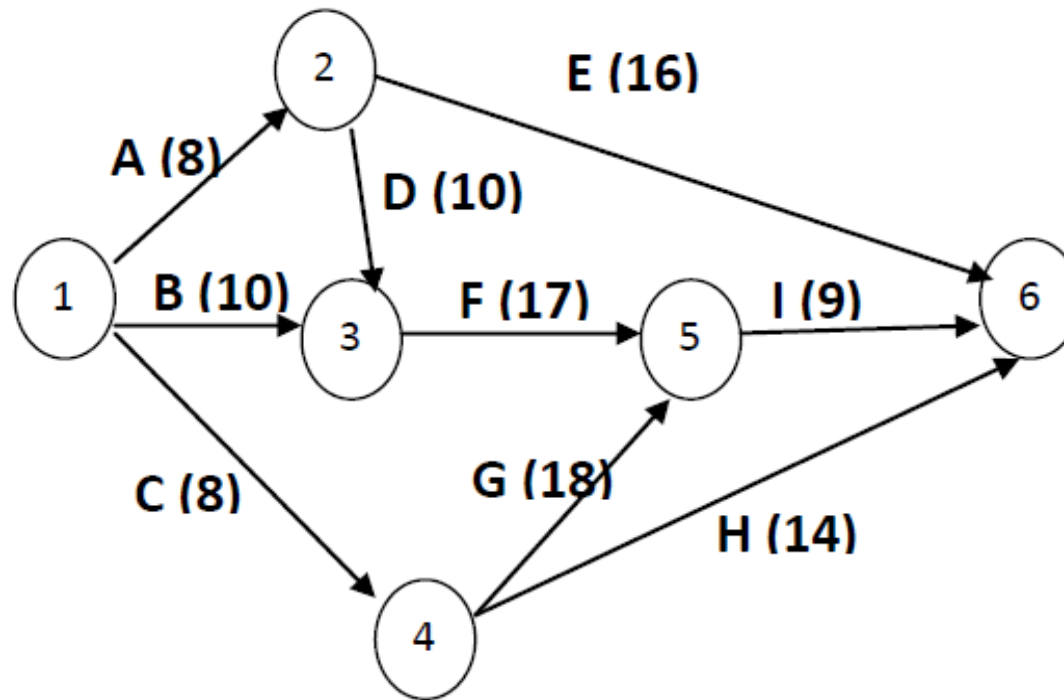
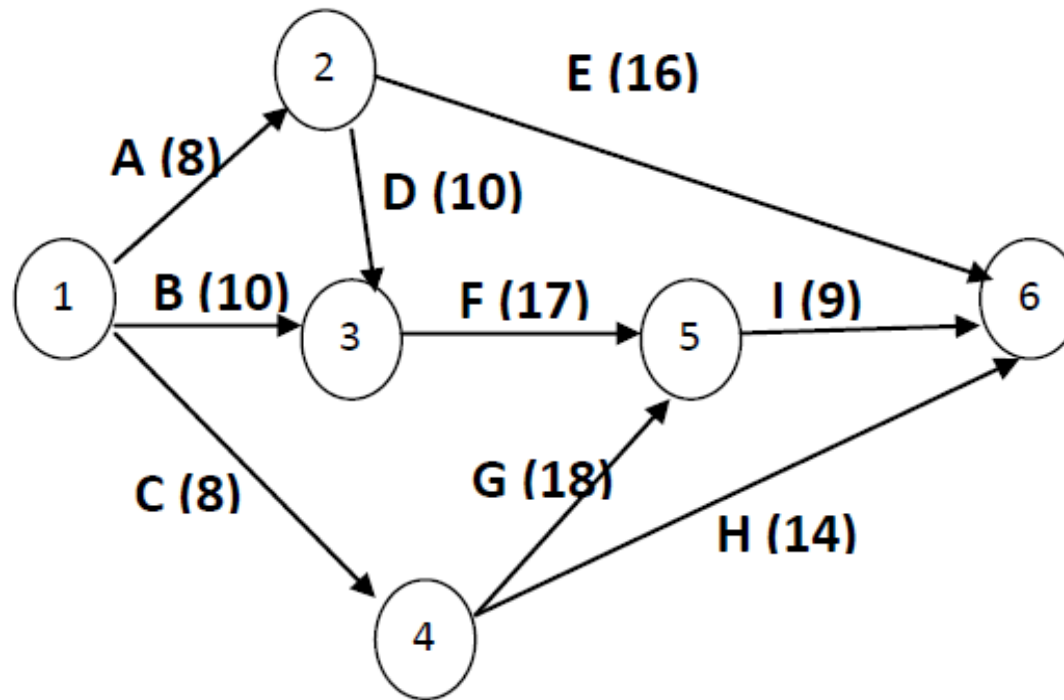


This is CPM(Critical Path Method) diagram.



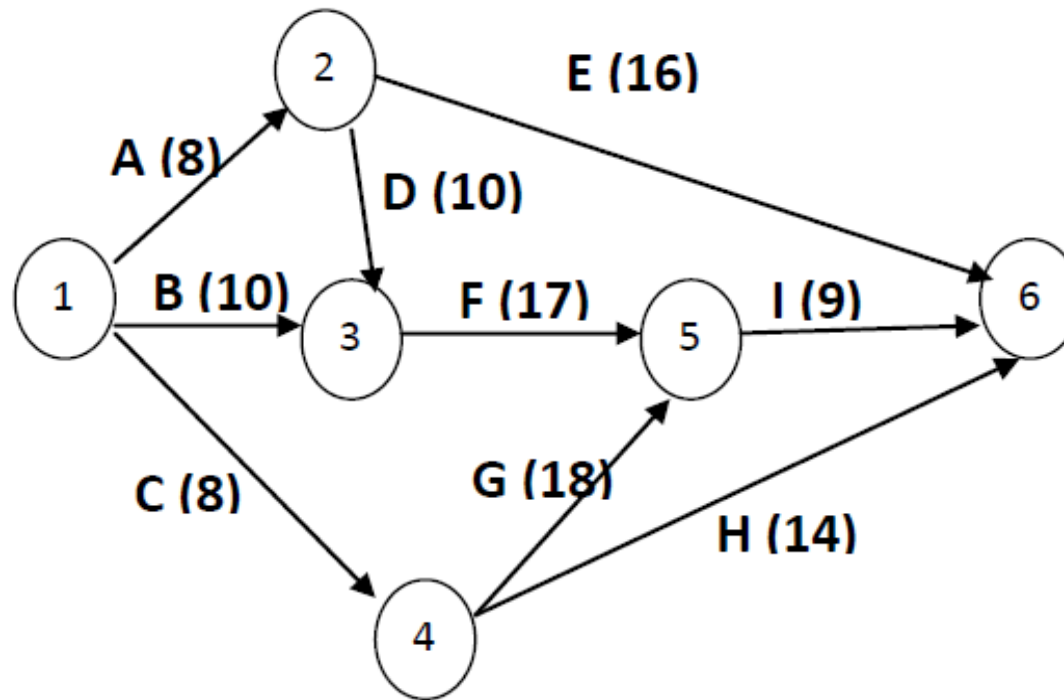
Circles: Event(Starting / Ending Points of Activity)

Edges: Activity

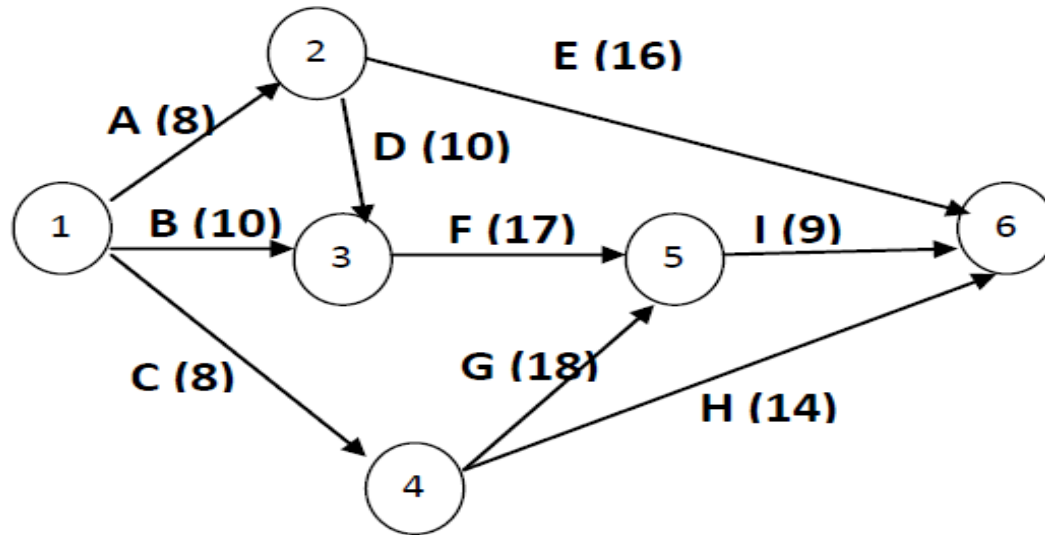


Activity	A	B	C	D	E	F	G	H	I
Duration (Days)	8	10	8	10	16	17	18	14	9

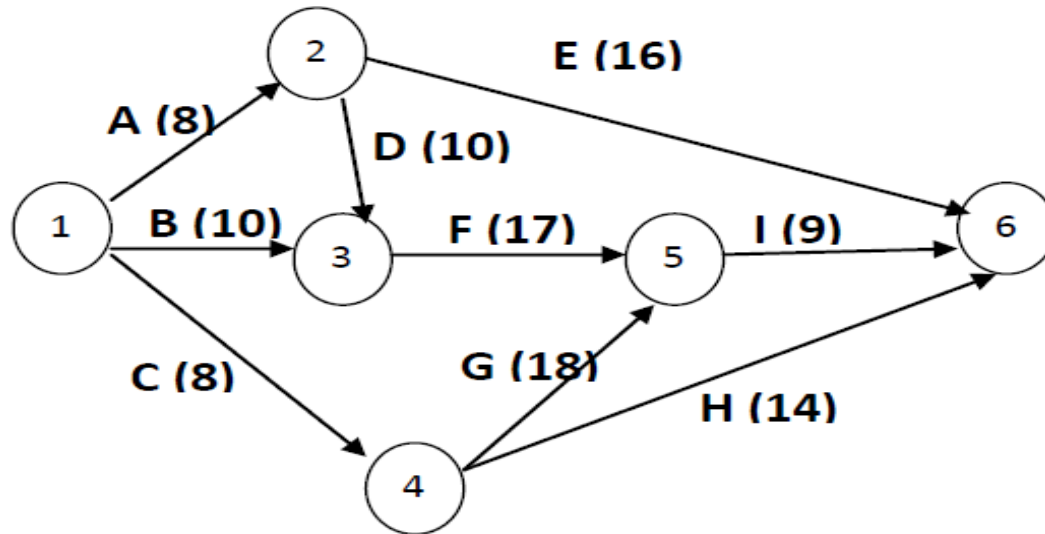
From diagram determine preceding activity



Activity	A	B	C	D	E	F	G	H	I
Duration (Days)	8	10	8	10	16	17	18	14	9
Precedence	-	-	-	A	A	B,D	C	C	F,G



**Calculate Earliest Possible Time(Days) for Event
E1,E2,E3,E4,E5,E6**



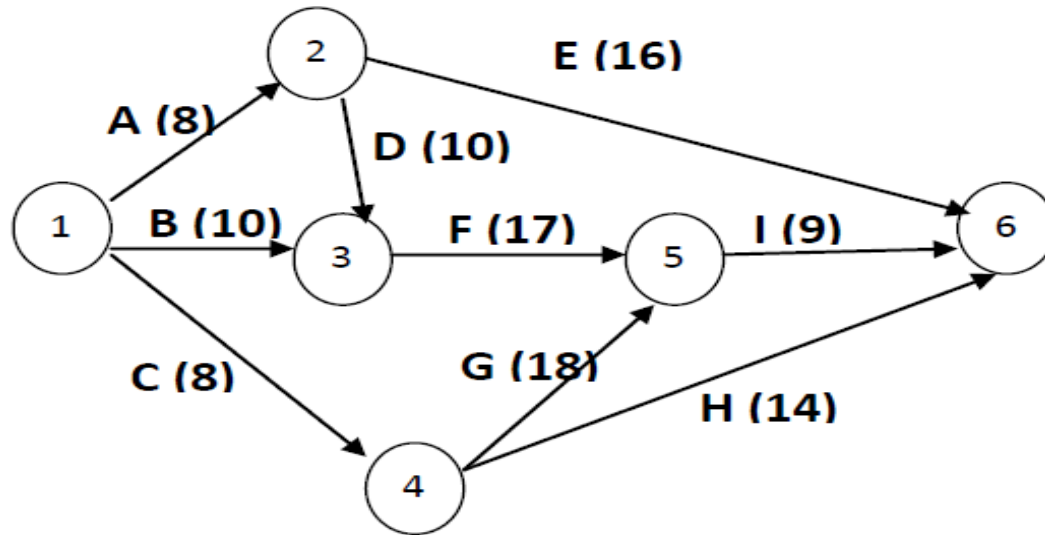
$$E_1=0, E_2=E_1+\text{Duration of A}=0+8=8$$

E3 is merged event because you see both of B and D end here. So we can write

$$E_3=E_1+\text{Duration of B}=0+10=10$$

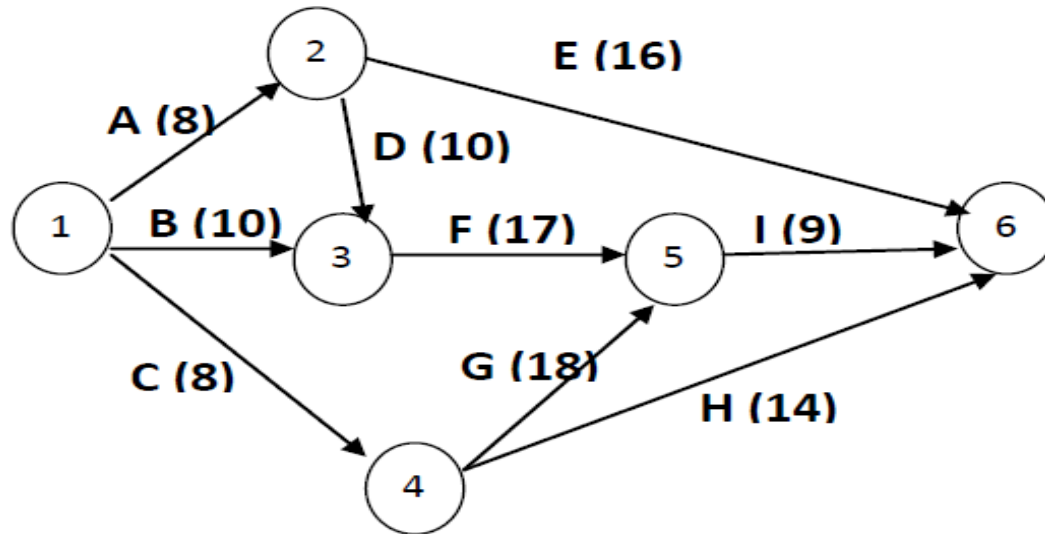
Or

$$E_3=E_2+\text{Duration of D}=8+10=18(\text{Maximum})$$



But we select $E_3 = E_2 + \text{Duration of D} = 8 + 10 = 18$
 For Merged Event like E_3 ,
 $E_3 = \max(E_1 + \text{Duration of B}, E_2 + \text{Duration of D})$
 $= \max(0 + 10, 8 + 10) = 18$

$E_4 = E_1 + \text{Duration of C} = 0 + 8 = 8$

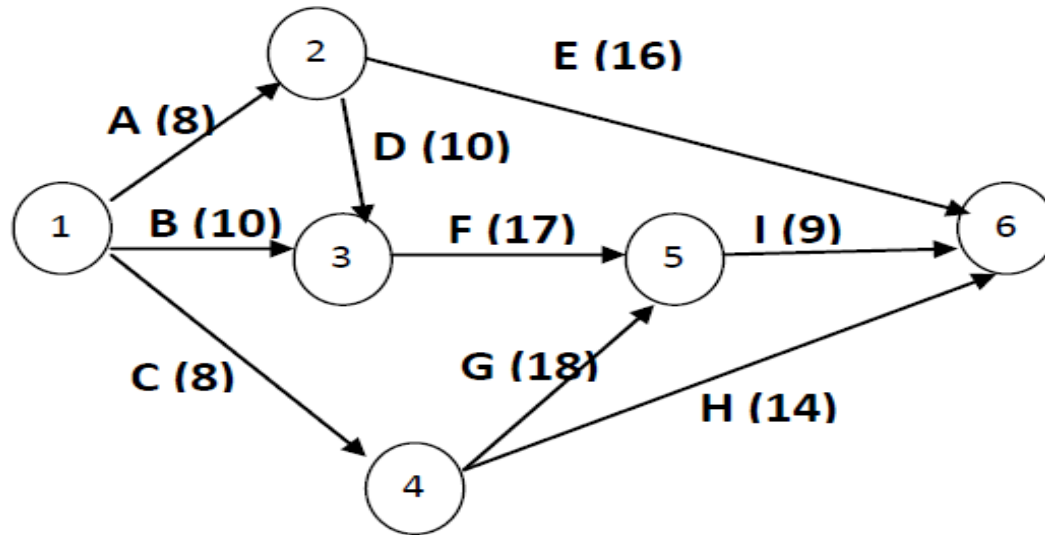


Other Merged Events(except 3):

- 1) Event-5 (Activities G and F end here)
- 2) Event-6 (Activities E,I,H end here)

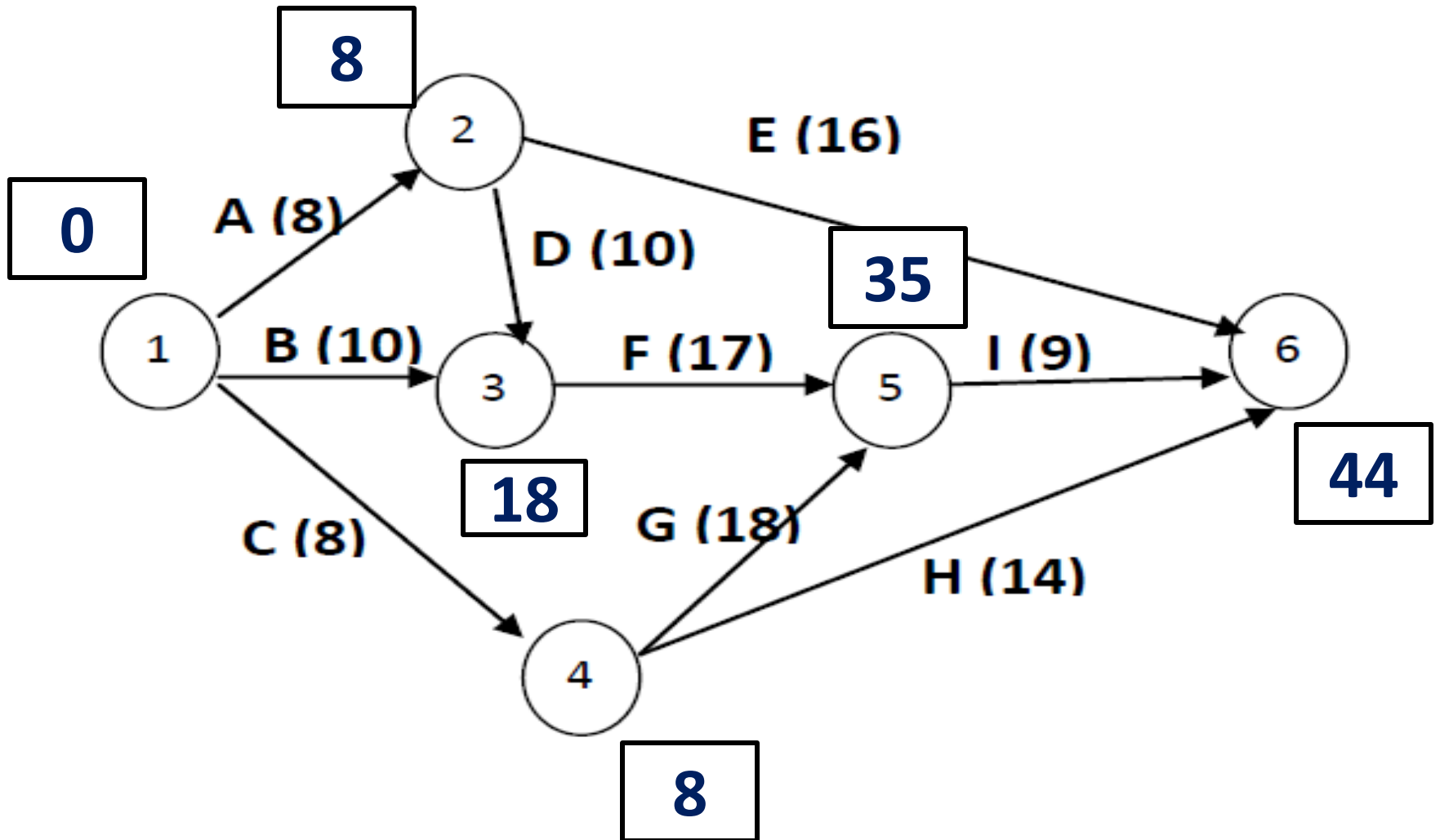
Applying same logic for the calculation of earliest possible time of E3 we find

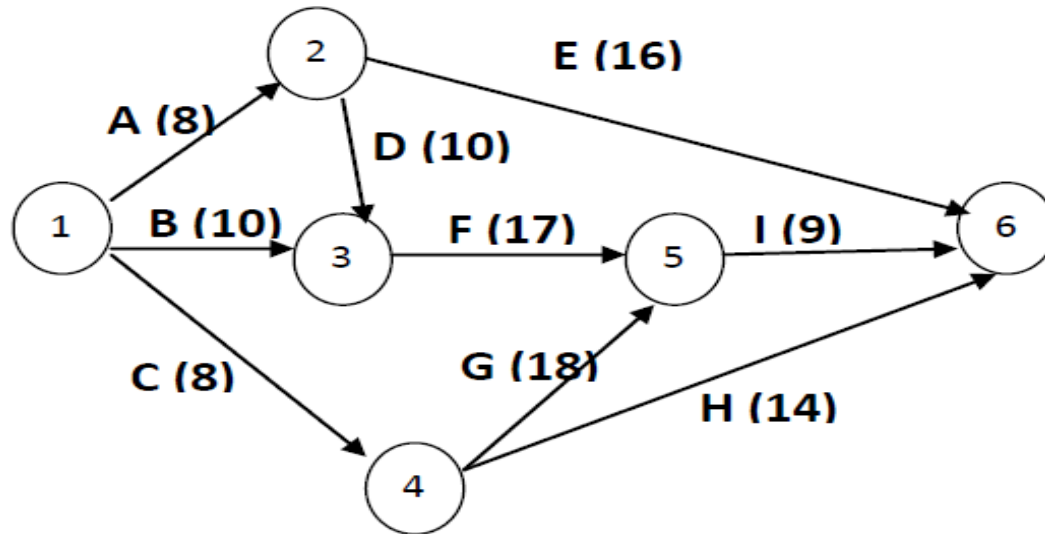
$$\begin{aligned}
 E_5 &= \max(E_4 + \text{Duration of G}, E_3 + \text{Duration of F}) \\
 &= \max(8 + 18, 18 + 17) = 35
 \end{aligned}$$



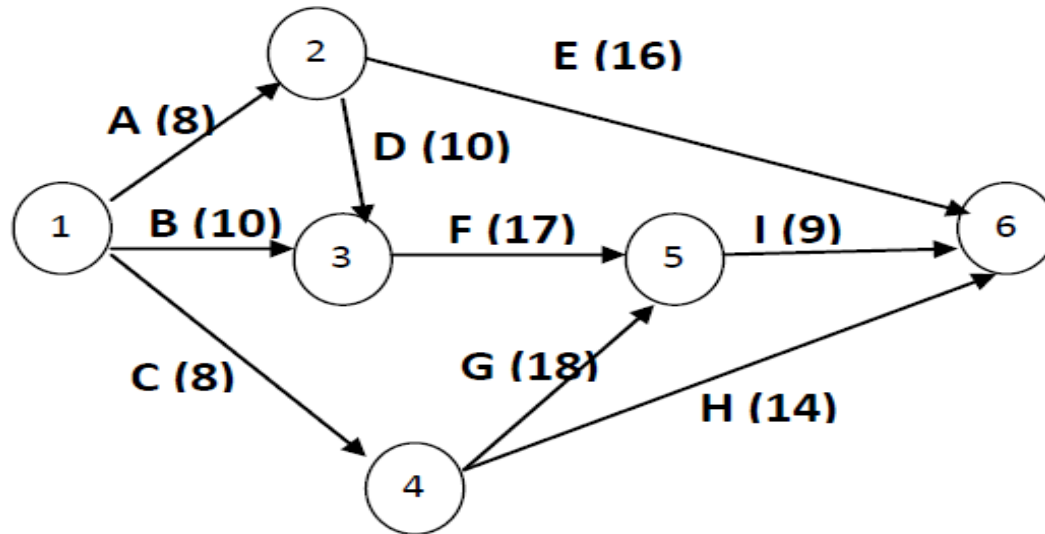
$$E_6 = \max(E_4 + \text{Duration of H}, E_2 + \text{Duration of E}, E_5 + \text{Duration of I})$$

$$= \max(8 + 14, 8 + 16, 35 + 9) = 44$$



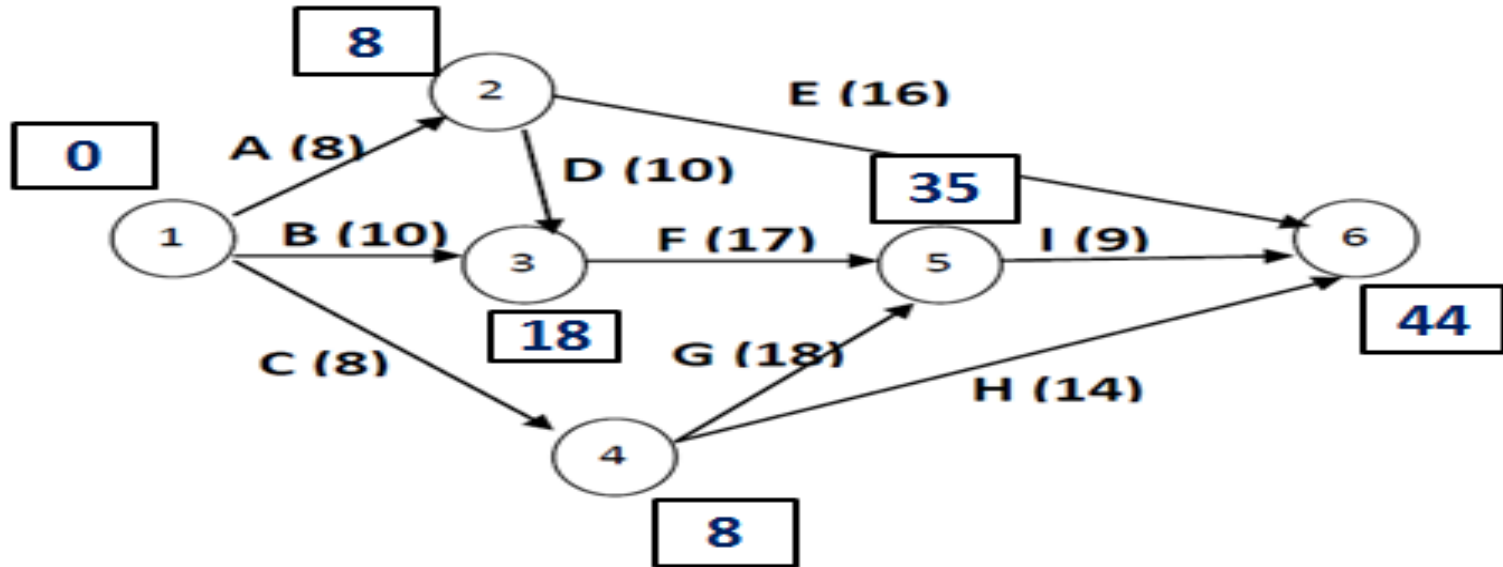


Calculate Latest Possible Time(Days) for Event
L1,L2,L3,L4,L5,L6



Find out burst events:

- 1) **Event-4: Activities G and H start from here.**
- 2) **Event-1: Activities A,B and C start from here.**
- 3) **Event-2: Activities D,E start from here**



$$L6=44$$

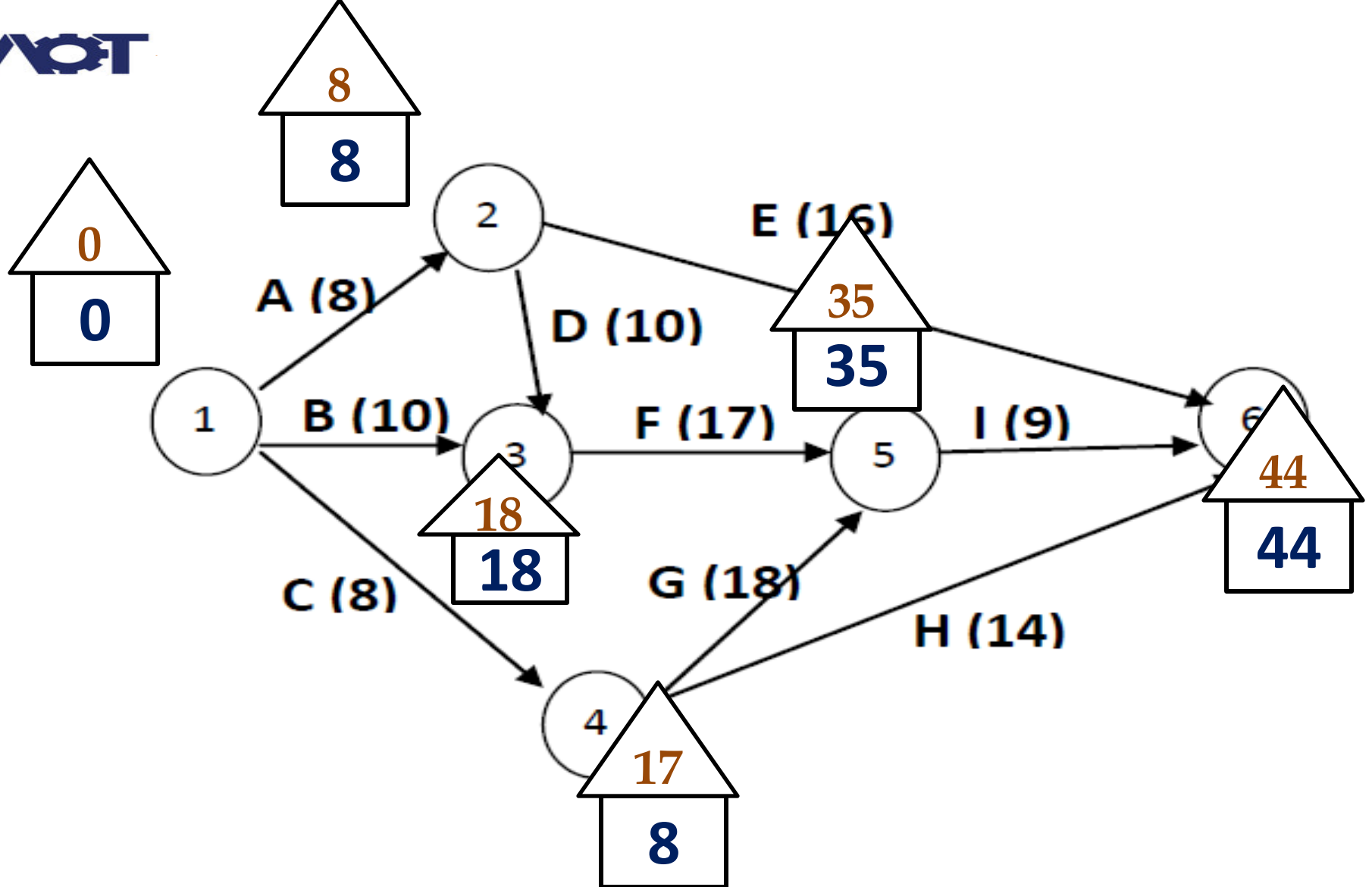
$$L5=L6 - \text{Duration of I}=35-9=44$$

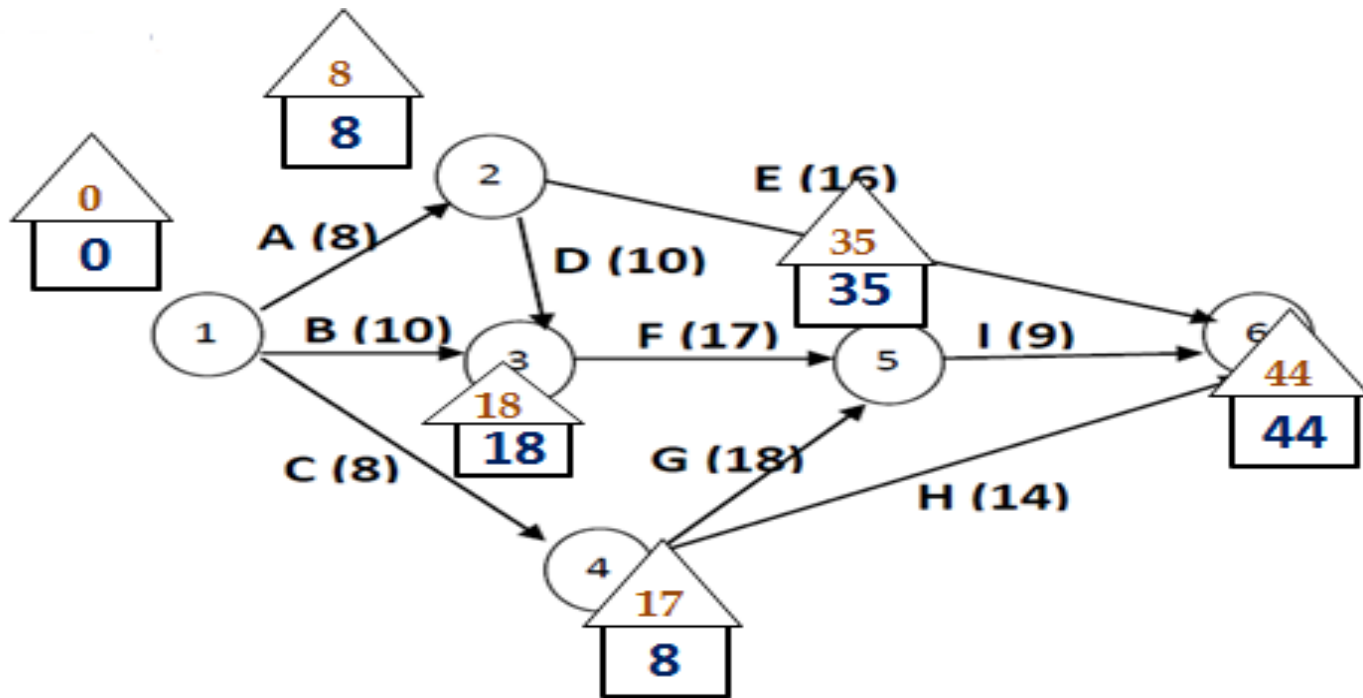
$$L4=\min(L6-\text{Duration of H}, L5-\text{Duration of G}) \\ =\min(44-14, 35-18)=17$$

$$L3=L5-\text{Duration of F}=35-17=18$$

$$L2=\min(L6-\text{Duration of E}, L3-\text{Duration of D})=\min(44-16, 18-10)=8$$

$$L1=\min(L2-\text{Duration of A}, L3-\text{Duration of B}, L4-\text{Duration of C}) \\ =\min(8-8, 18-10, 17-8)=0$$



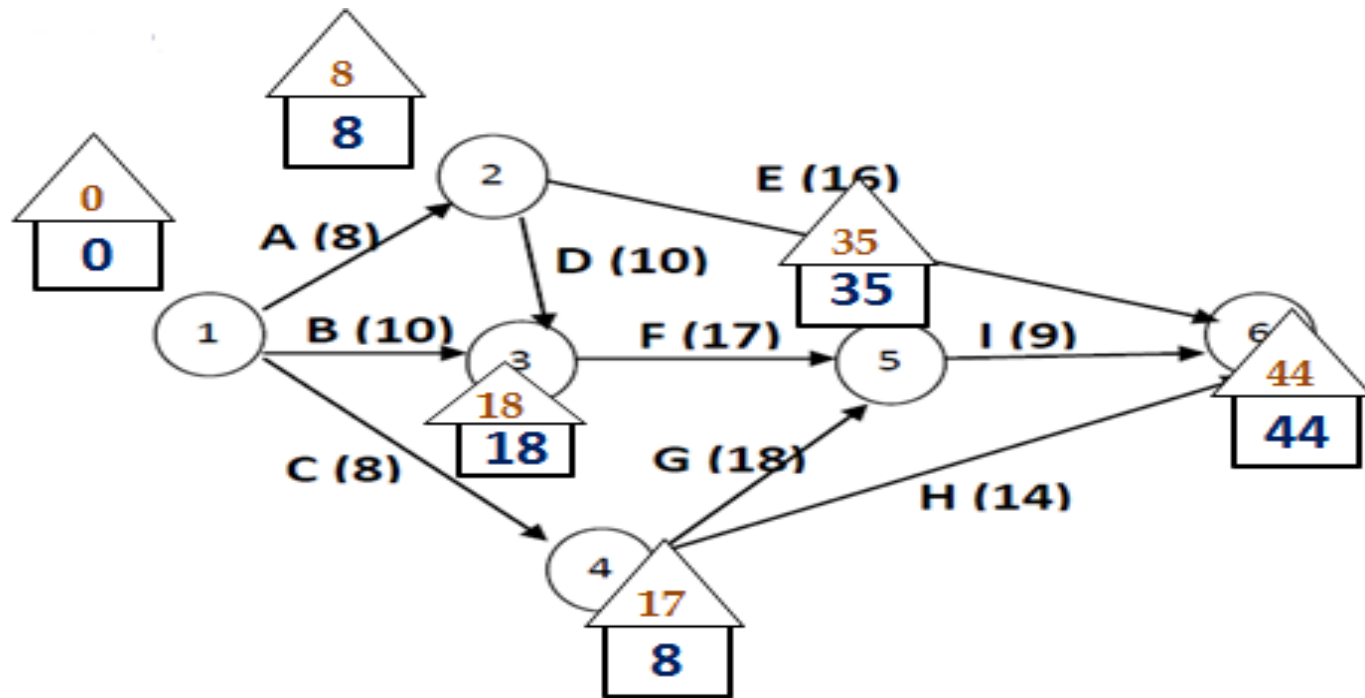


Consider an activity E:

This activity starts at Event-2 and ends at Event-6

Earliest Start Time for Event-2 is 8 days.

Latest Finish Time for Event-6 is 44 days.

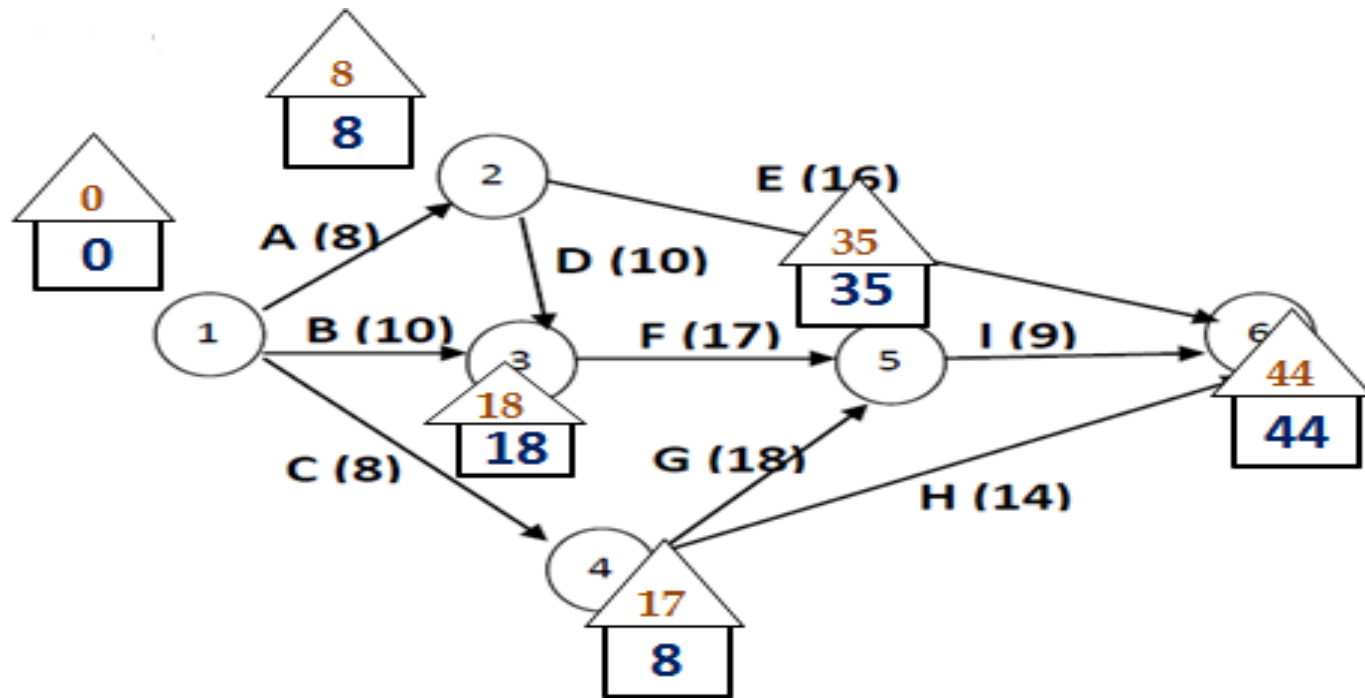


Earliest Start Time for E is Day-8.

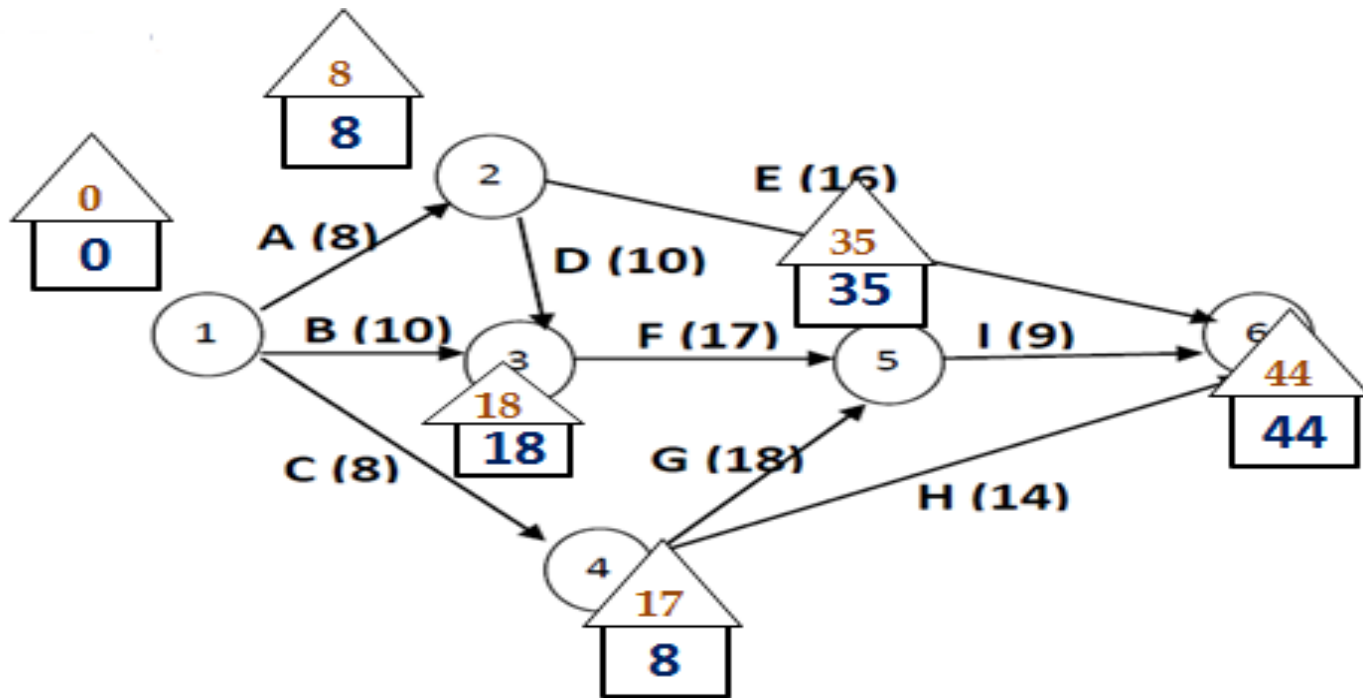
Latest Finish Time for E is 44 Day-44.

Earliest Finish Time for E is $(8 + \text{Duration of E}) = \text{Day 24}$.

Latest Finish Time for E is $(44 - \text{Duration of E}) = \text{Day 28}$



In this way we calculate ES(Earliest Start),EF(Earliest Finish),LS(Latest Start) and LF(Latest Finish) time for all activities.

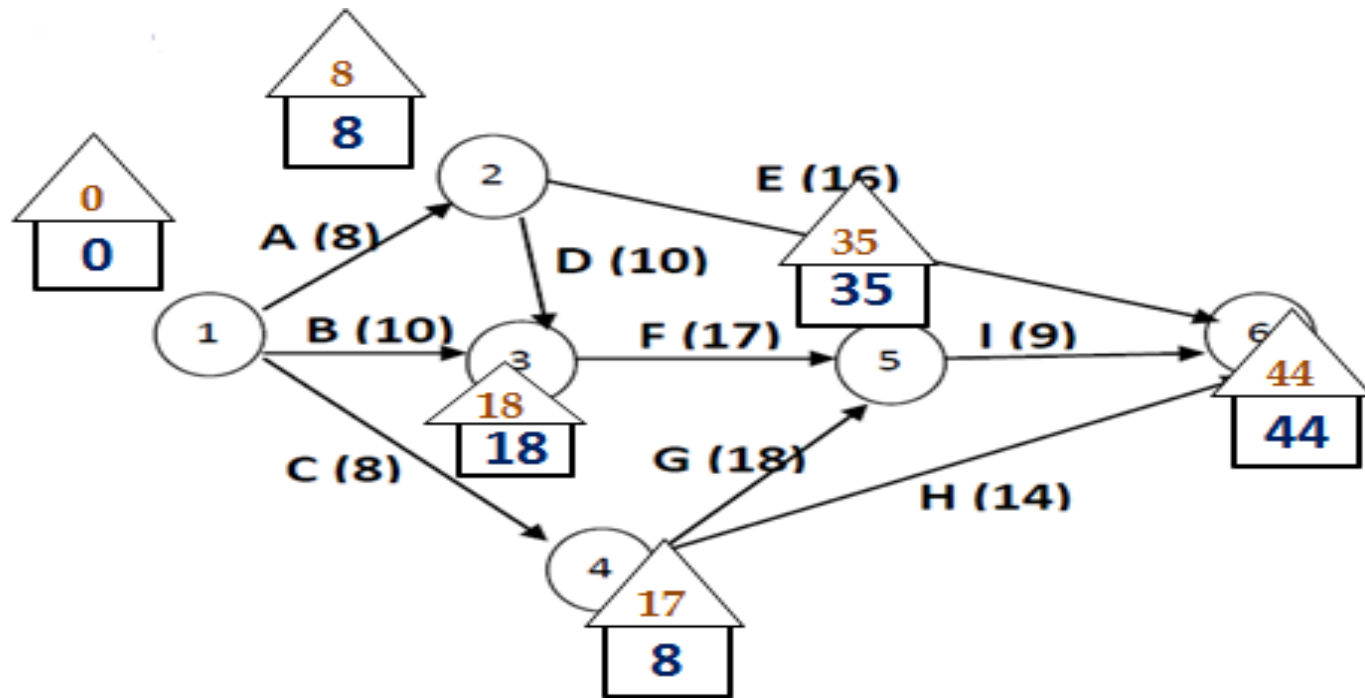


For an activity D, we find

$ES=8, EF=ES+ \text{Duration of D}=8+10=18$

$LF=18, LS=LF-\text{Duration of D}=18-10=8$

Now Total Float(TF) of D = $(LS-ES)$ or $(LF-EF) = (8-8)$ or $(8-8)=0$

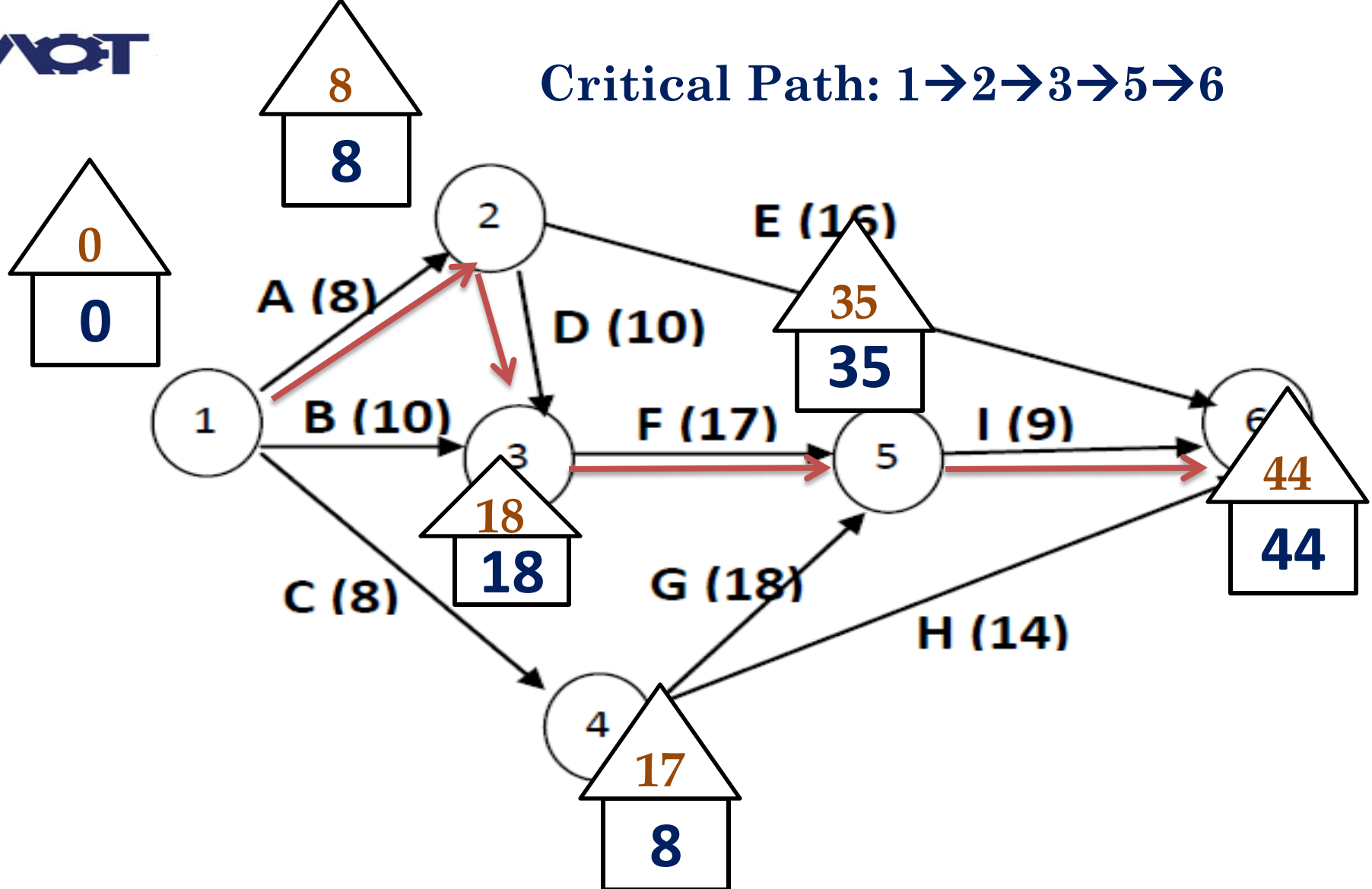


In this way, we find activities which have $TF=0$
A,D,F,I

Such activities are Critical Activities because each of them has $TF=0$.

Sequence of such activities forms Critical Path.

Critical Path: 1→2→3→5→6



**Total Duration of Project=Duration of A+ Duration of A+
Duration of D + Duration of F + Duration of I=8+10+17+9=44 Days**

