

GCSE

Edexcel GCSE

Mathematics A 1387

Paper 5525/06

Summer 2005

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Mark Scheme (Results)



NOTES ON MARKING PRINCIPLES

1 Types of mark

M marks: method marksA marks: accuracy marks

B marks: unconditional accuracy marks (independent of M marks)

2 Abbreviations

cao -correct answer only
ft -follow through
isw -ignore subsequent working
SC: special case
oe -or equivalent (and appropriate)
dep -dependent
indep - independent

3 No working

If no working is shown then correct answers normally score full marks If no working is shown then incorrect (even though nearly correct) answers score no marks.

4 With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks. Send the response to review, and discuss each of these situations with your Team Leader.

Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks. Discuss each of these situations with your Team Leader. If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work. If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

5 Follow through marks

Follow through marks which involve a single stage calculation can be awarded without working since you can check the answer yourself, but if ambiguous do not award.

Follow through marks which involve more than one stage of calculation can only be awarded on sight of the relevant working, even if it appears obvious that there is only one way you could get the answer given.

6 Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. incorrect cancelling of a fraction that would otherwise be correct. It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

7 Probability

Probability answers must be given a fractions, percentages or decimals. If a candidate gives a decimal equivalent to a probability, this should be written to at least 2 decimal places (unless tenths).

Incorrect notation should lose the accuracy marks, but be awarded any implied method marks.

If a probability answer is given on the answer line using both incorrect and correct notation, award the marks.

If a probability fraction is given then cancelled incorrectly, ignore the incorrectly cancelled answer.

8 Linear equations

Full marks can be gained if the solution alone is given on the answer line, or otherwise unambiguously indicated in working (without contradiction elsewhere). Where the correct solution only is shown substituted, but not identified as the solution, the accuracy mark is lost but any method marks can be awarded.

9 Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in anoth

Par	Paper 5525/06					
	No	Working	Answer	Mark	Notes	
1	(a)	v - u = 5t	$\frac{v-u}{5}$	2	M1 for isolating $\pm 5t$ or $\pm t$ or for dividing through by 5 A1 oe	
	(b)	$ \begin{array}{l} x - 3 &= 5x - 25 \\ 22 &= 4x \end{array} $	$\frac{\overline{5}}{5\frac{1}{2}}$	3	M1 for $x - 3 = 5(x - 5)$ or $\frac{x}{5} - \frac{3}{5} = x - 5$	
					M1 for isolating terms in x correctly from $ax + b = cx + d$	
					A1 cao accept $5\frac{1}{2}, \frac{11}{2}, 5.5$	
2	(a)	36 ÷ (7+3+2)	21	3	M1 for $36 \div (7+3+2)$	
		"3" × 7			M1 (dep) for "3" × 7 or 3 or 2	
					A1 cao	
	(b)	$51.5 \times \frac{8.5}{100} = 4.3775$	47 or 47.1 or 47.12	4	M1 for 51.5 $\times \frac{8.5}{100}$ or 4.37(75) seen	
		51.5 - 4.3775 = 47.1225			M1 (dep) for 51.5 – "4.37(75)"	
					A1 for 47 or better	
					B1 (indep) for rounding their answer correctly to the nearest	
					whole number or 1 or 2 d.p OR	
					M1 for $51.5 \times \frac{100 - 8.5}{100}$	
					M1 for 51.5×"0.915" or 0.515 ×"91.5"	
					A1 for 47 or better	
					B1 (indep) for rounding their answer correct to the nearest whole number or 1 or 2 d.p	

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No	Working	Answer	Mark	Notes			
3	$3 \rightarrow 15$ $4 \rightarrow 48$ $3.1 \rightarrow 17.3(91)$ $3.2 \rightarrow 19.9(68)$ $3.3 \rightarrow 22.7(37)$ $3.4 \rightarrow 25.7(04)$ $3.5 \rightarrow 28.8(75)$ $3.4 \rightarrow 25.7(04)$ $3.3 \rightarrow 22.7(37)$ $3.35 \rightarrow 24.1(95375)$	3.3	4	B2 for trial between 3.3 and 3.4 inclusive (B1 for trial between 3 and 4 inclusive) B1 for different trial between 3.3 and 3.4 exclusive B1 (dep on at least one previous B1) for 3.3 NB trials should be evaluated to at least 1 dp truncated or rounded			
4 (a)		Angle in a semicircle	1	B1 oe			
(b)	$12^2 + 16^2 = 400$ $\sqrt{400} = 20$	20	3	M1 for $12^2 + 16^2$ M1 for $\sqrt{144 + 256}$ A1 cao			
(c)	$\pi \times 10^2$	314	3	M1 for $\pi \times \left(\frac{"20"}{2}\right)^2$ M1 (indep) for correct order of evaluation of $\pi \times r^2$ for any r A1 for 314 – 315 inclusive			

Paper 5525/	Paper 5525/06						
No	Working	Answer	Mark	Notes			
5 (a)	$(1 \times 10)+(3 \times 15)+(5 \times 30)+(7 \times 35)+$ $(9 \times 25)+(11 \times 5)=730$ "730" ÷ 120 = 6.08333	6.08	4	M1 for use of fx with x consistent within intervals (including end points) M1 (dep) for use of midpoints M1 (dep on 1 st M1) for use of $\frac{\sum fx}{\sum f}$ A1 6.08 to 6.085			
(b)		(10),25,55,90, 115,120	1	B1 for all correct			
(c)		graph	2	B1 ft for 5 or 6 points plotted correctly ± 1 full (2mm) square at the end of interval dep on sensible table (condone 1 addition error) B1(dep) for points joined by curve or line segments provided no gradient is negative – ignore any part of graph outside range of their points. (SC: B1 if 5 or 6 points plotted not at end but consistent within each interval and joined)			
(d)		72 – 74	2	M1 (ft dep on graph being cf) for reading from graph at 7 A1 ft ± 1 full (2 mm) square Or B2 for $72-74$			

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No	Working	Answer	Mark	Notes
6 (a)		a^7	1	B1 accept a^{4+3}
(b)		$15x^3y^4$	2	B2 cao (B1 for two of 15, x^3 , y^4 in a product)
(c)		x-1	1	B1 cao
(d)		(a+3b)(a-3b)	2	B2 for $(a + 3b)(a - 3b)$ (B1 for $(a \pm 3b)(a \pm 3b)$
7	80% = 220 $220 \div 80 \times 100$	275	3	M1 for recognising that 80% is equivalent to 220 M1 for 220 ÷ 80 × 100 oe A1 cao
8		x = 3 $y = 0.5$	3	M1 for coefficients of <i>x</i> or <i>y</i> the same followed by correct operation, condone one arithmetical error M1 (dep) for substituting found value in one equation A1 cao SC: B1 for one correct answer only if Ms not awarded
9		1.4×10^{10}	2	B2 for 1.4×10^{10} or 1.44×10^{10} (B1 for 14.4×10^{9} or $14400,000,000$ or $14000,000,000$ or 14×10^{9})

Paper 5	Paper 5525/06					
No	0	Working	Answer	Mark	Notes	
10	(a)	$\tan x = \frac{1.9}{3.2}$ $x = \tan^{-1} \left(\frac{1.9}{3.2} \right) = 30.7$	30.7	3	M1 for $\tan x = \frac{1.9}{3.2}$ or $\tan \frac{1.9}{3.2}$ M1 for $\tan^{-1} \left(\frac{1.9}{3.2} \right)$ A1 for $30.6 - 30.7$	
	(b)	90 + "30.7"	121	1	B1 (indep) ft for 90 + "30.7" rounded to 3 or 4 s.f	
	(a) (b)	$SF = \frac{12}{9}$ $\frac{12}{9} \times 6 = 8$ $SF = \frac{9}{12}, \frac{9}{12} \times 7 = 5.25$	5.25	2	M1 for $\frac{12}{9}$ or $\frac{9}{12}$ or 1.33 seen or 0.75 seen or 8 seen or $\frac{6}{9}$ or $\frac{9}{6}$ or 0.66 or 1.5 or $\frac{1}{3}$ or 3 oe seen A1 cao M1 for $\frac{BE}{7} = \frac{9}{12}$ oe A1 cao	

Pape	Paper 5525/06						
	No	Working	Answer	Mark	Notes		
12	(a)	$84 = 6.7 \pi + 2 \times 6.7 + 2a$ 2a + 13.4 = 62.95 or $2a + 34.44 = 84$	24.8	3	M1 for substituting correctly, π may be left M1 for correct rearrangement as far as $\pm 2a$ A1 for $24.7 - 24.8$		
	(b)	$P = \pi r + 2r + 2a$ $P - 2a = \pi r + 2r$ $P - 2a = (\pi + 2)r$	$\frac{P-2a}{\pi+2}$	3	M1 subtracting $2a$ from each side M1 for factorising to get $(\pi + 2)r$ A1 for $\frac{P-2a}{\pi + 2}$ oe S.C $\frac{p-2a}{5.14}$ oe is M1 M1 A0		
13		Area $\triangle ABC = \frac{1}{2} \times 14 \times 8 \times \sin 106 \ (= 53.8)$	53.8	3	M1 for ½ × 14 × 8 × sin 106 M1 (dep) for 56 × 0.961(26) or 107.6 A1 53.8 – 53.9 SC 107.6 is B2		
14	(a)		4.5	1	B1 cao		
	(b)	500 x 1.045 ²⁰ = 1205.857	1205.86	2	M1 for 500×1.045 ²⁰ A1 for 1205.85 – 1206 (SC:B1 for 705.85 – 706 no working)		

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15 (a)	$6x^2 + 11x - 10 + 6x - 4 = 25$ $6x^2 + 17x - 39 = 0$		3	M1 for an expression for the area involving either $(3x-2)(2x+5)+2(3x-2)$ or $3x(3x-2)+(3x-2)(7-x)$ or $3x(2x+5)-2(7-x)$ or $(3x-2)^2+2(3x-2)+(3x-2)(7-x)$ where in each case at least one of 2 or 3 product terms must be correct M1 (indep) for one correct expansion involving x^2 A1 for simplification to final answer		

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No	Working	Answer	Mark	Notes		
15 (b)(i)	$x = \frac{-17 \pm \sqrt{17^2 - 4 \times 6 \times (-39)}}{2 \times 6}$ $= \frac{-17 \pm \sqrt{289 + 936}}{12}$ $x = +\frac{18}{12} \text{ or } -4.33$ $x^2 + \frac{17}{6}x - \frac{39}{6} = 0$ $\left(x + \frac{17}{12}\right)^2 - \left(\frac{17}{12}\right)^2 - \frac{39}{6} = 0$	$1.5, -\frac{13}{3}$	4	M1 for $x = \frac{-17 \pm \sqrt{17^2 - 4 \times 6 \times (-39)}}{2 \times 6}$ up to signs in b & c M1 for $x = \frac{-17 \pm \sqrt{1225}}{12}$ A1 $x = 1.5$ or -4.33 , or better OR M2 for $(3x + 13)(2x - 3)$ (M1 for $(3x \pm a)(2x \pm b)$ with $ab = \pm 39$ A1 $x = 1.5$ or -4.33 , or better OR M1 for $\left(x + \frac{17}{12}\right)^2$ seen M1 $\left(x + \frac{17}{12}\right)^2 = \left(\frac{17}{12}\right)^2 + \frac{39}{6}$		
(ii)	$\left(x + \frac{17}{12}\right)^2 = \left(\frac{17}{12}\right)^2 + \frac{39}{6}$	8		A1 $x = 1.5$ or -4.33 , or better SC:M1 for answer "1.5" with no working or T & I B1 cao length = 8		

Pape	Paper 5525/06					
	No	Working	Answer	Mark	Notes	
16	(a)	$P(win) = \frac{2}{5} \times \frac{3}{5} + \frac{2}{5} \times \frac{1}{5} (= \frac{8}{25})$	$\frac{8}{25}$	3	M1 for $\frac{2}{5} \times \frac{3}{5}$ or $\frac{2}{5} \times \frac{1}{5}$ or for clearly identifying in P(R) \times P(R) + P(B) \times P(B) M1 for P(win) = " $\frac{2}{5} \times \frac{3}{5} + \frac{2}{5} \times \frac{1}{5}$ A1 for $\frac{8}{25}$, oe	
	(b)	$\frac{8}{25} \times 100 \ (=32)$ $100 \times 20 - "32" \times 50$	£4	2	M1 for $(\frac{8}{25}^{"} \times 100) \times 50$ or $\times 0.5$ A1 cao	

Paper 5525/06	Paper 5525/06						
No	Working	Answer	Mark	Notes			
17	Lower bound of 1200 is 1150 Upper bound of 60 is 65 1150 ÷ 65	17	4	B1 for 1150 or 1250 seen B1 for 65 or 55 seen M1 (Lower bound of load) ÷ (Upper bound of weight) Where 1150 ≤ LB load < 1200 and 60 < UB Weight ≤ 65 A1 for 17 requires fully correct working OR B1 for 1150 or 1250 seen B1 for 65 or 55 seen M1 (upper bound of load) ÷ (lower bound of weight) Where 1200 < UB load ≤ 1250 and 55 ≤ LB weight < 60 A1 for 22 requires fully correct working OR M2 1200 ÷ 55 A1 21.8 A1 21 requires fully correct working OR M2 1200 ÷ 65 A1 18.4(6) A1 18 requires fully correct working			
18 (a)	$3^4 x^4 y^8$	$81x^4y^8$	2	B2 for $81x^4y^8$ (B1 for 2 of 81, x^4 , y^8)			
(b)	$\frac{x(x-3)}{(x-5)(x-3)}$	$\frac{x}{x-5}$	3	B1 for $x(x-3)$ B1 for $(x-5)(x-3)$ B1 cao			

Paper 5525/06						
No	Working	Answer	Mark	Notes		
19 (a) (b)	Working $6^{2}-2^{2} = 32$ V $DVA = 2 \times \sin^{-1}(\frac{2}{6})$ OR $\cos DVA = \frac{6^{2}+6^{2}-16}{2 \times 6 \times 6}$ $= \frac{56}{72}$ $DVA = \cos^{-1}\left(\frac{56}{72}\right) = 38.94$	5.66 38.9	3 3	Notes M1 for $6^2 - 2^2$ (= 32) A1 5.65 - 5.66 M1 sinx = $\frac{2}{6}$ oe M1 for $DVA = 2 \times \sin^{-1}(\frac{2}{6})$ A1 38.9 - 38.95 OR M1 for $(\cos DVA) = \frac{6^2 + 6^2 - 4^2}{2 \times 6 \times 6}$ M1 for $DVA = \cos^{-1}(\frac{56}{72})$ A1 38.9 - 38.95		

Paper 5525/06	Paper 5525/06					
No	Working	Answer	Mark	Notes		
19 (c)	Working $AC^2 = 2^2 + 2^2 - 2 \times 2 \times 2 \times \cos 120^\circ$ $AC = \sqrt{12}$ OR $AN = 2 \times \sin 60 = \sqrt{3}$ OR $VN = \sqrt{"32" + 1} = \sqrt{33}$ $\cos AVC = \frac{6^2 + 6^2 - 12}{2 \times 6 \times 6}$ $\cos AVC = \frac{60}{72}$ OR $AVC = 2 \times \sin^{-1} \frac{\sqrt{3}}{6}$, using AN OR $AVC = 2 \times \cos^{-1} \frac{\sqrt{33}}{6}$, using VN	33.6	4	M1 for any valid method for AC or AN or VN where N is the midpoint of AC A1 for $AC^2 = 12$ or $AC = \sqrt{12}$ (= 3.46) or $AN = \sqrt{3}$ (=1.73) or $VN = \sqrt{33}$ (=5.74) M1 (indep) for correct method to find angle AVC A1 33.55 – 33.6		

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	No	Working	Answer	Mark	Notes
20	(a)	Graph translated 1 unit to the right passing through the points (-1,0), (1,2) and (2,0)		2	M1 for translation of $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$ or $\begin{pmatrix} -1 \\ 0 \end{pmatrix}$ A1 for right through the 3 points, $\pm \frac{1}{4}$ sq
	(b)	Graph stretched 2 units parallel to y-axis; passing through the points (-2,0), (0,4) and (1,0)		2	M1 for graph stretched parallel to the y-axis by scale factor 2 A1 through all 3 points; $\pm \frac{1}{4}$ sq not on grid at $x = 2$