



# SJÄLVSTÄNDIGA ARBETEN I MATEMATIK

MATEMATISKA INSTITUTIONEN, STOCKHOLMS UNIVERSITET

Gröbner Bases and Elimination in Macaulay 2

av

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2026 - No 5



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Självständigt arbete i matematik 15 högskolepoäng, grundnivå

Handledare: Sofia Tirabassi

2026



## **Abstract**

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# 1 Introduction

Hello world

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