



# SJÄLVSTÄNDIGA ARBETEN I MATEMATIK

MATEMATISKA INSTITUTIONEN, STOCKHOLMS UNIVERSITET

Gröbner Bases and Elimination in Macaulay 2

av

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# Gröbner Bases and Elimination in Macaulay 2

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Självständigt arbete i matematik 15 högskolepoäng, grundnivå

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## **Abstract**

Your summary goes here



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# 1 Introduction

Hello world [LM21]

## **2 What is Algebreic Geometry?**

**2.1 Polynomials**

**2.2 Affine Varieties**

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**2.4 Ordering Polynomials**

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## References

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