



SJÄLVSTÄNDIGA ARBETEN I MATEMATIK

MATEMATISKA INSTITUTIONEN, STOCKHOLMS UNIVERSITET

Gröbner Bases and Elimination in Macaulay 2

av

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Abstract

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1 Introduction

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2 What is Algebraic Geometry?

2.1 Polynomials

- 2.2 Affine Varieties
- 2.3 Rings and Ideals
- 2.4 Ordering Polynomials
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3 Gröbner Bases

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3.3 Properties of Gröbner Bases

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