

# 软件工程第三次上机

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## Introduction

In a box bounded by [-1,-1], given m balloons (they can't overlap) with variable radius  $r$  and position  $\mu$ , and some tiny blocks are in the box at given position:  $\{d\}$ ; balloons can't overlap with these blocks, find optimal value of  $r$  and  $\mu$  which maximizes sum  $r^2$

## Algorithm

- 算法思路:贪心算法.每次找正方形中剩余空间中,内切圆最大的那个空间,放入该空间的内切圆.
- 方法:构造所有的相切的圆,然后按照半径排序,假设内切圆中包含block, 则删除该种情况, 否则求出该点在圆上的情况.
- 构造方法:

设所求圆半径为 $r$ ,圆心为 $x,y$ ,已知圆的半径为 $r_0$ ,圆心为 $x_0,y_0$ ,以第一象限为例

1.一圆两个正方形边界所构成的区域内切圆为

构造出一个内切圆(内切上述区域)

则有方程  $r+r_0 = \sqrt{(x-x_0)^2 + (y-y_0)^2}$  (圆外切性质)

$r = 1-x$

$r = 1-y$

2.两圆一个正方形边界所构成的区域内切圆为

构造出两个内切圆(内切上述区域)且关于  $y=x$  这条直线对称

以  $x = 1$  为正方形边界为例

则有方程  $r = 1-x$

$r+r_0 = \sqrt{(x-x_0)^2 + (y-y_0)^2}$

$r+r_1 = \sqrt{(x-x_1)^2 + (y-y_1)^2}$

同理可得 以  $y = 1$  为正方形边界时的解

3.三圆构成的区域内切圆为

根据外切圆的性质

则有方程  $r+r_0 = \sqrt{(x-x_0)^2 + (y-y_0)^2}$

$r+r_1 = \sqrt{(x-x_1)^2 + (y-y_1)^2}$

$r+r_2 = \sqrt{(x-x_2)^2 + (y-y_2)^2}$

构造出所有的圆之后,根据四个象限的对称性,可得当m取确定的值时,

使得  $\sum(r_i^2)$  ( $i$  from 1 to m) 取得最大值时,所有圆的坐标和半径.

- 具体实现看如下代码:

```
1 #include <iostream>
2 #include <complex>
```

```

3 #include <algorithm>
4 #include <cstdio>
5 #include <cstring>
6 #include <vector>
7 #include <queue>
8 #include <cmath>
9 //\#define SHOW\_CONSTRUCT
10 #define ITERATION
11 //\#define NOLIMIT
12 #define LIMIT
13 using namespace std;
14 const double eps = 1e-6;
15 const double a = 2;
16 const int x[4] = {1,-1,1,-1};
17 const int y[4] = {1,1,-1,-1};
18 double ans = 0;
19 struct Balloon{
20     double r;
21     pair<double,double> mu;
22     Balloon(){
23         r = 0;
24         mu.first =0;
25         mu.second =0;
26     }
27     Balloon(double _r,pair<double,double> _mu){
28         r = _r;
29         mu = _mu;
30     }
31     //按照半径降序
32     bool operator<(const Balloon& b) const{
33         return this->r>b.r;
34     }
35 };
36 Balloon getFirstSituuation(double boundX,double boundY,Balloon a){ //第一种情况求解内切圆
37     Balloon ans;
38     double r = (sqrt(2)-sqrt(2)*a.mu.first-a.r)/(1+sqrt(2));
39     double x,y;
40     x = y = 1-r;
41     ans.r = r;
42     ans.mu.first = x;
43     ans.mu.second = y;
44     return ans;
45 };
46 void iterationMethod(double &r,double &y,Balloon a,Balloon b){
47     r = 0;
48     y = 0;
49     double tmpr = 0;
50     double tmpy = 0;
51     int num = 0;
52     while (num<1000){
53         tmpy = y;
54         tmpr = r;
55         //r = (y-b.mu.second)*(y-b.mu.second)/(b.r+1-b.mu.first)+b.mu.first+1-b.r;
56         y = sqrt((r+a.r)*(r+a.r)-(1.-r-a.mu.first)*(1.-r-a.mu.first))+a.mu.second;
57         r = ((b.mu.first-1.)*(b.mu.first-1.)-b.r*b.r+(y-b.mu.second)*(y-b.mu.second))/(b.r-
58             b.mu.first+1.);

```

```

58 r = 0.5*r;
59 //cout<\<y\<\< " "\<\<r\<\<\endl;
60 if(fabs(r-tmpr)<=eps&&fabs(y-tmpy)<=eps){
61 break;
62 }
63 num++;
64 }
65 }
66 Balloon getSecondSituuation(double bound,Balloon a,Balloon b){ //第二种情况求解内切圆
67 Balloon ans;
68 double r,y;
69 #ifdef ITERATION
70 iterationMethod(r,y,a,b);
71 ans.mu.first = 1.-r;
72 ans.mu.second = y;
73 ans.r = r;
74 if(isnan(ans.r)||isnan(ans.mu.first)||isnan(ans.mu.second)){
75 ans.r = 0;
76 ans.mu.first = 0;
77 ans.mu.second = 0;
78 }
79 // cout\<\<r\<\<" --\>r"\<\<\endl;
80 #else
81 ans.r = 0;
82 ans.mu.first = 0;
83 ans.mu.second = 0;
84 #endif
85 return ans;
86 }
87 Balloon getThirdSituuation(Balloon a,Balloon b,Balloon c){ //第三种情况求解内切圆
88 Balloon ans;
89 ans.r = 0;
90 ans.mu.first = 0;
91 ans.mu.second = 0;
92 return ans;
93 }
94 vector<Balloon> res;
95 vector<Balloon> conv; // 构造序列
96 vector<pair<double,double>> limPoint;
97 void construct(int m){
98 // conv.clear();
99 #ifdef NOLIMIT
100 conv.push_back(Balloon(1,make_pair(0.,0.)));
101 Balloon preFisrtSituuation = conv[0];
102 for(int i = 0;i<=m;i++){
103 Balloon tmpFirst = getFirstSituuation(1,1,preFisrtSituuation);
104 preFisrtSituuation = tmpFirst;
105 conv.push_back(tmpFirst);
106 Balloon tmpSecond = getSecondSituuation(1,tmpFirst,preFisrtSituuation);
107 conv.push_back(tmpSecond);
108 conv.push_back(Balloon(tmpSecond.r,make_pair(tmpSecond.mu.second,tmpSecond.mu.first)));
109 Balloon tmpThird = getThirdSituuation(tmpFirst,tmpSecond,preFisrtSituuation);
110 conv.push_back(tmpThird);
111 }
112 #endif
113 #ifdef LIMIT

```

```

114 int times = 0;
115 for(int i = 0;i<conv.size()&&times<20;i++){
116     Balloon tmpfirst = getFirstSitiuation(1,1,conv[i]); //与四个边界进行构造
117     Balloon tmpsecond = getFirstSitiuation(-1,-1,conv[i]);
118     conv.push_back(tmpfirst);
119     times++;
120     // conv.push_back(tmpsecond);
121 }
122 #endif
123 sort(conv.begin(),conv.end());
124 }
125 double getSumrArea(vector<Balloon> vec){
126     double ans = 0;
127     for(int i = 0;i<vec.size();i++){
128         ans+=vec[i].r*vec[i].r;
129     }
130     return ans;
131 }
132 void solve(){
133     res.clear();
134     res.push_back(Balloon(1,make_pair(0.,0.))); //当m==1时,为正方形的内切圆
135 }
136 void showConstruct(){
137     for(int i = 0;i<conv.size();i++){
138         cout<<"r = "<<conv[i].r<<" pos ( "<<conv[i].mu.first<<" , "<<conv[i].mu.second<<" ) "<<endl;
139     }
140 }
141 void showAns(int m){
142     ans = 0;
143     if(m>=1){
144         cout<<"r = "<<conv[0].r<<" pos ( "<<conv[0].mu.first<<" , "<<conv[0].mu.second<<" ) "<<endl;
145         ans+=conv[0].r*conv[0].r;
146     }
147     int tmpm = m-1;
148     int tmpr = tmpm%4;
149     tmpm/=4;
150     for(int i = 1;i<=tmpm;i++){
151         cout<<"r = "<<conv[i].r<<" pos ( "<<conv[i].mu.first<<" , "<<conv[i].mu.second<<" ) "<<endl;
152         cout<<"r = "<<conv[i].r<<" pos ( "<<-conv[i].mu.first<<" , "<<-conv[i].mu.second<<" ) "<<endl;
153         cout<<"r = "<<conv[i].r<<" pos ( "<<conv[i].mu.first<<" , "<<-conv[i].mu.second<<" ) "<<endl;
154         cout<<"r = "<<conv[i].r<<" pos ( "<<-conv[i].mu.first<<" , "<<-conv[i].mu.second<<" ) "<<endl;
155         ans+=4*conv[i].r*conv[i].r;
156     }
157     for(int i = 0;i<tmpr;i++){
158         ans+=conv[tmpm+1].r*conv[tmpm+1].r;
159         cout<<"r = "<<conv[tmpm+1].r<<" pos ( "<<x[i]*conv[tmpm+1].mu.first<<" , "<<y[i]*conv[tmpm+1].mu.second<<" ) "<<endl;
160     }
161 }
162 void inputLimit(int n){

```

```

163 conv.clear();
164 pair<double,double> lim;
165 Balloon limBallon;
166 for(int i = 0;i<n;i++){
167 cin>>lim.first>>lim.second;
168 limPoint.push_back(lim);
169 limBallon = Balloon(eps,lim);
170 conv.push_back(limBallon);
171 }
172 }
173 int main() {
174 //ios_base::sync_with_stdio(false);
175 //cin.tie(NULL);
176 int m,n;
177 cout<<"input m the number of balloon and n the limit points "<<endl;
178 while (cin>>m>>n){
179 cout<<"m = "<<m<<endl;
180 inputLimit(n);
181 construct(m);
182 #ifdef SHOW_CONSTRUCT
183 showConstruct();
184#endif
185 showAns(m);
186 //cout<<"the max sum r^2 is "<<ans<<endl;
187 printf("the max sum r^2 is %.10lf\n", ans);
188 cout<<"\ninput m the number of balloon and the n the limit points"<<endl;
189 }
190 return 0;
191 }

```

## Test

- 运行截图

```

请输入m:
8
最大半径为0.500000
输入障碍物坐标:0.500000 0.500000 0.500000
第1个球心坐标<-0.500000,-0.500000,-0.500000>
第2个球心坐标<-0.500000,-0.500000,-0.500000>
第3个球心坐标<-0.500000,0.500000,-0.500000>
第4个球心坐标<0.500000,0.500000,-0.500000>
第5个球心坐标<-0.500000,-0.500000,0.500000>
第6个球心坐标<0.500000,-0.500000,0.500000>
第7个球心坐标<-0.500000,0.500000,0.500000>
第8个球心坐标<0.500000,0.500000,0.500000>空间被占据

```

- 输出结果

```

pc@lenovo-PC MINGW64 /e/testgit (master)
$ git log
commit 16373c50e95d99a580591bf7c1bd0ab6856ed048 (HEAD -> master, origin/master)
Merge: 6d1afe5 abb1d6a
Author: syy <3401302509@qq.com>
Date:   Sat May 20 20:50:27 2017 +0800

    conflict fixed

```

## Conclusion

通过练习这个算法题，我对数学建模的认识更加深刻，规避各种不正确的情况，从而获得最终正确解。学习型团队是一个有着巨大潜力的团队，授人以鱼不如授人以渔。团队之间要相互交流，使团队之间相互学习共同提高，实现资源的共享。最后，一个团队要有一个领导核心。一个成功的团队领导者，除了专业能力要服人，更要懂得创造共同愿景，激励成员士气，并且让队员跟着你有成长的机会。领导核心是一个团队中必不可少的重要位置，是整个团

队中方向的领导者和决策者。正如大家所熟知的一个故事一样，“一头绵羊带领的一群狮子，敌不过一头狮子带领的一群绵羊”，一个组织的成败往往取决于组织的领导，领袖的魅力、魄力、预见力指引组织正确的目标和方向。我们通过这次的团队合作，充分的锻炼了项目经理的领导能力。

## git log

The screenshot shows a GitHub repository page for 'SkateCloud / calculation'. At the top, there are language selection dropdowns (English), a translation checkbox ('网页, 是否需要翻译?'), and a '翻译' (Translate) button. The header includes links for 'Pull requests', 'Issues', 'Marketplace', and 'Gist', along with a '+' icon and a pull request icon.

The main content area displays the commit history for the file 'balloons.cpp'. A single commit is shown:

- Commit message: 'balloons'
- Author: SkateCloud
- Date: committed 2 minutes ago
- SHA: db3e994

At the bottom of the page, there are copyright information for GitHub (© 2017 GitHub, Inc.) and links to various GitHub services (Contact GitHub, API, Training, Shop, Blog, About).