 eV <sup>2</sup>	✓ 8 E bins from 5.6 eV <sup>2</sup> to 56 eV <sup>2</sup>
× 8 z bins from -1 to 0	✓ 8 z bins from -1 to 1	✓ 8 zenith angle bins from -1 to 1
× Use "Overall" and "relative $\nu_e$ to $\nu_\mu$ " normalization	× Use "Overall" and "relative $\nu_e$ to $\nu_\mu$ " normalization	✓ Flux normalization uncertainty of 25%
× Prior on spectral index	× Prior on spectral index	✓ Zenith angle uncertainty of 4%
× No zenith angle normalization	× No zenith angle normalization	✓ No priors on oscillation parameters
✓ No priors on $\Delta m_{31}^2, \theta_{23}, \theta_{13}$	✓ No priors on $\Delta m_{31}^2, \theta_{23}$	✓ Marginalize $\Delta m_{31}^2$ and $\theta_{23}$ . All other oscillation parameters are fixed.
	✓ Fixes $\Delta m_{21}^2, \theta_{12}, \theta_{13}$	
	× Uncertainty on hadron production in atmosphere	
	× Uncertainty on neutrino nucleon cross section	